Control System Toolbox™ Reference

MATLAB®



R2015**b**

How to Contact MathWorks



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Control System Toolbox[™] Reference

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Revision History

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Functions — Alphabetical List

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Block Reference

Functions – Alphabetical List

abs

Entrywise magnitude of frequency response

Syntax

absfrd = abs(sys)

Description

absfrd = abs(sys) computes the magnitude of the frequency response contained in the FRD model sys. For MIMO models, the magnitude is computed for each entry. The output absfrd is an FRD object containing the magnitude data across frequencies.

See Also

bodemag | sigma | fnorm

Introduced in R2006a

absorbDelay

Replace time delays by poles at z = 0 or phase shift

Syntax

```
sysnd = absorbDelay(sysd)
[sysnd,G] = absorbDelay(sysd)
```

Description

sysnd = absorbDelay(sysd) absorbs all time delays of the dynamic system model sysd into the system dynamics or the frequency response data.

For discrete-time models (other than frequency response data models), a delay of k sampling periods is replaced by k poles at z = 0. For continuous-time models (other than frequency response data models), time delays have no exact representation with a finite number of poles and zeros. Therefore, use **pade** to compute a rational approximation of the time delay.

For frequency response data models in both continuous and discrete time, absorbDelay absorbs all time delays into the frequency response data as a phase shift.

[sysnd,G] = absorbDelay(sysd) returns the matrix G that maps the initial states of the ss model sysd to the initial states of the sysnd.

Examples

Example 1

Create a discrete-time transfer function that has a time delay and absorb the time delay into the system dynamics as poles at z = 0.

```
z = tf('z',-1);
sysd = (-.4*z -.1)/(z^2 + 1.05*z + .08);
sysd.InputDelay = 3
```

These commands produce the result:

```
Sample time: unspecified
```

The display of sysd represents the InputDelay as a factor of $z^{(-3)}$, separate from the system poles that appear in the transfer function denominator.

Absorb the delay into the system dynamics.

```
sysnd = absorbDelay(sysd)
```

The display of sysnd shows that the factor of $z^{(-3)}$ has been absorbed as additional poles in the denominator.

```
Transfer function:

-0.4 z - 0.1

z^5 + 1.05 z^4 + 0.08 z^3

Sample time: unspecified

Additionally, sysnd has no input delay:

sysnd.InputDelay

ans =

0
```

Example 2

Convert "nk" into regular coefficients of a polynomial model.

Consider the discrete-time polynomial model:

 $m = idpoly(1, [0 \ 0 \ 0 \ 2 \ 3]);$

The value of the B polynomial, m.b, has 3 leading zeros. Two of these zeros are treated as input-output delays. Consequently:

sys = tf(m)

creates a transfer function such that the numerator is [0 2 3] and the IO delay is 2. In order to treat the leading zeros as regular B coefficients, use absorbDelay:

m2 = absorbDelay(m); sys2 = tf(m2);

sys2's numerator is $[0\ 0\ 2\ 3]$ and IO delay is 0. The model m2 treats the leading zeros as regular coefficients by freeing their values. m2.Structure.b.Free(1:2) is TRUE while m.Structure.b.Free(1:2) is FALSE.

See Also

totaldelay | hasdelay | pade

Introduced in R2011b

allmargin

Gain margin, phase margin, delay margin and crossover frequencies

Syntax

```
S = allmargin(sys)
S = allmargin(mag,phase,w,ts)
```

Description

S = allmargin(sys) computes the gain margin, phase margin, delay margin and the corresponding crossover frequencies of the SISO open-loop model sys. The allmargin command is applicable to any SISO model, including models with delays.

The output S is a structure with the following fields:

- GMFrequency All -180° (modulo 360°) crossover frequencies in rad/TimeUnit, where TimeUnit is the time units of the input dynamic system, specified in the TimeUnit property of sys.
- GainMargin Corresponding gain margins, defined as 1/G, where G is the gain at the -180° crossover frequency. Gain margins are in absolute units.
- PMFrequency All 0 dB crossover frequencies in rad/TimeUnit, where TimeUnit is the time units of the input dynamic system, specified in the TimeUnit property of sys).
- PhaseMargin Corresponding phase margins in degrees.
- DMFrequency and DelayMargin Critical frequencies and the corresponding delay margins. Delay margins are specified in the time units of the system for continuous-time systems and multiples of the sample time for discrete-time systems.
- Stable 1 if the nominal closed-loop system is stable, 0 otherwise.

Where stability cannot be assessed, **Stable** is set to NaN. In general, stability cannot be assessed for an frd system.

S = allmargin(mag,phase,w,ts) computes the stability margins from the frequency response data mag, phase, w, and the sample time, ts. Provide magnitude values mag

in absolute units, and phase values phase in degrees. You can provide the frequency vector w in any units; allmargin returns frequencies in the same units. allmargin interpolates between frequency points to approximate the true stability margins.

See Also

linearSystemAnalyzer | margin

Introduced before R2006a

AnalysisPoint

Points of interest for linear analysis

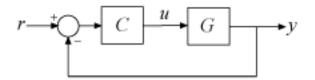
Syntax

AP = AnalysisPoint(name)
AP = AnalysisPoint(name,N)

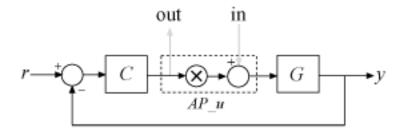
Description

AnalysisPoint is a Control Design Block for marking a location in a control system model as a point of interest for linear analysis and controller tuning. You can combine an AnalysisPoint block with numeric LTI models, tunable LTI models, and other Control Design Blocks to build tunable models of control systems. AnalysisPoint locations are available for analysis with commands such as getIOTransfer or getLoopTransfer. Such locations are also available for specifying design goals for control system tuning.

For example, consider the following control system.



Suppose that you are interested in the effects of disturbance injected at u in this control system. Inserting an AnalysisPoint block at the location u associates an implied input, implied output, and the option to open the loop at that location, as in the following diagram.



Suppose that T is a model of the control system including the AnalysisPoint block, AP_u. In this case, the command getIOTransfer(T, 'AP_u', 'y') returns a model of the closed-loop transfer function from u to y. Likewise, the command getLoopTransfer(T, 'AP_u', -1) returns a model of the negative-feedback open-loop response, CG, measured at the location u.

AnalysisPoint blocks are also useful when tuning a control system using Robust Control Toolbox[™] tuning commands such as systume. You can use an AnalysisPoint block to mark a loop-opening location for open-loop tuning requirements such as TuningGoal.LoopShape or TuningGoal.Margins. You can also use a AnalysisPoint block to mark the specified input or output for tuning requirements such as TuningGoal.Gain. For example, Req = TuningGoal.Margins('AP_u',5,40) constrains the gain and phase margins at the location *u*.

You can create AnalysisPoint blocks explicitly using the AnalysisPoint command and connect them with other block diagram components using model interconnection commands. For example, the following code creates a model of the system illustrated above. (See "Construction" on page 1-10 and "Examples" on page 1below for more information.)

```
G = tf(1,[1 2]);
C = ltiblock.pid('C','pi');
AP_u = AnalysisPoint('u');
T = feedback(G*AP u*C,1); % closed loop r->y
```

You can also create analysis points implicitly, using the connect command. The following syntax creates a dynamic system model with analysis points, by interconnecting multiple models sys1, sys2, ..., sysN:

```
sys = connect(sys1,sys2,...,sysN,inputs,outputs,APs);
```

The string vector APs lists the signal locations at which to insert analysis points. The software automatically creates and inserts an AnalysisPoint block with channels corresponding to these locations. See connect for more information.

Construction

AP = AnalysisPoint(name) creates a single-channel analysis point. Insert AP anywhere in the generalized model of your control system to mark a point of interest for linear analysis or controller tuning. name specifies the block name.

AP = AnalysisPoint(name,N) creates a multi-channel analysis point with N channels. Use this block to mark a vector-valued signal as a point of interest or to bundle together several points of interest.

Input Arguments

name

Analysis point name, specified as a string. This input argument sets the value of the Name property of the AnalysisPoint block. (See "Properties" on page 1-10.) When you build a control system model using the block, the Name property is what appears in the Blocks list of the resulting genss model.

Ν

Number of channels for a multichannel analysis point, specified as a scalar integer.

Properties

Location

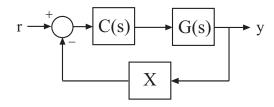
Names of channels in the AnalysisPoint blocks, specified as a string or a cell array of strings.

By default, the analysis-point channels are named after the name argument. For example, if you have a single-channel analysis point, AP, that has name 'AP', then AP.Location = 'AP' by default. If you have a multi-channel analysis point, then AP.Location = {'AP(1)', 'AP(2)',...} by default. Set AP.Location to a different value if you want to customize the channel names.

0pen

Loop-opening state, specified as a logical value or vector of logical values. This property tracks whether the loop is open or closed at the analysis point.

For example, consider the feedback loop of the following illustration.



You can model this feedback loop as follows.

```
G = tf(1,[1 2]);
C = ltiblock.pid('C','pi');
X = AnalysisPoint('X');
T = feedback(G*C,X);
```

You can get the transfer function from r to y with the feedback loop open at X as follows.

Try = getIOTransfer(T, 'r', 'y', 'X');

In the resulting generalized state-space (genss) model, the AnalysisPoint block 'X' is marked open. In other words, Try.Blocks.X.Open = 1.

For a multi-channel analysis point, then **Open** is a logical vector with as many entries as the analysis point has channels.

Default: 0 for all channels

Ts

Sample time. For AnalysisPoint blocks, the value of this property is automatically set to the sample time of other blocks and models you connect it with.

Default: 0 (continuous time)

TimeUnit

String representing the unit of the time variable. This property specifies the units for the time variable, the sample time Ts, and any time delays in the model. Use any of the following values:

- 'nanoseconds'
- 'microseconds'
- 'milliseconds'
- 'seconds'
- 'minutes'
- 'hours'
- 'days'
- 'weeks'
- 'months'
- 'years'

Changing this property has no effect on other properties, and therefore changes the overall system behavior. Use chgTimeUnit to convert between time units without modifying system behavior.

Default: 'seconds'

InputName

Input channel names. Set InputName to a string for single-input model. For a multiinput model, set InputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign input names for multi-input models. For example, if **sys** is a two-input model, enter:

sys.InputName = 'controls';

The input names automatically expand to { 'controls(1) '; 'controls(2) '}.

You can use the shorthand notation u to refer to the InputName property. For example, sys.u is equivalent to sys.InputName.

Input channel names have several uses, including:

- · Identifying channels on model display and plots
- · Extracting subsystems of MIMO systems
- · Specifying connection points when interconnecting models

Default: Empty string ' ' for all input channels

InputUnit

Input channel units. Use InputUnit to keep track of input signal units. For a singleinput model, set InputUnit to a string. For a multi-input model, set InputUnit to a cell array of strings. InputUnit has no effect on system behavior.

Default: Empty string ' ' for all input channels

InputGroup

Input channel groups. The InputGroup property lets you assign the input channels of MIMO systems into groups and refer to each group by name. Specify input groups as a structure. In this structure, field names are the group names, and field values are the input channels belonging to each group. For example:

sys.InputGroup.controls = [1 2]; sys.InputGroup.noise = [3 5];

creates input groups named controls and noise that include input channels 1, 2 and 3, 5, respectively. You can then extract the subsystem from the controls inputs to all outputs using:

sys(:,'controls')

Default: Struct with no fields

OutputName

Output channel names. Set OutputName to a string for single-output model. For a multioutput model, set OutputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign output names for multi-output models. For example, if **sys** is a two-output model, enter:

```
sys.OutputName = 'measurements';
```

```
The output names automatically expand to { 'measurements(1) '; 'measurements(2) '}.
```

You can use the shorthand notation y to refer to the OutputName property. For example, sys.y is equivalent to sys.OutputName.

Output channel names have several uses, including:

- · Identifying channels on model display and plots
- Extracting subsystems of MIMO systems
- · Specifying connection points when interconnecting models

Default: Empty string ' ' for all output channels

OutputUnit

Output channel units. Use OutputUnit to keep track of output signal units. For a single-output model, set OutputUnit to a string. For a multi-output model, set OutputUnit to a cell array of strings. OutputUnit has no effect on system behavior.

Default: Empty string ' ' for all output channels

OutputGroup

Output channel groups. The OutputGroup property lets you assign the output channels of MIMO systems into groups and refer to each group by name. Specify output groups as a structure. In this structure, field names are the group names, and field values are the output channels belonging to each group. For example:

```
sys.OutputGroup.temperature = [1];
sys.InputGroup.measurement = [3 5];
```

creates output groups named temperature and measurement that include output channels 1, and 3, 5, respectively. You can then extract the subsystem from all inputs to the measurement outputs using:

```
sys('measurement',:)
```

Default: Struct with no fields

Name

System name. Set Name to a string to label the system.

Default: ' '

Notes

Any text that you want to associate with the system. Set Notes to a string or a cell array of strings.

Default: { }

UserData

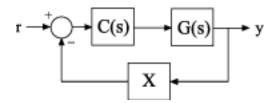
Any type of data you want to associate with system. Set $\tt UserData$ to any $\tt MATLAB^{\circledast}$ data type.

Default: []

Examples

Feedback Loop with Analysis Point

Create a model of the following feedback loop with an analysis point in the feedback path.



For this example, the plant model is G = 1/(s+2). *C* is a tunable PI controller, and *X* is the analysis point.

```
G = tf(1,[1 2]);
C = ltiblock.pid('C','pi');
X = AnalysisPoint('X');
T = feedback(G*C,X);
T.InputName = 'r';
T.OutputName = 'y';
```

T is a tunable genss model. T.Blocks contains the Control Design Blocks of the model, which are the controller, C, and the analysis point, X.

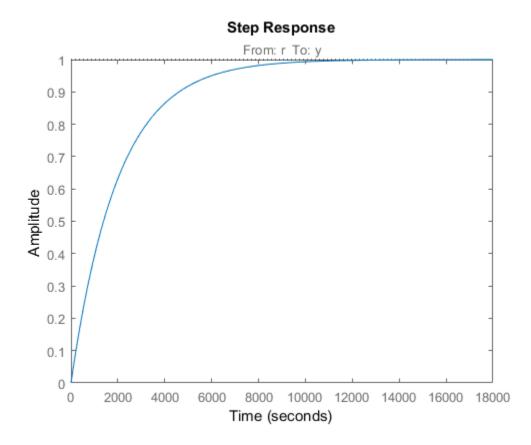
T.Blocks

ans =

C: [1x1 ltiblock.pid]
X: [1x1 AnalysisPoint]

Examine the step response of T.

stepplot(T)



The presence of the AnalysisPoint block does not change the dynamics of the model.

You can use the analysis point for linear analysis of the system. For instance, extract the system response at 'y' to a disturbance injected at the analysis point.

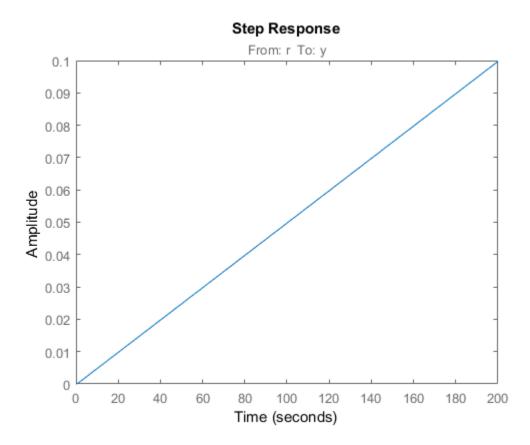
Txy = getIOTransfer(T, 'X', 'y');

The AnalysisPoint block also allows you to temporarily open the feedback loop at that point. For example, compute the open-loop response from 'r' to 'y'.

```
Try_open = getIOTransfer(T, 'r', 'y', 'X');
```

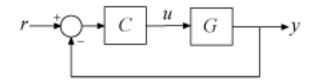
Specifying the analysis point name as the last argument to getIOTransfer extracts the response with the loop open at that point. Examine the step response of Try_open to verify that it is the open-loop response.

stepplot(Try_open);



Feedback Loop With Analysis Point Inserted by connect

Create a model of the following block diagram from r to y. Insert an analysis point at an internal location, u.



Create C and G, and name the inputs and outputs.

```
C = pid(2,1);
C.InputName = 'e';
C.OutputName = 'u';
G = zpk([],[-1,-1],1);
G.InputName = 'u';
G.OutputName = 'y';
```

Create the summing junction.

Sum = sumblk('e = r - y');

Combine C, G, and the summing junction to create the aggregate model, with an analysis point at u.

```
T = connect(G,C,Sum, 'r', 'y', 'u')
```

Τ =

Generalized continuous-time state-space model with 1 outputs, 1 inputs, 3 states, and AnalysisPoints : Analysis point, 1 channels, 1 occurrences.

Type "ss(T)" to see the current value, "get(T)" to see all properties, and "T.Blocks"

The resulting T is a genss model. The connect command creates the AnalysisPoint block, AnalysisPoints_, and inserts it into T. To see the name of the analysis point channel in AnalysisPoints_, use getPoints.

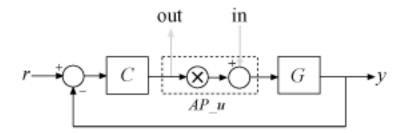
```
getPoints(T)
```

```
ans =
'u'
```

The analysis point channel is named 'u'. You can use this analysis point to extract system responses. For example, the following commands extract the open-loop transfer at u and the closed-loop response at y to a disturbance injected at u.

```
L = getLoopTransfer(T, 'u', -1);
Tuy = getIOTransfer(T, 'u', 'y');
```

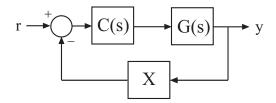
T is equivalent to the following block diagram, where AP_u designates the AnalysisPoint block AnalysisPoints_ with channel name u.



Multi-Channel Analysis Points

Create a block for marking two analysis points in a MIMO model.

In the control system of the following illustration, consider each signal a vector-valued signal of size 2. In other words, the signal r represents $\{r(1), r(2)\}$, y represents $\{y(1), y(2)\}$, and so on.



The feedback signal is therefore also a vector-valued signal of size 2.

Create a block for marking the two analysis points in the feedback path.

```
Multi-channel analysis point at locations:
   X(1)
   X(2)
Type "ss(AP)" to see the current value and "get(AP)" to see all properties.
```

The AnalysisPoint block is stored as a variable in the MATLAB workspace called AP. In addition, the Name property of the block is set to X. When you interconnect the block with numeric LTI models or other Control Design Blocks, this analysis-point block is identified in the Blocks property of the resulting genss model as X. The block name X is automatically expanded to generate the channel names X(1) and X(2).

It is sometimes convenient to change the channel names to match the names of the signals they correspond to in a block diagram of your model. For example, suppose the points of interest you want to mark in your model are signals named L and V. Change the Location property of AP to make the names match those signals.

```
AP.Location = {'L';'V'}
AP =
Multi-channel analysis point at locations:
    L
    V
Type "ss(AP)" to see the current value and "get(AP)" to see all properties.
```

Although the channel names have changed, the block name remains X.

AP.Name

ans =

Х

Therefore, the Blocks property of a genss model you build with this block still identifies the block as X. Use getPoints to find the channel names of available analysis points in a genss model.

"Control System with Multichannel Analysis Points"

More About

"Control Design Blocks"

- "Models with Tunable Coefficients"
- "Marking Signals of Interest for Control System Analysis and Design"

See Also

genss | getPoints | connect

Introduced in R2014b

append

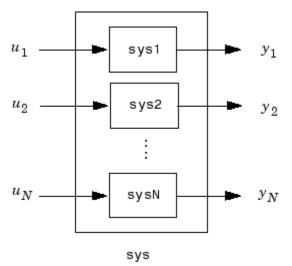
Group models by appending their inputs and outputs

Syntax

sys = append(sys1,sys2,...,sysN)

Description

sys = append(sys1,sys2,...,sysN) appends the inputs and outputs of the models sys1,...,sysN to form the augmented model sys depicted below.



For systems with transfer functions $H_1(s), \ldots, H_N(s)$, the resulting system **sys** has the block-diagonal transfer function

$\left[H_1(s)\right]$	0		0
0	$H_2(s)$		÷
:	÷	·.	0
0		0	$H_N(s)$

For state-space models **sys1** and **sys2** with data (A_1, B_1, C_1, D_1) and (A_2, B_2, C_2, D_2) , **append(sys1,sys2)** produces the following state-space model:

$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} A_1 \\ 0 \end{bmatrix}$	$ \begin{bmatrix} 0 \\ A_2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} B_1 \\ 0 \end{bmatrix} $	$\begin{bmatrix} 0 \\ B_2 \end{bmatrix} \begin{bmatrix} u_1 \\ u_2 \end{bmatrix}$
$\begin{bmatrix} y_1 \\ y_2 \end{bmatrix} = \begin{bmatrix} C_1 \\ 0 \end{bmatrix}$	$ \begin{array}{c} 0\\ C_2 \end{array} \begin{bmatrix} x_1\\ x_2 \end{bmatrix} + \begin{bmatrix} D_1\\ 0 \end{bmatrix} $	$\begin{bmatrix} 0 \\ D_2 \end{bmatrix} \begin{bmatrix} u_1 \\ u_2 \end{bmatrix}$

Arguments

The input arguments **sys1**,..., **sysN** can be model objects s of any type. Regular matrices are also accepted as a representation of static gains, but there should be at least one model in the input list. The models should be either all continuous, or all discrete with the same sample time. When appending models of different types, the resulting type is determined by the precedence rules (see "Rules That Determine Model Type" for details).

There is no limitation on the number of inputs.

Examples

The commands

sys1 = tf(1,[1 0]); sys2 = ss(1,2,3,4); sys = append(sys1,10,sys2)

produce the state-space model

a	= x1 x2	x1 0 0	x2 0 1	
b	=	u1	u2	u3
	x1	1	0	0
	x2	0	0	2

С	=			
		x1	x2	
	y1	1	0	
	y2	0	0	
	уЗ	0	3	
d	=			
~	-			
ŭ	-	u1	u2	u3
ŭ	y1	u1 0	u2 0	u3 0
u		-		
ŭ	y1	0	0	0

Continuous-time model.

See Also

connect | feedback | parallel | series

Introduced before R2006a

augstate

Append state vector to output vector

Syntax

```
asys = augstate(sys)
```

Description

asys = augstate(sys) appends the state vector to the outputs of a state-space model.

Given a state-space model sys with equations

$$\dot{x} = Ax + Bu$$
$$y = Cx + Du$$

(or their discrete-time counterpart), augstate appends the states x to the outputs y to form the model

$$\dot{x} = Ax + Bu$$
$$\begin{bmatrix} y \\ x \end{bmatrix} = \begin{bmatrix} C \\ I \end{bmatrix} x + \begin{bmatrix} D \\ 0 \end{bmatrix} u$$

This command prepares the plant so that you can use the feedback command to close the loop on a full-state feedback u = -Kx.

Limitation

Because <code>augstate</code> is only meaningful for state-space models, it cannot be used with TF, ZPK or FRD models.

See Also

feedback | parallel | series

Introduced before R2006a

balreal

Gramian-based input/output balancing of state-space realizations

Syntax

```
[sysb, g] = balreal(sys)
[sysb, g] = balreal(sys, 'AbsTol', ATOL, 'RelTol', RTOL, 'Offset', ALPHA)
[sysb, g] = balreal(sys, condmax)
[sysb, g, T, Ti] = balreal(sys)
[sysb, g] = balreal(sys, opts)
```

Description

[sysb, g] = balreal(sys) computes a balanced realization sysb for the stable portion of the LTI model sys. balreal handles both continuous and discrete systems. If sys is not a state-space model, it is first and automatically converted to state space using ss.

For stable systems, **Sysb** is an equivalent realization for which the controllability and observability Gramians are equal and diagonal, their diagonal entries forming the vector G of Hankel singular values. Small entries in G indicate states that can be removed to simplify the model (use **modred** to reduce the model order).

If **sys** has unstable poles, its stable part is isolated, balanced, and added back to its unstable part to form **sysb**. The entries of **g** corresponding to unstable modes are set to Inf.

[*sysb*, *g*] = balreal(*sys*, 'AbsTol',*ATOL*, 'RelTol',*RTOL*, 'Offset',*ALPHA*) specifies additional options for the stable/unstable decomposition. See the stabsep reference page for more information about these options. The default values are ATOL = 0, RTOL = 1e-8, and ALPHA = 1e-8.

[*sysb*, *g*] = balreal(*sys*, *condmax*) controls the condition number of the stable/ unstable decomposition. Increasing condmax helps separate close by stable and unstable modes at the expense of accuracy. By default condmax=1e8. [sysb, g, T, Ti] = balreal(sys) also returns the vector g containing the diagonal of the balanced gramian, the state similarity transformation $x_b = Tx$ used to convert sys to sysb, and the inverse transformation $Ti = T^{I}$.

If the system is normalized properly, the diagonal g of the joint gramian can be used to reduce the model order. Because g reflects the combined controllability and observability of individual states of the balanced model, you can delete those states with a small g(i) while retaining the most important input-output characteristics of the original system. Use modred to perform the state elimination.

[sysb, g] = balreal(sys, opts) computes the balanced realization using the options specified in the hsvdOptions object opts.

Examples

Balanced Realization of Stable System

Consider the following zero-pole-gain model, with near-canceling pole-zero pairs:

```
sys = zpk([-10 -20.01],[-5 -9.9 -20.1],1)
```

A state-space realization with balanced gramians is obtained by

```
[sysb,g] = balreal(sys);
```

The diagonal entries of the joint gramian are

g '

ans = 0.1006 0.0001 0.0000

This indicates that the last two states of **sysb** are weakly coupled to the input and output. You can then delete these states by

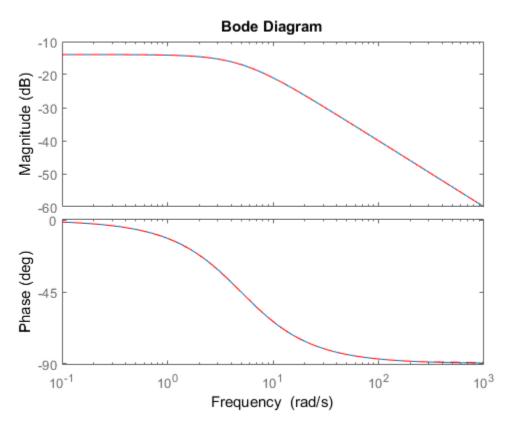
```
sysr = modred(sysb,[2 3],'del');
```

This yields the following first-order approximation of the original system.

```
zpk(sysr)
ans =
    1.0001
    (s+4.97)
Continuous-time zero/pole/gain model.
```

Compare the Bode responses of the original and reduced-order models.

```
bodeplot(sys,sysr,'r--')
```



The plots shows that removing the second and third states does not have much effect on system dynamics.

Balanced Realization of Unstable System

Create this unstable system:

Apply balreal to create a balanced gramian realization.

```
[sysb,g]=balreal(sys1)
a =
            x2
       х1
            0
   х1
        1
   х2
        0
           - 1
b =
            u1
       0.7071
   x1
   x2
       0.7071
c =
                       x2
             x1
                -0.7071
   y1
        0.7071
d =
       u1
   y1
        0
Continuous-time model.
g =
       Inf
    0.2500
```

The unstable pole shows up as Inf in vector g.

More About

Algorithms

Consider the model

$$\dot{x} = Ax + Bu$$
$$y = Cx + Du$$

with controllability and observability gramians W_c and W_o . The state coordinate transformation $\bar{x} = Tx$ produces the equivalent model

$$\dot{\overline{x}} = TAT^{-1}\overline{x} + TBu$$
$$y = CT^{-1}\overline{x} + Du$$

and transforms the gramians to

$$\overline{W}_c = T W_c T^T, \quad \overline{W}_o = T^{-T} W_o T^{-1}$$

The function balreal computes a particular similarity transformation T such that

$$\bar{W}_{c} = \bar{W}_{o} = diag(g)$$

See [1], [2] for details on the algorithm.

References

- [1] Laub, A.J., M.T. Heath, C.C. Paige, and R.C. Ward, "Computation of System Balancing Transformations and Other Applications of Simultaneous Diagonalization Algorithms," *IEEE[®] Trans. Automatic Control*, AC-32 (1987), pp. 115-122.
- [2] Moore, B., "Principal Component Analysis in Linear Systems: Controllability, Observability, and Model Reduction," *IEEE Transactions on Automatic Control*, AC-26 (1981), pp. 17-31.
- [3] Laub, A.J., "Computation of Balancing Transformations," Proc. ACC, San Francisco, Vol.1, paper FA8-E, 1980.

See Also

hsvdOptions | ss | gram | modred

Introduced before R2006a

balred

Model order reduction

Syntax

```
rsys = balred(sys,ORDERS)
rsys = balred(sys,ORDERS,BALDATA)
rsys = balred(____,opts)
```

Description

rsys = balred(sys,ORDERS) computes a reduced-order approximation rsys of the LTI model sys. The desired order (number of states) for rsys is specified by ORDERS. You can try multiple orders at once by setting ORDERS to a vector of integers, in which case rsys is a vector of reduced-order models. balred uses implicit balancing techniques to compute the reduced- order approximation rsys. Use hsvd to plot the Hankel singular values and pick an adequate approximation order. States with relatively small Hankel singular values can be safely discarded.

When **sys** has unstable poles, it is first decomposed into its stable and unstable parts using **stabsep**, and only the stable part is approximated. Use **balredOptions** to specify additional options for the stable/unstable decomposition.

When you have System Identification Toolbox[™] software installed, **sys** can only be an identified state-space model (idss). The reduced-order model is also an idss model.

rsys = balred(sys,ORDERS,BALDATA) uses balancing data returned by hsvd. Because hsvd does most of the work needed to compute rsys, this syntax is more efficient when using hsvd and balred jointly.

rsys = balred(____, opts) computes the model reduction using the specified
options for the stable/unstable decomposition and state elimination method. Use the
balredOptions command to create the option setopts.

Note: The order of the approximate model is always at least the number of unstable poles and at most the minimal order of the original model (number NNZ of nonzero Hankel singular values using an eps-level relative threshold)

More About

• "Why Simplify Models?"

References

 [1] Varga, A., "Balancing-Free Square-Root Algorithm for Computing Singular Perturbation Approximations," Proc. of 30th IEEE CDC, Brighton, UK (1991), pp. 1062-1065.

See Also

balredOptions | hsvd | order | minreal | sminreal

Related Examples

- "Approximate Model with Lower-Order Model"
- "Approximate Model with Unstable or Near-Unstable Pole"

Introduced before R2006a

balredOptions

Create option set for model order reduction

Syntax

```
opts = balredOptions
opts = balredOptions('OptionName', OptionValue)
```

Description

opts = balredOptions returns the default option set for the balred command.

opts = balredOptions('OptionName', OptionValue) accepts one or more comma-separated name/value pairs. Specify OptionName inside single quotes.

Input Arguments

Name-Value Pair Arguments

'StateElimMethod'

State elimination method. Specifies how to eliminate the weakly coupled states (states with smallest Hankel singular values). Specified as one of the following values:

'MatchDC'	Discards the specified states and alters the remaining states to preserve the DC gain.
'Truncate'	Discards the specified states without altering the remaining states. This method tends to product a better approximation in the frequency domain, but the DC gains are not guaranteed to match.

Default: 'MatchDC'

'AbsTol, RelTol'

Absolute and relative error tolerance for stable/unstable decomposition. Positive scalar values. For an input model G with unstable poles, balred first extracts the stable

dynamics by computing the stable/unstable decomposition $G \rightarrow GS + GU$. The AbsTol and RelTol tolerances control the accuracy of this decomposition by ensuring that the frequency responses of G and GS + GU differ by no more than AbsTol + RelTol*abs(G). Increasing these tolerances helps separate nearby stable and unstable modes at the expense of accuracy. See stabsep for more information.

Default: AbsTol = 0; RelTol = 1e-8

'Offset'

Offset for the stable/unstable boundary. Positive scalar value. In the stable/unstable decomposition, the stable term includes only poles satisfying

```
Re(s) < -Offset * max(1, |Im(s)|) (Continuous time)</li>
|z| < 1 - Offset (Discrete time)</li>
```

Increase the value of Offset to treat poles close to the stability boundary as unstable.

Default: 1e-8

For additional information on the options and how to use them, see the **balred** reference page.

Examples

Reduced-Order Approximation with Offset Option

Compute a reduced-order approximation of the system given by:

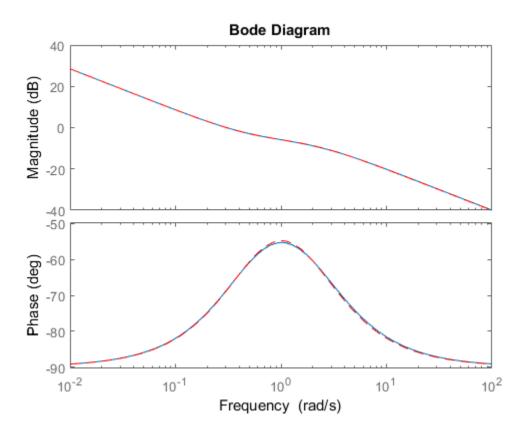
$$G\left(s\right) = \frac{\left(s + 0.5\right)\left(s + 1.1\right)\left(s + 2.9\right)}{\left(s + 10^{-6}\right)\left(s + 1\right)\left(s + 2\right)\left(s + 3\right)}.$$

Use the Offset option to exclude the pole at $s = 10^{-6}$ from the stable term of the stable/ unstable decomposition.

```
sys = zpk([-.5 -1.1 -2.9],[-1e-6 -2 -1 -3],1);
% Create balredOptions
opt = balredOptions('Offset',.001,'StateElimMethod','Truncate');
% Compute second-order approximation
rsys = balred(sys,2,opt);
```

Compare the responses of the original and reduced-order models.

```
bodeplot(sys,rsys,'r--')
```



See Also balred | stabsep

Introduced in R2010a

bandwidth

Frequency response bandwidth

Syntax

```
fb = bandwidth(sys)
fb = bandwidth(sys,dbdrop)
```

Description

fb = bandwidth(sys) computes the bandwidth fb of the SISO dynamic system model sys, defined as the first frequency where the gain drops below 70.79 percent (-3 dB) of its DC value. The frequency fb is expressed in rad/TimeUnit, where TimeUnit is the time units of the input dynamic system, specified in the TimeUnit property of sys.

For FRD models, bandwidth uses the first frequency point to approximate the DC gain.

fb = bandwidth(sys,dbdrop) specifies the critical gain drop in dB. The default value is -3 dB, or a 70.79 percent drop.

If ${\tt sys}$ is an S1-by...-by-Sp array of models, ${\tt bandwidth}$ returns an array of the same size such that

 $fb(j1,\ldots,jp) = bandwidth(sys(:,:,j1,\ldots,jp))$

See Also issiso | dcgain

Introduced before R2006a

bdschur

Block-diagonal Schur factorization

Syntax

[T,B,BLKS] = bdschur(A,CONDMAX)
[T,B] = bdschur(A,[],BLKS)

Description

[T,B,BLKS] = bdschur(A,CONDMAX) computes a transformation matrix T such that $B = T \setminus A * T$ is block diagonal and each diagonal block is a quasi upper-triangular Schur matrix.

[T,B] = bdschur(A,[],BLKS) pre-specifies the desired block sizes. The input matrix A should already be in Schur form when you use this syntax.

Input Arguments

- A: Matrix for block-diagonal Schur factorization.
- CONDMAX: Specifies an upper bound on the condition number of T. By default, CONDMAX = 1/sqrt(eps). Use CONDMAX to control the tradeoff between block size and conditioning of T with respect to inversion. When CONDMAX is a larger value, the blocks are smaller and T becomes more ill-conditioned.

Output Arguments

- T: Transformation matrix.
- B: Matrix $B = T \setminus A * T$.
- BLKS: Vector of block sizes.

See Also

ordschur | schur

Introduced in R2008a

blkdiag

Block-diagonal concatenation of models

Syntax

```
sys = blkdiag(sys1,sys2,...,sysN)
```

Description

sys = blkdiag(sys1,sys2,...,sysN) produces the aggregate system

 $\begin{bmatrix} sys1 & 0 & .. & 0 \\ 0 & sys2 & . & . \\ . & . & . & 0 \\ 0 & .. & 0 & sysN \end{bmatrix}$

blkdiag is equivalent to append.

Examples

The commands

sys1 = tf(1,[1 0]); sys2 = ss(1,2,3,4); sys = blkdiag(sys1,10,sys2)

produce the state-space model

	x1 x2	1 0	0 0	0 2
с	=			
		x1	x2	
	y1	1	0	
	y2	0	0	
	уЗ	0	3	
d	=			
		u1	u2	u3
	у1	0	0	0
	y2	0	10	0
	уЗ	0	0	4

Continuous-time model.

See Also

append | series | parallel | feedback

Introduced in R2009a

bode

Bode plot of frequency response, magnitude and phase of frequency response

Syntax

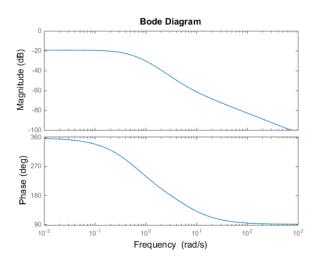
```
bode(sys)
bode(sys1,...,sysN)
bode(sys1,PlotStyle1,...,sysN,PlotStyleN)
bode(...,w)
[mag,phase] = bode(sys,w)
[mag,phase,wout] = bode(sys)
[mag,phase,wout,sdmag,sdphase] = bode(sys)
```

Description

bode(sys) creates a Bode plot of the frequency response of a dynamic system model **sys**. The plot displays the magnitude (in dB) and phase (in degrees) of the system response as a function of frequency.

When **sys** is a multi-input, multi-output (MIMO) model, **bode** produces an array of Bode plots, each plot showing the frequency response of one I/O pair.

bode automatically determines the plot frequency range based on system dynamics.



bode(sys1,...,sysN) plots the frequency response of multiple dynamic systems in a single figure. All systems must have the same number of inputs and outputs.

bode(sys1,PlotStyle1,...,sysN,PlotStyleN) plots system responses using the color, linestyle, and markers specified by the PlotStyle strings.

bode(...,w) plots system responses at frequencies determined by w.

- If w is a cell array {wmin,wmax}, bode(sys,w) plots the system response at frequency values in the range {wmin,wmax}.
- If w is a vector of frequencies, bode(sys,w) plots the system response at each of the frequencies specified in W.

[mag,phase] = bode(sys,w) returns magnitudes mag in absolute units and phase values phase in degrees. The response values in mag and phase correspond to the frequencies specified by w as follows:

- If w is a cell array {wmin,wmax}, [mag,phase] = bode(sys,w) returns the system response at frequency values in the range {wmin,wmax}.
- If w is a vector of frequencies, [mag,phase] = bode(sys,w) returns the system response at each of the frequencies specified in w.

[mag,phase,wout] = bode(sys) returns magnitudes, phase values, and frequency values wout corresponding to bode(sys). [mag,phase,wout,sdmag,sdphase] = bode(sys) additionally returns the estimated standard deviation of the magnitude and phase values when sys is an identified model and [] otherwise.

Input Arguments

sys

Dynamic system model, such as a Numeric LTI model, or an array of such models.

PlotStyle

Line style, marker, and color of both the line and marker, specified as a one-, two-, or three-part string enclosed in single quotes (' '). The elements of the string can appear in any order. The string can specify only the line style, the marker, or the color.

For more information about configuring the PlotStyle string, see "Specify Line Style, Color, and Markers" in the MATLAB documentation.

w

Input frequency values, specified as a row vector or a two-element cell array.

Possible values of W:

- Two-element cell array {wmin,wmax}, where wmin is the minimum frequency value and wmax is the maximum frequency value.
- Row vector of frequency values.

For example, use **logspace** to generate a row vector with logarithmically-spaced frequency values.

Specify frequency values in radians per TimeUnit, where TimeUnit is the time units of the input dynamic system, specified in the TimeUnit property of sys.

Output Arguments

mag

Bode magnitude of the system response in absolute units, returned as a 3-D array with dimensions (number of outputs) \times (number of inputs) \times (number of frequency points).

- For a single-input, single-output (SISO) sys, mag(1,1,k) gives the magnitude of the response at the kth frequency.
- For MIMO systems, mag(i,j,k) gives the magnitude of the response from the jth input to the ith output.

You can convert the magnitude from absolute units to decibels using:

magdb = 20*log10(mag)

phase

Phase of the system response in degrees, returned as a 3-D array with dimensions are (number of outputs) \times (number of inputs) \times (number of frequency points).

- For SISO sys, phase(1,1,k) gives the phase of the response at the kth frequency.
- For MIMO systems, phase(i, j, k) gives the phase of the response from the jth input to the ith output.

wout

Response frequencies, returned as a row vector of frequency points. Frequency values are in radians per TimeUnit, where TimeUnit is the value of the TimeUnit property of sys.

sdmag

Estimated standard deviation of the magnitude. sdmag has the same dimensions as mag.

If sys is not an identified LTI model, sdmag is [].

sdphase

Estimated standard deviation of the phase. sdphase has the same dimensions as phase.

If sys is not an identified LTI model, sdphase is [].

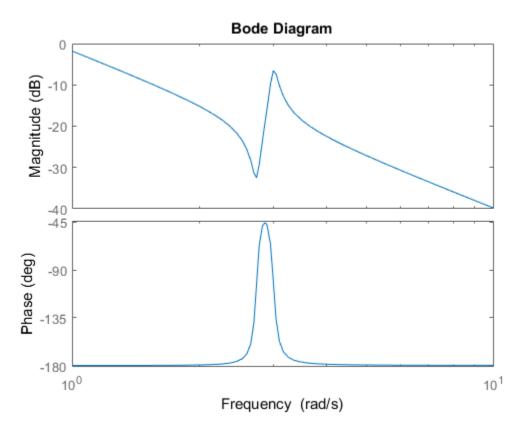
Examples

Bode Plot of Dynamic System

Create a Bode plot of the following continuous-time SISO dynamic system.

$$H(s) = \frac{s^2 + 0.1s + 7.5}{s^4 + 0.12s^3 + 9s^2}.$$

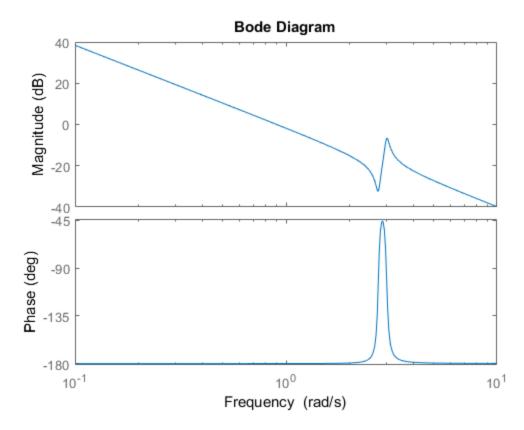
H = tf([1 0.1 7.5],[1 0.12 9 0 0]); bode(H)



bode automatically selects the plot range based on the system dynamics.

Bode Plot at Specified Frequencies

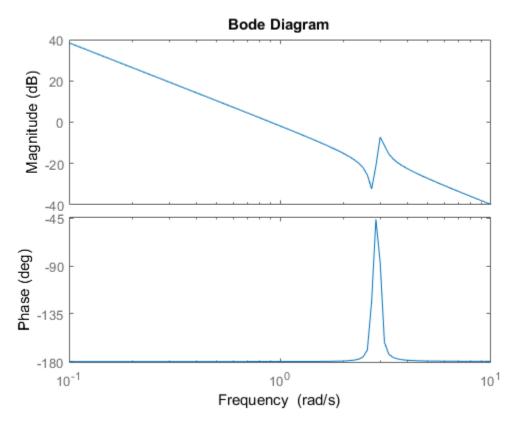
Create a Bode plot over a specified frequency range. Use this approach when you want to focus on the dynamics in a particular range of frequencies.



The cell array $\{0.1, 10\}$ specifies the minimum and maximum frequency values in the Bode plot. When you provide frequency bounds in this way, the software selects intermediate points for frequency response data.

Alternatively, specify a vector of frequency points to use for evaluating and plotting the frequency response.

w = logspace(-1,1,100); bode(H,w)



logspace defines a logarithmically spaced frequency vector in the range of 0.1-10 rad/s.

Compare Bode Plots of Several Dynamic Systems

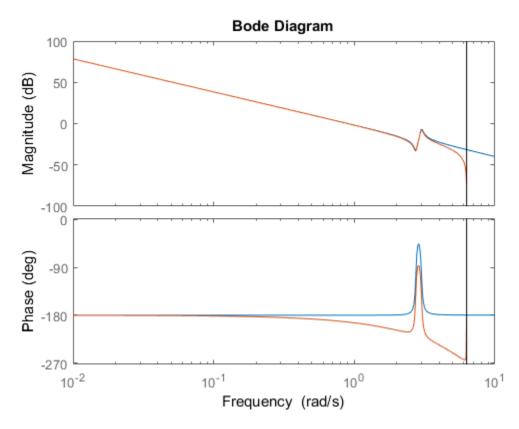
Compare the frequency response of a continuous-time system to an equivalent discretized system on the same Bode plot.

Create continuous-time and discrete-time dynamic systems.

H = tf([1 0.1 7.5],[1 0.12 9 0 0]); Hd = c2d(H,0.5, 'zoh');

Create a Bode plot that displays both systems.



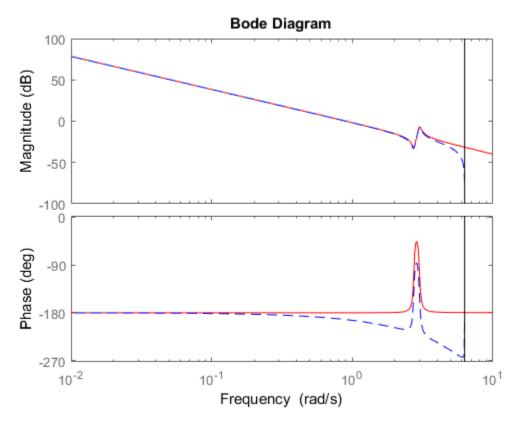


The Bode plot of a discrete-time system includes a vertical line marking the Nyquist frequency of the system.

Bode Plot with Specified Line and Marker Attributes

Specify the color, linestyle, or marker for each system in a Bode plot using the PlotStyle input arguments.

```
H = tf([1 0.1 7.5],[1 0.12 9 0 0]);
Hd = c2d(H,0.5,'zoh');
bode(H,'r',Hd,'b--')
```



The string 'r' specifies a solid red line for the response of H. The string 'b--' specifies a dashed blue line for the response of Hd.

Obtain Magnitude and Phase Data

Compute the magnitude and phase of the frequency response of a dynamic system.

H = tf([1 0.1 7.5],[1 0.12 9 0 0]); [mag phase wout] = bode(H);

Because H is a SISO model, the first two dimensions of mag and phase are both 1. The third dimension is the number of frequencies in wout.

Bode Plot of Identified Model

Compare the frequency response of a parametric model, identified from input/output data, to a nonparametric model identified using the same data.

Identify parametric and non-parametric models based on data.

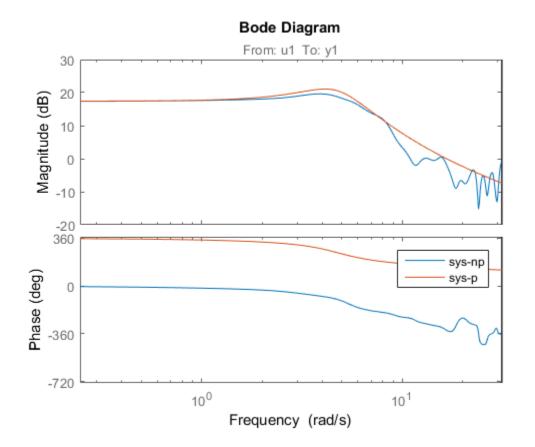
load iddata2 z2; w = linspace(0,10*pi,128); sys_np = spa(z2,[],w); sys_p = tfest(z2,2);

Using the spa and tfest commands requires System Identification Toolbox[™] software.

sys_np is a non-parametric identified model. sys_p is a parametric identified model.

Create a Bode plot that includes both systems.

bode(sys_np,sys_p,w); legend('sys-np','sys-p')



Obtain Magnitude and Phase Standard Deviation Data of Identified Model

Compute the standard deviation of the magnitude and phase of an identified model. Use this data to create a 30 plot of the response uncertainty.

Identify a transfer function model based on data. Obtain the standard deviation data for the magnitude and phase of the frequency response.

```
load iddata2 z2;
sys_p = tfest(z2,2);
w = linspace(0,10*pi,128);
```

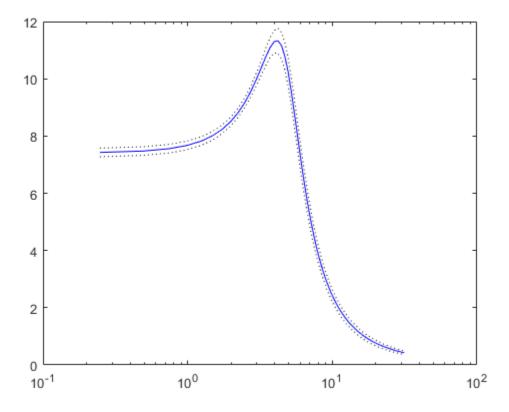
```
[mag,ph,w,sdmag,sdphase] = bode(sys_p,w);
```

Using the tfest command requires System Identification Toolbox[™] software.

sys_p is an identified transfer function model. sdmag and sdphase contain the standard deviation data for the magnitude and phase of the frequency response, respectively.

Use the standard deviation data to create a 3σ plot corresponding to the confidence region.

```
mag = squeeze(mag);
sdmag = squeeze(sdmag);
semilogx(w,mag, 'b',w,mag+3*sdmag, 'k:',w,mag-3*sdmag, 'k:');
```



Alternatives

Use bodeplot when you need additional plot customization options.

More About

Algorithms

bode computes the frequency response using these steps:

1 Computes the zero-pole-gain (zpk) representation of the dynamic system.

- **2** Evaluates the gain and phase of the frequency response based on the zero, pole, and gain data for each input/output channel of the system.
 - **a** For continuous-time systems, **bode** evaluates the frequency response on the imaginary axis $s = j\omega$ and considers only positive frequencies.
 - **b** For discrete-time systems, **bode** evaluates the frequency response on the unit circle. To facilitate interpretation, the command parameterizes the upper half of the unit circle as

$$z = e^{j\omega T_s}, \quad 0 \le \omega \le \omega_N = \frac{\pi}{T_s},$$

where T_s is the sample time. ω_N is the *Nyquist frequency*. The equivalent continuous-time frequency ω is then used as the *x*-axis variable. Because

 $H(e^{j\omega T_s})$ is periodic and has a period 2 ω_N , bode plots the response only up to the Nyquist frequency ω_N . If you do not specify a sample time, bode uses $T_s = 1$.

• "Dynamic System Models"

See Also

freqresp | nyquist | bodeplot | nichols

Introduced before R2006a

bodemag

Bode magnitude response of LTI models

Syntax

```
bodemag(sys)
bodemag(sys,{wmin,wmax})
bodemag(sys,w)
bodemag(sys1,sys2,...,sysN,w)
```

Description

bodemag(sys) plots the magnitude of the frequency response of the dynamic system model **sys** (Bode plot without the phase diagram). The frequency range and number of points are chosen automatically.

bodemag(sys, {wmin,wmax}) draws the magnitude plot for frequencies between wmin and wmax (in rad/TimeUnit, where TimeUnit is the time units of the input dynamic system, specified in the TimeUnit property of sys).

bodemag(sys,w) uses the user-supplied vector W of frequencies, in rad/TimeUnit, at
which the frequency response is to be evaluated.

bodemag(sys1,sys2,...,sysN,w) shows the frequency response magnitude of several models sys1,sys2,...,sysN on a single plot. The frequency vector w is optional. You can also specify a color, line style, and marker for each model. For example:

```
bodemag(sys1,'r',sys2,'y--',sys3,'gx')
```

See Also

bode | linearSystemAnalyzer

Introduced before R2006a

bodeoptions

Create list of Bode plot options

Syntax

```
P = bodeoptions
P = bodeoptions('cstprefs')
```

Description

P = bodeoptions returns a default set of plot options for use with the bodeplot. You can use these options to customize the Bode plot appearance using the command line. This syntax is useful when you want to write a script to generate plots that look the same regardless of the preference settings of the MATLAB session in which you run the script.

P = bodeoptions('cstprefs') initializes the plot options with the options you selected in the Control System and System Identification Toolbox Preferences Editor. For more information about the editor, see "Toolbox Preferences Editor" in the User's Guide documentation. This syntax is useful when you want to change a few plot options but otherwise use your default preferences. A script that uses this syntax may generate results that look different when run in a session with different preferences.

Option	Description
Title, XLabel, YLabel	Label text and style, specified as a structure with the following fields:
	 String — Label text, specified as a string
	• FontSize — Default : 8
	 FontWeight — Default: 'Normal'
	• Font Angle — Default : 'Normal'
	 Color — Vector of RGB values ranging from 0 to 1. Default: [0,0,0]
	• Interpreter — Default: 'tex'
TickLabel	Tick label style, specified as a structure with the following fields:

The following table summarizes the Bode plot options.

Option	Description
	FontSize Default: 8
	 FontWeight — Default: 'Normal'
	• Font Angle — Default : 'Normal'
	 Color — Vector of RGB values ranging from 0 to 1. Default: [0,0,0]
Grid	Show or hide the grid Specified as one of the following strings: 'off' 'on' Default: 'off'
GridColor	Color of the grid lines Specified as one of the following: Vector of RGB values in the range [0,1] color string 'none'. Default: [0.15,0.15,0.15]
XlimMode, YlimMode	Axis limit modes. Default : 'auto'
Xlim, Ylim	Axes limits, specified as an array of the form [min,max]
IOGrouping	Grouping of input-output pairs Specified as one of the following strings: 'none' 'inputs' 'outputs' 'all' Default: 'none'
InputLabels, OutputLabels	Input and output label styles
InputVisible, OutputVisible	Visibility of input and output channels
ConfidenceRegionNumbe	Number of standard deviations to use to plotting the response confidence region (identified models only).
	Default: 1.

Option	Description
FreqUnits	Frequency units, specified as one of the following strings:
	• 'Hz'
	 'rad/second'
	• 'rpm'
	• 'kHz'
	• 'MHz'
	• 'GHz'
	 'rad/nanosecond'
	 'rad/microsecond'
	• 'rad/millisecond'
	• 'rad/minute'
	• 'rad/hour'
	• 'rad/day'
	 'rad/week'
	• 'rad/month'
	• 'rad/year'
	• 'cycles/nanosecond'
	 'cycles/microsecond'
	• 'cycles/millisecond'
	• 'cycles/hour'
	• 'cycles/day'
	• 'cycles/week'
	• 'cycles/month'
	• 'cycles/year'
	Default: 'rad/s'
	You can also specify 'auto' which uses frequency units rad/TimeUnit relative to system time units specified in the TimeUnit property. For

Option	Description
	multiple systems with different time units, the units of the first system are used.
FreqScale	Frequency scale Specified as one of the following strings: 'linear' 'log' Default: 'log'
MagUnits	Magnitude units Specified as one of the following strings: 'dB' 'abs' Default: 'dB'
MagScale	Magnitude scale Specified as one of the following strings: 'linear' 'log' Default: 'linear'
MagVisible	Magnitude plot visibility Specified as one of the following strings: 'on' 'off' Default : 'on'
MagLowerLimMode	Enables a lower magnitude limit Specified as one of the following strings: 'auto' 'manual' Default: 'auto'
MagLowerLim	Specifies the lower magnitude limit
PhaseUnits	Phase units Specified as one of the following strings: 'deg' 'rad' Default: 'deg'
PhaseVisible	Phase plot visibility Specified as one of the following strings: 'on' 'off' Default: 'on'
PhaseWrapping	Enables phase wrapping Specified as one of the following strings: 'on' 'off' Default: 'off'
PhaseMatching	Enables phase matching Specified as one of the following strings: 'on' 'off' Default: 'off'
PhaseMatchingFreq	Frequency for matching phase
PhaseMatchingValue	The value to which phase responses are matched closely

Examples

Create Bode Plot with Custom Settings

Create a Bode plot that suppresses the phase plot and uses frequency units Hz instead of the default radians/second. Otherwise, the plot uses the settings that are saved in the toolbox preferences.

First, create an options set based on the toolbox preferences.

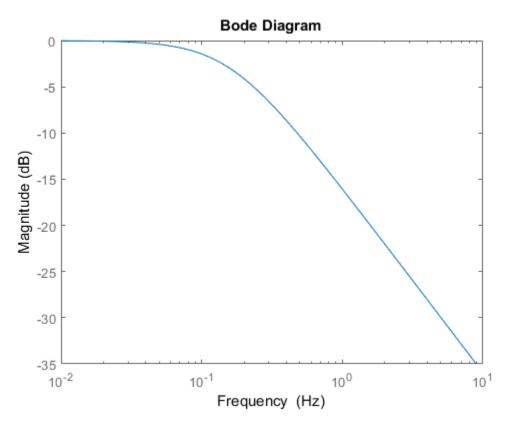
```
opts = bodeoptions('cstprefs');
```

Change properties of the options set.

opts.PhaseVisible = 'off'; opts.FreqUnits = 'Hz';

Create a plot using the options.

h = bodeplot(tf(1,[1,1]),opts);



Depending on your own toolbox preferences, the plot you obtain might look different from this plot. Only the properties that you set explicitly, in this example PhaseVisible and FreqUnits, override the toolbox preferences.

Custom Plot Settings Independent of Preferences

Create a Bode plot that uses 14-point red text for the title. This plot should look the same, regardless of the preferences of the MATLAB session in which it is generated.

First, create a default options set.

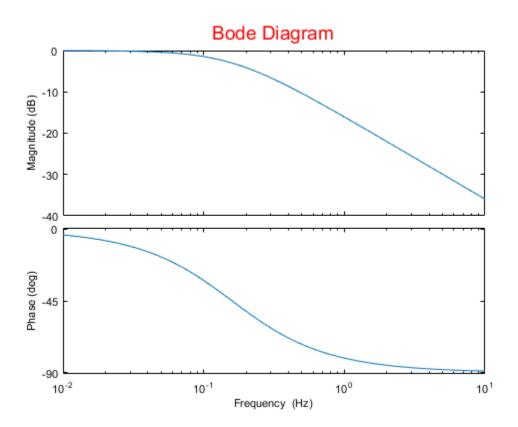
opts = bodeoptions;

Change properties of the options set.

opts.Title.FontSize = 14; opts.Title.Color = [1 0 0]; opts.FreqUnits = 'Hz';

Create a plot using the options.

h = bodeplot(tf(1,[1,1]),opts);



Because opts begins with a fixed set of options, the plot result is independent of the toolbox preferences of the MATLAB session.

See Also

bodeplot | getoptions | setoptions | bode

Introduced in R2008a

bodeplot

Plot Bode frequency response with additional plot customization options

Syntax

```
h = bodeplot(sys)
bodeplot(sys)
bodeplot(sys1,sys2,...)
bodeplot(AX,...)
bodeplot(..., plotoptions)
bodeplot(sys,w)
```

Description

h = bodeplot(sys) plot the Bode magnitude and phase of the dynamic system model sys and returns the plot handle h to the plot. You can use this handle to customize the plot with the getoptions and setoptions commands.

bodeplot(sys) draws the Bode plot of the model **sys**. The frequency range and number of points are chosen automatically.

bodeplot(sys1,sys2,...) graphs the Bode response of multiple models sys1,sys2,...
on a single plot. You can specify a color, line style, and marker for each model, as in

bodeplot(sys1,'r',sys2,'y--',sys3,'gx')

bodeplot(AX,...) plots into the axes with handle AX.

bodeplot(..., plotoptions) plots the Bode response with the options specified in
plotoptions. Type

help bodeoptions

for a list of available plot options. See "Match Phase at Specified Frequency." on page 1-70 for an example of phase matching using the PhaseMatchingFreq and PhaseMatchingValue options.

bodeplot(sys,w) draws the Bode plot for frequencies specified by w. When w =
{wmin,wmax}, the Bode plot is drawn for frequencies between wmin and wmax (in rad/
TimeUnit, where TimeUnit is the time units of the input dynamic system, specified in
the TimeUnit property of sys.). When w is a user-supplied vector w of frequencies, in
rad/TimeUnit, the Bode response is drawn for the specified frequencies.

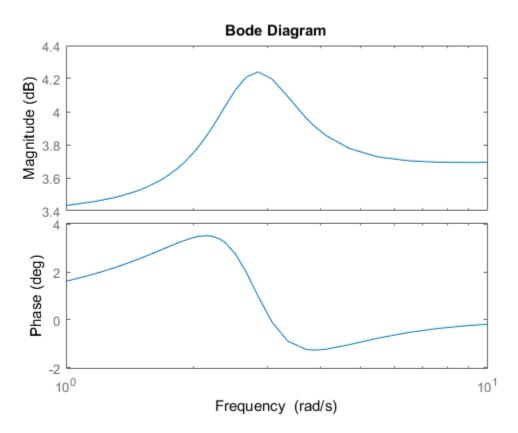
See logspace to generate logarithmically spaced frequency vectors.

Examples

Change Bode Plot Options with Plot Handle

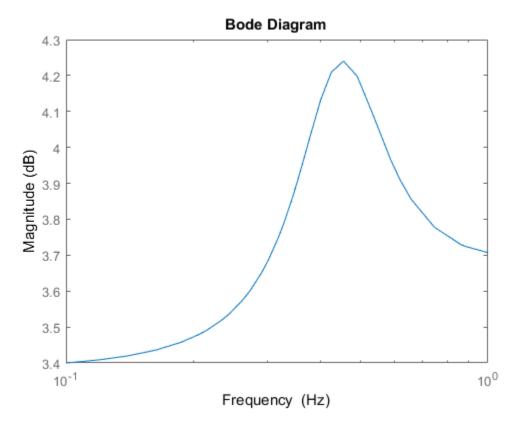
Generate a Bode plot.

sys = rss(5); h = bodeplot(sys);



Change the units to Hz and suppress the phase plot. To do so, edit properties of the plot handle, $\mathsf{h}.$

setoptions(h, 'FreqUnits', 'Hz', 'PhaseVisible', 'off');

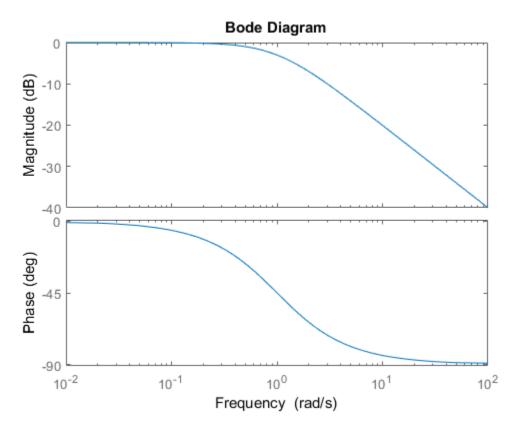


The plot automatically updates when you call setoptions.

Match Phase at Specified Frequency.

Create a Bode plot of a dynamic system.

sys = tf(1,[1 1]); h = bodeplot(sys);

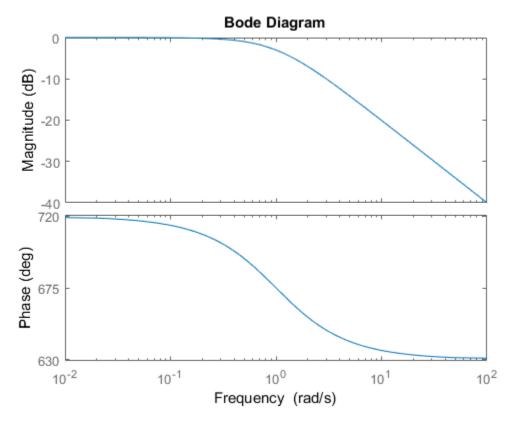


Fix the phase at 1 rad/s to 750 degrees. To do so, get the plot properties. Then alter the properties PhaseMatchingFreq and PhaseMatchingValue to match a phase to a specified frequency.

```
p = getoptions(h);
p.PhaseMatching = 'on';
p.PhaseMatchingFreq = 1;
p.PhaseMatchingValue = 750;
```

Update the plot.

setoptions(h,p);



The first bode plot has a phase of -45 degrees at a frequency of 1 rad/s. Setting the phase matching options so that at 1 rad/s the phase is near 750 degrees yields the second Bode plot. Note that, however, the phase can only be -45 + N*360, where N is an integer, and so the plot is set to the nearest allowable phase, namely 675 degrees (or 2*360 - 45 = 675).

Display Confidence Regions of Identified Models

Compare the frequency responses of identified state-space models of order 2 and 6 along with their 2 σ confidence regions.

```
load iddata1
sys1 = n4sid(z1, 2) % discrete-time IDSS model of order 2
```

```
sys2 = n4sid(z1, 6) % discrete-time IDSS model of order 6
```

Both models produce about 76% fit to data. However, sys2 shows higher uncertainty in its frequency response, especially close to Nyquist frequency as shown by the plot:

```
w = linspace(8,10*pi,256);
h = bodeplot(sys1,sys2,w);
setoptions(h, 'PhaseMatching', 'on', 'ConfidenceRegionNumberSD', 2);
```

Use the context menu by right-clicking **Characteristics** > **Confidence Region** to turn on the confidence region characteristic.

Frequency Response of Identified Parametric and Nonparametric models

Compare the frequency response of a parametric model, identified from input/output data, to a nonparametric model identified using the same data.

1 Identify parametric and non-parametric models based on data.

```
load iddata2 z2;
w = linspace(0,10*pi,128);
sys_np = spa(z2,[],w);
sys_p = tfest(z2,2);
```

spa and tfest require System Identification Toolbox software. sys_np is a
nonparametric identified model. sys_p is a parametric identified model.

2 Create a Bode plot that includes both systems.

```
opt = bodeoptions; opt.PhaseMatching = 'on';
bodeplot(sys_np,sys_p,w, opt);
```

More About

Tips

You can change the properties of your plot, for example the units. For information on the ways to change properties of your plots, see "Ways to Customize Plots".

See Also

bodeoptions | getoptions | setoptions | bode

Introduced before R2006a

c2d

Convert model from continuous to discrete time

Syntax

```
sysd = c2d(sys,Ts)
sysd = c2d(sys,Ts,method)
sysd = c2d(sys,Ts,opts)
[sysd,G] = c2d(sys,Ts,method)
[sysd,G] = c2d(sys,Ts,opts)
```

Description

sysd = c2d(sys,Ts) discretizes the continuous-time dynamic system model sys using zero-order hold on the inputs and a sample time of Ts seconds.

sysd = c2d(sys,Ts,method) discretizes sys using the specified discretization
method method.

sysd = c2d(sys,Ts,opts) discretizes sys using the option set opts, specified using the c2dOptions command.

[sysd,G] = c2d(sys,Ts,method) returns a matrix, G that maps the continuous initial conditions x_0 and u_0 of the state-space model sys to the discrete-time initial state vector x [0]. method is optional. To specify additional discretization options, use [sysd, G] = c2d(sys,Ts,opts).

Input Arguments

sys

Continuous-time dynamic system model (except frequency response data models). **sys** can represent a SISO or MIMO system, except that the 'matched' discretization method supports SISO systems only.

sys can have input/output or internal time delays; however, the 'matched' and 'impulse' methods do not support state-space models with internal time delays.

The following identified linear systems cannot be discretized directly:

- idgrey models with FcnType is 'c'. Convert to idss model first.
- idproc models. Convert to idtf or idpoly model first.

For the syntax [sysd,G] = c2d(sys,Ts,opts), sys must be a state-space model.

Ts

Sample time.

method

String specifying a discretization method:

- 'zoh' Zero-order hold (default). Assumes the control inputs are piecewise constant over the sample time Ts.
- 'foh' Triangle approximation (modified first-order hold). Assumes the control inputs are piecewise linear over the sample time Ts.
- 'impulse' Impulse invariant discretization.
- 'tustin' Bilinear (Tustin) method.
- 'matched' Zero-pole matching method.

For more information about discretization methods, see "Continuous-Discrete Conversion Methods".

opts

Discretization options. Create opts using c2dOptions.

Output Arguments

sysd

Discrete-time model of the same type as the input system sys.

When sys is an identified (IDLTI) model, sysd:

- Includes both measured and noise components of sys. The innovations variance λ of the continuous-time identified model sys, stored in its NoiseVarianceproperty, is interpreted as the intensity of the spectral density of the noise spectrum. The noise variance in sysd is thus λ/Ts .
- Does not include the estimated parameter covariance of **sys**. If you want to translate the covariance while discretizing the model, use **translatecov**.

G

Matrix relating continuous-time initial conditions x_0 and u_0 of the state-space model **sys** to the discrete-time initial state vector x [0], as follows:

$$x[0] = G \cdot \begin{bmatrix} x_0 \\ u_0 \end{bmatrix}$$

For state-space models with time delays, c2d pads the matrix G with zeroes to account for additional states introduced by discretizing those delays. See "Continuous-Discrete Conversion Methods" for a discussion of modeling time delays in discretized systems.

Examples

Discretize a Transfer Function

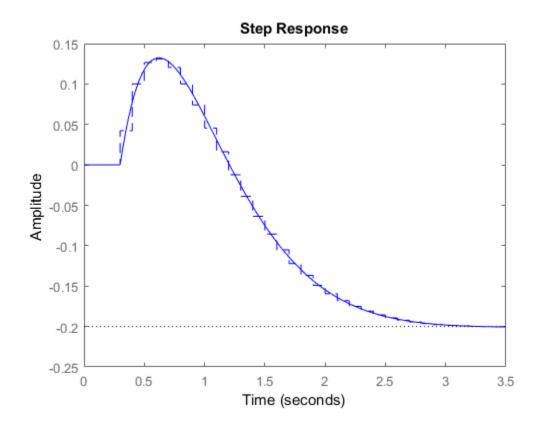
Discretize the following continuous-time transfer function:

$$H(s) = e^{-0.3s} \frac{s-1}{s^2+4s+5}.$$

This system has an input delay of 0.3 s. Discretize the system using the triangle (first-order-hold) approximation with sample time Ts = 0.1 s.

```
H = tf([1 -1],[1 4 5],'InputDelay', 0.3);
Hd = c2d(H,0.1,'foh');
```

Compare the step responses of the continuous-time and discretized systems. step(H, '-', Hd, '--')



Discretize Model with Fractional Delay Asborbed into Coefficients

Discretize the following delayed transfer function using zero-order hold on the input, and a 10-Hz sampling rate.

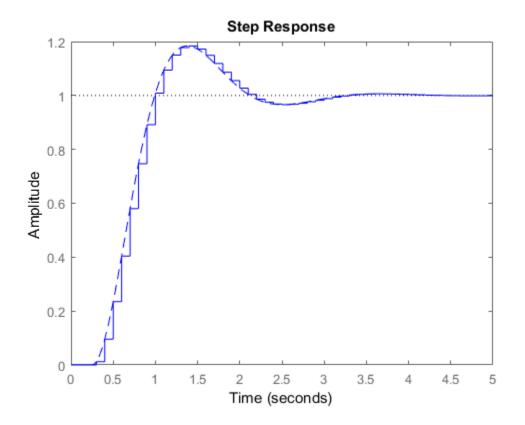
$$H(s) = e^{-0.25s} \frac{10}{s^2 + 3s + 10}$$

```
h = tf(10,[1 3 10],'iodelay',0.25);
hd = c2d(h, 0.1)
hd =
2^{(-3)} * \cdots 2^{2} + 0.06408 \ z + 0.009721 \ z^{2} - 1.655 \ z + 0.7408
Sample time: 0.1 seconds
Discrete-time transfer function.
```

In this example, the discretized model hd has a delay of three sampling periods. The discretization algorithm absorbs the residual half-period delay into the coefficients of hd.

Compare the step responses of the continuous-time and discretized models.

```
step(h,'--',hd,'-')
```



Discretize Model With Approximated Fractional Delay

Discretize a state-space model with time delay, using a Thiran filter to model fractional delays:

sys = ss(tf([1, 2], [1, 4, 2])); % create a state-space model sys.InputDelay = 2.7 % add input delay This command creates a continuous-time state-space model with two states, as the output shows:

a = x1 x2 x1 -4 -2

```
х2
       1
          0
b =
       u1
        2
   x1
   х2
        0
с =
        х1
             х2
   y1
       0.5
              1
d =
       u1
   y1
        0
Input delays (listed by channel): 2.7
Continuous-time model.
```

Use c2dOptions to create a set of discretization options, and discretize the model. This example uses the Tustin discretization method.

```
opt = c2dOptions('Method', 'tustin', 'FractDelayApproxOrder', 3);
sysd1 = c2d(sys, 1, opt) % 1s sample time
These commands yield the result
a =
               x1
                          x2
                                      хЗ
                                                  х4
                                                              х5
   х1
         -0.4286
                     -0.5714
                                -0.00265
                                            0.06954
                                                          2.286
          0.2857
                      0.7143
   х2
                              -0.001325
                                             0.03477
                                                          1.143
   хЗ
                0
                            0
                                 -0.2432
                                              0.1449
                                                         -0.1153
                0
                            0
                                    0.25
   х4
                                                               0
                                                   0
   х5
                0
                            0
                                       0
                                               0.125
                                                               0
b =
              u1
       0.002058
   х1
   х2
       0.001029
   хЗ
               8
               0
   х4
   х5
               0
с =
                                                              х5
               х1
                          х2
                                      хЗ
                                                  х4
          0.2857
                      0.7143 -0.001325
                                                          1.143
                                            0.03477
   y1
```

```
d =
u1
y1 0.001029
Sample time: 1
Discrete-time model.
```

The discretized model now contains three additional states x3, x4, and x5 corresponding to a third-order Thiran filter. Since the time delay divided by the sample time is 2.7, the third-order Thiran filter (FractDelayApproxOrder = 3) can approximate the entire time delay.

Discretized Identified Model

Discretize an identified, continuous-time transfer function and compare its performance against a directly estimated discrete-time model

Estimate a continuous-time transfer function and discretize it.

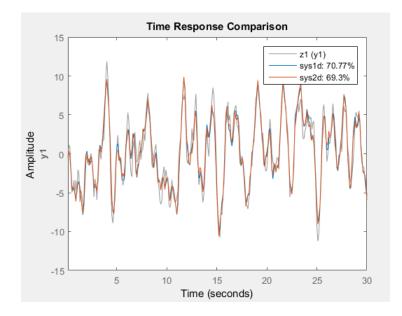
```
load iddata1
sys1c = tfest(z1,2);
sys1d = c2d(sys1c,0.1,'zoh');
```

Estimate a second order discrete-time transfer function.

```
sys2d = tfest(z1,2,'Ts',0.1);
```

Compare the two models.

compare(z1,sys1d,sys2d)



The two systems are virtually identical.

Build Predictor Model

Discretize an identified state-space model to build a one-step ahead predictor of its response.

```
load iddata2
sysc = ssest(z2,4);
sysd = c2d(sysc,0.1,'zoh');
[A,B,C,D,K] = idssdata(sysd);
Predictor = ss(A-K*C,[K B-K*D],C,[0 D],0.1);
```

The Predictor is a two input model which uses the measured output and input signals ([z1.y z1.u]) to compute the 1-step predicted response of sysc.

More About

Tips

- Use the syntax sysd = c2d(sys,Ts,method) to discretize sys using the default options for method. To specify additional discretization options, use the syntax sysd = c2d(sys,Ts,opts).
- To specify the tustin method with frequency prewarping (formerly known as the 'prewarp' method), use the PrewarpFrequency option of c2dOptions.

Algorithms

For information about the algorithms for each c2d conversion method, see "Continuous-Discrete Conversion Methods".

- "Dynamic System Models"
- "Discretize a Compensator"
- "Continuous-Discrete Conversion Methods"

See Also

d2c | d2d | c2dOptions | thiran | translatecov

Introduced before R2006a

c2dOptions

Create option set for continuous- to discrete-time conversions

Syntax

```
opts = c2dOptions
opts = c2dOptions('OptionName', OptionValue)
```

Description

opts = c2dOptions returns the default options for c2d.

opts = c2dOptions('OptionName', OptionValue) accepts one or more commaseparated name/value pairs that specify options for the c2d command. Specify OptionName inside single quotes.

Input Arguments

Name-Value Pair Arguments

'Method'

Discretization method, specified as one of the following values:

'zoh'	Zero-order hold, where $c2d$ assumes the control inputs are piecewise constant over the sample time Ts .
'foh'	Triangle approximation (modified first-order hold), where c2d assumes the control inputs are piecewise linear over the sample time Ts. (See [1], p. 228.)
'impulse'	Impulse-invariant discretization.
'tustin'	Bilinear (Tustin) approximation. By default, c2d discretizes with no prewarp and rounds any fractional time delays to the nearest multiple of the sample time. To include prewarp, use the PrewarpFrequency option. To approximate fractional time delays, use theFractDelayApproxOrder option.

'matched' Zero-pole matching method. (See [1], p. 224.) By default, c2d rounds any fractional time delays to the nearest multiple of the sample time. To approximate fractional time delays, use the FractDelayApproxOrder option.

Default: 'zoh'

'PrewarpFrequency'

Prewarp frequency for 'tustin' method, specified in rad/TimeUnit, where TimeUnit is the time units, specified in the TimeUnit property, of the discretized system. Takes positive scalar values. A value of 0 corresponds to the standard 'tustin' method without prewarp.

Default: 0

'FractDelayApproxOrder'

Maximum order of the Thiran filter used to approximate fractional delays in the 'tustin' and 'matched' methods. Takes integer values. A value of 0 means that c2d rounds fractional delays to the nearest integer multiple of the sample time.

Default: 0

Examples

Discretize two models using identical discretization options.

```
% generate two arbitrary continuous-time state-space models
sys1 = rss(3, 2, 2);
sys2 = rss(4, 4, 1);
Use c2dOptions to create a set of discretization options.
opt = c2dOptions('Method', 'tustin', 'PrewarpFrequency', 3.4);
Then, discretize both models using the option set.
```

```
dsys1 = c2d(sys1, 0.1, opt); % 0.1s sample time
dsys2 = c2d(sys2, 0.2, opt); % 0.2s sample time
The c2dOptions option set does not include the sample time Ts. You can use the same
discretization options to discretize systems using a different sample time.
```

References

[1] Franklin, G.F., Powell, D.J., and Workman, M.L., *Digital Control of Dynamic Systems* (3rd Edition), Prentice Hall, 1997.

See Also

c2d

Introduced in R2010a

canon

State-space canonical realization

Syntax

```
csys = canon(sys,type)
[csys,T]= canon(sys,type)
csys = canon(sys,'modal',condt)
```

Description

csys = canon(sys,type) transforms the linear model sys into a canonical statespace model csys. The argument type specifies whether csys is in modal or companion form.

[csys,T]= canon(sys,type) also returns the state-coordinate transformation T that relates the states of the state-space model sys to the states of csys.

csys = canon(sys, 'modal', condt) specifies an upper bound condt on the condition
number of the block-diagonalizing transformation.

Input Arguments

sys

Any linear dynamic system model, except for frd models.

type

String specifying the type of canonical form of **csys**. **type** can take one of the two following values:

- 'modal' convert sys to modal form.
- 'companion' convert sys to companion form.

condt

Positive scalar value specifying an upper bound on the condition number of the blockdiagonalizing transformation that converts **sys** to **csys**. This argument is available only when **type** is 'modal'.

Increase condt to reduce the size of the eigenvalue clusters in the A matrix of csys. Setting condt = Inf diagonalizes A.

Default: 1e8

Output Arguments

csys

State-space (SS) model. CSYS is a state-space realization of SYS in the canonical form specified by type.

т

Matrix specifying the transformation between the state vector x of the state-space model sys and the state vector x_c of csys:

 $x_c = Tx$

This argument is available only when **sys** is state-space model.

Examples

This example uses **canon** to convert a system having doubled poles and clusters of close poles to modal canonical form.

Consider the system G having the following transfer function:

$$G(s) = 100 \frac{(s-1)(s+1)}{s(s+10)(s+10.0001)(s-(1+i))^2 (s-(1-i))^2}.$$

To create a linear model of this system and convert it to modal canonical form, enter:

G = zpk([1 -1],[0 -10 -10.0001 1+1i 1-1i 1+1i 1-1i],100); Gc = canon(G,'modal');

The system *G* has a pair of nearby poles at s = -10 and s = -10.0001. *G* also has two complex poles of multiplicity 2 at s = 1 + i and s = 1 - i. As a result, the modal form, has a block of size 2 for the two poles near s = -10, and a block of size 4 for the complex eigenvalues. To see this, enter the following command:

Gc.A

ans =

0	0	0	0	0	0	0
0	1.0000	1.0000	0	0	0	0
0	-1.0000	1.0000	2.0548	0	0	0
0	0	0	1.0000	1.0000	0	0
0	0	0	-1.0000	1.0000	0	0
0	0	0	0	0	-10.0000	8.0573
0	0	0	0	0	0	-10.0001

To separate the two poles near s = -10, you can increase the value of condt. For example:

```
Gc2 = canon(G,'modal',1e10);
Gc2.A
```

ans =

0	0	0	0	0	0	0
0	1.0000	1.0000	0	0	0	0
0	-1.0000	1.0000	2.0548	0	0	0
0	0	0	1.0000	1.0000	0	0
0	0	0	-1.0000	1.0000	0	0
0	0	0	0	0	-10.0000	0
0	0	0	0	0	0	-10.0001

The *A* matrix of **GC2** includes separate diagonal elements for the poles near s = -10. The cost of increasing the maximum condition number of *A* is that the *B* matrix includes some large values.

format shortE Gc2.B ans = 3.2000e-001 -6.5691e-003 5.4046e-002 -1.9502e-001 1.0637e+000 3.2533e+005 3.2533e+005

This example estimates a state-space model that is freely parameterized and convert to companion form after estimation.

```
load icEngine.mat
z = iddata(y,u,0.04);
FreeModel = n4sid(z,4,'InputDelay',2);
CanonicalModel = canon(FreeModel, 'companion')
```

Obtain the covariance of the resulting form by running a zero-iteration update to model parameters.

```
opt = ssestOptions; opt.SearchOption.MaxIter = 0;
CanonicalModel = ssest(z, CanonicalModel, opt)
```

Compare frequency response confidence bounds of FreeModel to CanonicalModel.

```
h = bodeplot(FreeModel, CanonicalModel)
```

the bounds are identical.

More About

Modal Form

In modal form, A is a block-diagonal matrix. The block size is typically 1-by-1 for real eigenvalues and 2-by-2 for complex eigenvalues. However, if there are repeated eigenvalues or clusters of nearby eigenvalues, the block size can be larger.

For example, for a system with eigenvalues $(\lambda_1, \sigma \pm j\omega, \lambda_2)$, the modal *A* matrix is of the form

ſλ	L 0	0	0]
0	σ	ω	0
0	-ω	σ	0
	0	0	λ_2

Companion Form

In the companion realization, the characteristic polynomial of the system appears explicitly in the rightmost column of the A matrix. For a system with characteristic polynomial

$$p(s) = s^n + \alpha_1 s^{n-1} + \ldots + \alpha_{n-1} s + \alpha_n$$

the corresponding companion A matrix is

A =	0	0			0	
	1	0	0	••	0 : :	$-\alpha_n - 1$
	0	1	0		:	:
	:	0		1	:	:
	0			1	0	$-\alpha_2$
	0		••	0	1	$-\alpha_1$

The companion transformation requires that the system be controllable from the first input. The companion form is poorly conditioned for most state-space computations; avoid using it when possible.

Algorithms

The canon command uses the bdschur command to convert sys into modal form and to compute the transformation T. If sys is not a state-space model, the algorithm first converts it to state space using ss.

The reduction to companion form uses a state similarity transformation based on the controllability matrix [1].

References

[1] Kailath, T. Linear Systems, Prentice-Hall, 1980.

See Also

ctrb | ctrbf | ss2ss

Introduced before R2006a

care

Continuous-time algebraic Riccati equation solution

Syntax

```
[X,L,G] = care(A,B,Q)
[X,L,G] = care(A,B,Q,R,S,E)
[X,L,G,report] = care(A,B,Q,...)
[X1,X2,D,L] = care(A,B,Q,..., 'factor')
```

Description

[X,L,G] = care(A,B,Q) computes the unique solution X of the continuous-time algebraic Riccati equation

 $A^T X + XA - XBB^T X + Q = 0$

The care function also returns the gain matrix, $G = R^{-1}B^T X E$.

[X,L,G] = care(A,B,Q,R,S,E) solves the more general Riccati equation

 $\boldsymbol{A}^T\boldsymbol{X}\boldsymbol{E} + \boldsymbol{E}^T\boldsymbol{X}\boldsymbol{A} - (\boldsymbol{E}^T\boldsymbol{X}\boldsymbol{B} + \boldsymbol{S})\boldsymbol{R}^{-1}(\boldsymbol{B}^T\boldsymbol{X}\boldsymbol{E} + \boldsymbol{S}^T) + \boldsymbol{Q} = \boldsymbol{0}$

When omitted, R, S, and E are set to the default values R=I, S=0, and E=I. Along with the solution X, care returns the gain matrix $G = R^{-1}(B^T XE + S^T)$ and a vector L of closed-loop eigenvalues, where

L=eig(A-B*G,E)

[X,L,G,report] = care(A,B,Q,...) returns a diagnosis report with:

- -1 when the associated Hamiltonian pencil has eigenvalues on or very near the imaginary axis (failure)
- -2 when there is no finite stabilizing solution \boldsymbol{X}

This syntax does not issue any error message when X fails to exist.

[X1, X2, D, L] = care(A, B, Q, ..., 'factor') returns two matrices X1, X2 and a diagonal scaling matrix D such that $X = D^*(X2/X1)^*D$.

The vector L contains the closed-loop eigenvalues. All outputs are empty when the associated Hamiltonian matrix has eigenvalues on the imaginary axis.

Examples

Example 1

Solve Algebraic Riccati Equation

Given

$$A = \begin{bmatrix} -3 & 2\\ 1 & 1 \end{bmatrix} \qquad B = \begin{bmatrix} 0\\ 1 \end{bmatrix} \qquad C = \begin{bmatrix} 1 & -1 \end{bmatrix} \qquad R = 3$$

you can solve the Riccati equation

$$A^T X + XA - XBR^{-1}B^T X + C^T C = 0$$

by

```
a = [-3 2;1 1]
b = [0 ; 1]
c = [1 -1]
r = 3
[x,l,g] = care(a,b,c'*c,r)
```

This yields the solution

x x = 0.5895 1.8216 1.8216 8.8188

You can verify that this solution is indeed stabilizing by comparing the eigenvalues of a and a-b*g.

```
[eig(a) eig(a-b*g)]
ans =
    -3.4495 -3.5026
    1.4495 -1.4370
```

Finally, note that the variable 1 contains the closed-loop eigenvalues eig(a-b*g).

```
1
1 =
-3.5026
-1.4370
```

Example 2

Solve H-infinity (H_∞)-like Riccati Equation

To solve the $\,H_{\!\infty}$ -like Riccati equation

$$A^{T}X + XA + X(\gamma^{-2}B_{1}B_{1}^{T} - B_{2}B_{2}^{T})X + C^{T}C = 0$$

rewrite it in the care format as

$$A^{T}X + XA - X[\underbrace{B_{1}, B_{2}}_{B}] \underbrace{\begin{bmatrix} -\gamma^{2}I & 0\\ 0 & I \end{bmatrix}}_{R}^{-1} \begin{bmatrix} B_{1}^{T}\\ B_{2}^{T} \end{bmatrix} X + C^{T}C = 0$$

You can now compute the stabilizing solution X by

```
B = [B1 , B2]
m1 = size(B1,2)
m2 = size(B2,2)
R = [-g^2*eye(m1) zeros(m1,m2) ; zeros(m2,m1) eye(m2)]
```

X = care(A,B,C'*C,R)

Limitations

The (A, B) pair must be stabilizable (that is, all unstable modes are controllable). In addition, the associated Hamiltonian matrix or pencil must have no eigenvalue on the imaginary axis. Sufficient conditions for this to hold are (Q, A) detectable when S = 0 and R > 0, or

$$\begin{bmatrix} Q & S \\ S^T & R \end{bmatrix} > 0$$

More About

Algorithms

care implements the algorithms described in [1]. It works with the Hamiltonian matrix when R is well-conditioned and E = I; otherwise it uses the extended Hamiltonian pencil and QZ algorithm.

References

 Arnold, W.F., III and A.J. Laub, "Generalized Eigenproblem Algorithms and Software for Algebraic Riccati Equations," *Proc. IEEE*, 72 (1984), pp. 1746-1754

See Also

dare | lyap

Introduced before R2006a

chgFreqUnit

Change frequency units of frequency-response data model

Syntax

```
sys_new = chgFreqUnit(sys,newfrequnits)
```

Description

sys_new = chgFreqUnit(sys,newfrequnits) changes units of the frequency points
in sys to newfrequnits. Both Frequency and FrequencyUnit properties of sys
adjust so that the frequency responses of sys and sys_new match.

Input Arguments

sys

Frequency-response data (frd, idfrd, or genfrd) model

newfrequnits

New units of frequency points, specified as one of the following strings:

- 'rad/TimeUnit'
- 'cycles/TimeUnit'
- 'rad/s'
- 'Hz'
- 'kHz'
- 'MHz'
- 'GHz'
- 'rpm'

rad/TimeUnit and cycles/TimeUnit express frequency units relative to the system time units specified in the TimeUnit property.

Default: 'rad/TimeUnit'

Output Arguments

sys_new

Frequency-response data model of the same type as **sys** with new units of frequency points. The frequency response of **sys_new** is same as **sys**.

Examples

This example shows how to change units of the frequency points in a frequency-response data model.

1 Create a frequency-response data model.

```
load AnalyzerData;
sys = frd(resp,freq);
```

The data file AnalyzerData has column vectors freq and resp. These vectors contain 256 test frequencies and corresponding complex-valued frequency response points, respectively. The default frequency units of sys is rad/TimeUnit, where TimeUnit is the system time units.

2 Change the frequency units.

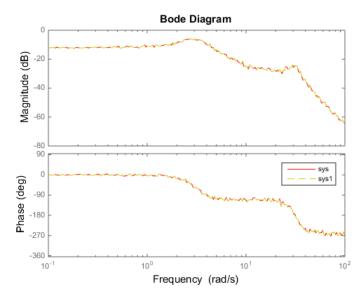
```
sys1 = chgFreqUnit(sys,'rpm');
```

The FrequencyUnit property of sys1 is rpm.

3 Compare the Bode responses of **sys** and **sys1**.

```
bodeplot(sys,'r',sys1,'y--');
legend('sys','sys1')
```

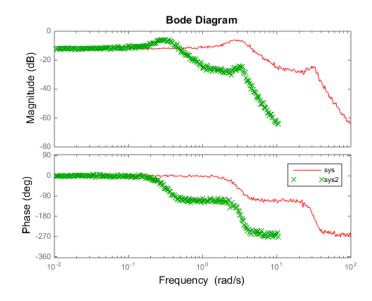
The magnitude and phase of sys and sys1 match.



4 (Optional) Change the FrequencyUnit property of sys to compare the Bode response with the original system.

sys2=sys; sys2.FrequencyUnit = 'rpm'; bodeplot(sys,'r',sys2,'gx'); legend('sys','sys2');

Changing the FrequencyUnit property changes the original system. Therefore, the Bode responses of sys and sys2 do not match. For example, the original corner frequency at 2 rad/s changes to 2 rpm (or 0.2 rad/s).



More About

Tips

• Use chgFreqUnit to change the units of frequency points without modifying system behavior.

See Also

chgTimeUnit | frd

Introduced in R2011a

chgTimeUnit

Change time units of dynamic system

Syntax

```
sys_new = chgTimeUnit(sys,newtimeunits)
```

Description

sys_new = chgTimeUnit(sys,newtimeunits) changes the time units of sys to newtimeunits. The time- and frequency-domain characteristics of sys and sys_new match.

Input Arguments

sys

Dynamic system model

newtimeunits

New time units, specified as one of the following strings:

- 'nanoseconds'
- 'microseconds'
- 'milliseconds'
- 'seconds'
- 'minutes'
- 'hours'
- 'days'
- 'weeks'

- 'months'
- 'years'

Default: 'seconds'

Output Arguments

sys_new

Dynamic system model of the same type as **sys** with new time units. The time response of **sys_new** is same as **sys**.

If **sys** is an identified linear model, both the model parameters as and their minimum and maximum bounds are scaled to the new time units.

Examples

Change Time Units of Dynamic System Model

Create a transfer function model.

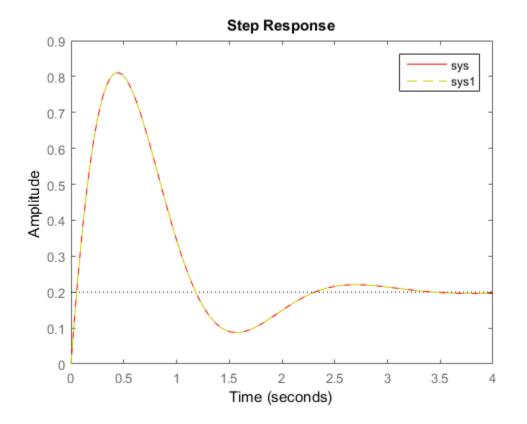
```
num = [4 2];
den = [1 3 10];
sys = tf(num,den);
```

By default, the time unit of **sys** is '**seconds**'. Create a new model with the time units changed to minutes.

```
sys1 = chgTimeUnit(sys,'minutes');
```

This command sets the TimeUnit property of sys1 to 'minutes', without changing the dynamics. To confirm that the dynamics are unchanged, compare the step responses of sys and sys1.

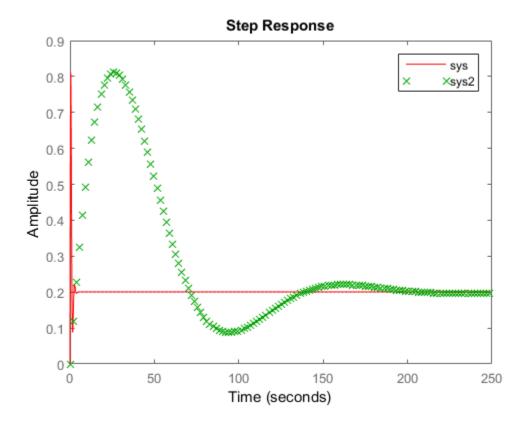
```
stepplot(sys,'r',sys1,'y--');
legend('sys','sys1');
```



The step responses are the same.

If you change the TimeUnit property of the system instead of using ChgTimeUnit, the dynamics of the system do change. To see this, change the TimeUnit property of a copy of sys and compare the step response with the original system.

```
sys2 = sys;
sys2.TimeUnit = 'minutes';
stepplot(sys,'r',sys2,'gx');
legend('sys','sys2');
```



The step responses of sys and sys2 do not match. For example, the original rise time of 0.04 seconds changes to 0.04 minutes.

• "Specify Model Time Units"

More About

Tips

• Use chgTimeUnit to change the time units without modifying system behavior.

See Also

chgFreqUnit | tf | zpk | ss | frd | pid

Introduced in R2011a

conj

Form model with complex conjugate coefficients

Syntax

sysc = conj(sys)

Description

sysc = **conj**(**sys**) constructs a complex conjugate model **sysc** by applying complex conjugation to all coefficients of the LTI model **sys**. This function accepts LTI models in transfer function (TF), zero/pole/gain (ZPK), and state space (SS) formats.

Examples

If sys is the transfer function

(2+i)/(s+i)

then conj(sys) produces the transfer function

(2-i)/(s-i)

This operation is useful for manipulating partial fraction expansions.

See Also append | ss | tf | zpk

Introduced before R2006a

connect

Block diagram interconnections of dynamic systems

Syntax

```
sysc = connect(sys1,...,sysN,inputs,outputs)
sysc = connect(sys1,...,sysN,inputs,outputs,APs)
sysc = connect(blksys,connections,inputs,outputs)
sysc = connect(____,opts)
```

Description

sysc = connect(sys1,...,sysN,inputs,outputs) connects the block diagram elements sys1,...,sysN based on signal names. The block diagram elements sys1,...,sysN are dynamic system models. These models can include summing junctions that you create using sumblk. The connect command interconnects the block diagram elements by matching the input and output signals that you specify in the InputName and OutputName properties of sys1,...,sysN. The aggregate model sysc is a dynamic system model having inputs and outputs specified by inputs and outputs respectively.

sysc = connect(sys1,...,sysN,inputs,outputs,APs) inserts an AnalysisPoint at every signal location specified in APs. Use analysis points to mark locations of interest which are internal signals in the aggregate model. For instance, a location at which you want to extract a loop transfer function or measure the stability margins is a location of interest.

sysc = connect(blksys,connections,inputs,outputs) uses index-based interconnection to build sysc out of an aggregate, unconnected model blksys. The matrix connections specifies how the outputs and inputs of blksys interconnect. For index-based interconnections, inputs and outputs are index vectors that specify which inputs and outputs of blksys are the external inputs and outputs of sysc. This syntax can be convenient when you do not want to assign names to all inputs and outputs of all models to connect. However, in general, it is easier to keep track of named signals.

sysc = connect(_____, opts) builds the interconnected model using additional
options. You can use opts with the input arguments of any of the previous syntaxes.

Input Arguments

sys1,...,sysN

Dynamic system models that correspond to the elements of your block diagram. For example, the elements of your block diagram can include one or more tf or ss models that represent plant dynamics. Block diagram elements can also include a pid or ltiblock.pid model representing a controller. You can also include one or more summing junction that you create using sumblk. Provide multiple arguments sys1,...,sysN to represent all of the block diagram elements and summing junctions.

inputs

For name-based interconnection, a string or string vector that specifies the inputs of the aggregate model sysc. The strings in inputs must correspond to entries in the InputName or OutputName property of one or more of the block diagram elements sys1,...,sysN.

outputs

For name-based interconnection, a string or string vector that specifies the outputs of the aggregate model sysc. The strings in outputs must correspond to entries in the OutputName property of one or more of the block diagram elements sys1,...,sysN.

APs

A string or string vector that specifies locations (internal signals) of interest in the aggregate model. The resulting model contains an analysis point at each such location. (See AnalysisPoint). Each string in APs must correspond to an entry in the InputName or OutputName property of one or more of the block diagram elements sys1,...,sysN.

blksys

Unconnected aggregate model. To obtain blksys, use append to join dynamic system models of the elements of your block diagram. For example, if your block diagram contains dynamic system models C, G, and S, create blksys with the following command:

blksys = append(C,G,S)

connections

Matrix that specifies the connections and summing junctions of the block diagram. Each row of connections specifies one connection or summing junction in terms of the input vector u and output vector y of the unconnected aggregate model blksys. For example, the row:

[3 2 0 0]

specifies that y(2) connects into u(3). The row

[7 2 -15 6]

indicates that y(2) - y(15) + y(6) feeds into u(7).

If you do not specify any connection for a particular input or output, **connect** omits that input or output from the aggregate model.

opts

Additional options for interconnection, specified as an options set that you create with connectOptions.

Output Arguments

sysc

Interconnected system, returned as either a state-space model or frequency-response model. The type of model returned depends on the input models. For example:

- Interconnecting numeric LTI models (other than frd models) returns an ss model.
- Interconnecting a numeric LTI model with a Control Design Block returns a generalized LTI model. For instance, interconnecting a tf model with an ltiblock.pid Control Design Block returns a genss.
- Interconnecting any model with frequency-response data model returns a frequency response data model.

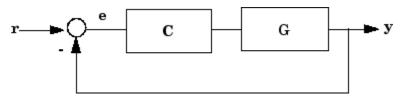
By default, connect automatically discards states that do not contribute to the I/O transfer function from the specified inputs to the specified outputs of the interconnected model. To retain the unconnected states, set the Simplify option of connectOptions to false. For example:

```
opt = connectOptions('Simplify',false);
sysc = connect(sys1,sys2,sys3,'r','y',opt);
```

Examples

SISO Feedback Loop

Create an aggregate model of the following block diagram from $\ensuremath{\mathsf{r}}$ to $\ensuremath{\mathsf{y}}.$



Create ${\bf C}$ and ${\bf G},$ and name the inputs and outputs.

```
C = pid(2,1);
C.u = 'e';
C.y = 'u';
G = zpk([],[-1,-1],1);
G.u = 'u';
G.y = 'y';
```

The notations C.u and C.y are shorthand expressions equivalent to C.InputName and C.OutputName, respectively. For example, entering C.u = 'e' is equivalent to entering C.InputName = 'e'. The command sets the InputName property of C to the value 'e'.

Create the summing junction.

Sum = sumblk('e = r - y');

Combine C, G, and the summing junction to create the aggregate model from \boldsymbol{r} to $\boldsymbol{y}.$

T = connect(G,C,Sum, 'r', 'y');

connect automatically joins inputs and outputs with matching names.

MIMO Feedback Loop

Create the control system of the previous example where ${\tt G}$ and ${\tt C}$ are both 2-input, 2-output models.

```
C = [pid(2,1),0;0,pid(5,6)];
C.InputName = 'e';
C.OutputName = 'u';
G = ss(-1,[1,2],[1;-1],0);
G.InputName = 'u';
G.OutputName = 'y';
```

When you specify single names for vector-valued signals, the software automatically performs vector expansion of the signal names. For example, examine the names of the inputs to C.

C.InputName

ans = 'e(1)' 'e(2)'

Create a 2-input, 2-output summing junction.

Sum = sumblk('e = r-y',2);

sumblk also performs vector expansion of the signal names.

Interconnect the models to obtain the closed-loop system.

T = connect(G,C,Sum, 'r', 'y');

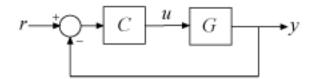
The block diagram elements G, C, and Sum are all 2-input, 2-output models. Therefore, connect performs the same vector expansion. connect selects all entries of the two-input signals 'r' and 'y' as inputs and outputs to T, respectively. For example, examine the input names of T.

T.InputName

ans = 'r(1)' 'r(2)'

Feedback Loop With Analysis Point Inserted by connect

Create a model of the following block diagram from r to y. Insert an analysis point at an internal location, u.



Create C and G, and name the inputs and outputs.

```
C = pid(2,1);
C.InputName = 'e';
C.OutputName = 'u';
G = zpk([],[-1,-1],1);
G.InputName = 'u';
G.OutputName = 'y';
```

Create the summing junction.

Sum = sumblk('e = r - y');

Combine C, G, and the summing junction to create the aggregate model, with an analysis point at u.

T = connect(G,C,Sum, 'r', 'y', 'u')

Τ =

Generalized continuous-time state-space model with 1 outputs, 1 inputs, 3 states, and AnalysisPoints : Analysis point, 1 channels, 1 occurrences.

Type "ss(T)" to see the current value, "get(T)" to see all properties, and "T.Blocks" \cdot

The resulting T is a genss model. The connect command creates the AnalysisPoint block, AnalysisPoints_, and inserts it into T. To see the name of the analysis point channel in AnalysisPoints_, use getPoints.

```
getPoints(T)
```

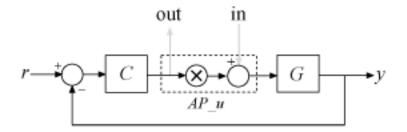
ans =

' u '

The analysis point channel is named 'u'. You can use this analysis point to extract system responses. For example, the following commands extract the open-loop transfer at u and the closed-loop response at y to a disturbance injected at u.

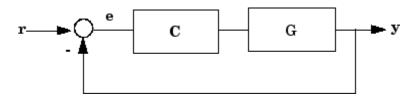
```
L = getLoopTransfer(T, 'u', -1);
Tuy = getIOTransfer(T, 'u', 'y');
```

T is equivalent to the following block diagram, where AP_u designates the AnalysisPoint block AnalysisPoints_ with channel name u.



Index-Based Interconnection

Create an aggregate model of the following block diagram from \boldsymbol{r} to \boldsymbol{y} using index-based interconnection.



Create C, G, and the unconnected aggregate model blksys.

```
C = pid(2,1);
G = zpk([],[-1,-1],1);
blksys = append(C,G);
```

The inputs u(1), u(2) of blksys correspond to the inputs of C and G, respectively. The outputs w(1), w(2) of blksys correspond to the outputs of C and G, respectively.

Create the matrix connections, which specifies which outputs of blksys connect to which inputs of blksys.

```
connections = [2 1; 1 -2];
```

The first row indicates that W(1) connects to U(2); in other words, that the output of C connects to the input of G. The second row indicates that -W(2) connects to U(1); in other words, that the negative of the output of G connects to the input of C.

Create the connected aggregate model from r to y.

```
T = connect(blksys,connections,1,2)
```

The last two arguments specify the external inputs and outputs in terms of the indices of blksys. The argument 1 specifies that the external input connects to u(1). The last argument, 2, specifies that the external output connects from w(2).

More About

- "Multi-Loop Control System"
- "MIMO Control System"
- "MIMO Feedback Loop"
- "Mark Analysis Points in Closed-Loop Models"

See Also

| append | sumblk | AnalysisPoint | feedback | parallel | series | lft |
connectOptions

Introduced before R2006a

connectOptions

Options for the connect command

Syntax

opt = connectOptions
opt = connectOptions(Name,Value)

Description

opt = connectOptions returns the default options for connect.

opt = connectOptions(Name,Value) returns an options set with the options
specified by one or more Name,Value pair arguments.

Examples

Retain Unconnected States in Model Interconnection

Use connectOptions to cause the connect command to retain unconnected states in an interconnected model.

Suppose you have dynamic system models sys1, sys2, and sys3. Combine these dynamic system models to build an interconnected model with input 'r' and output 'y'. Set the option to retain states in the model that do not contribute to the dynamics in the path from 'r' or 'y'.

```
opt = connectOptions('Simplify',false);
sysc = connect(sys1,sys2,sys3,'r','y',opt);
```

Input Arguments

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside single

quotes (' '). You can specify several name and value pair arguments in any order as Name1, Value1,..., NameN, ValueN.

Example: 'Simplify',false

'Simplify' - Automatic elimination of unconnected states

true (default) | false

Automatic elimination of unconnected states, specified as either true or false.

- true connect eliminates all states that do not contribute to the I/O transfer function from the specified inputs to the specified outputs of the interconnected system.
- false connect retains unconnected states. This option can be useful, for example, when you want to compute the interconnected system response from known initial state values of the components.

Data Types: logical

Output Arguments

opt - Options for connect

connectOptions options set

Options for connect, returned as a connectOptions options set. Use opt as the last argument to connect when interconnecting models.

See Also

connect

Introduced in R2013b

controlSystemDesigner

Interactively design and tune SISO feedback loops

Syntax

```
controlSystemDesigner
controlSystemDesigner(plant)
controlSystemDesigner(plant,comp)
controlSystemDesigner(plant,comp,sensor,prefilt)
controlSystemDesigner(views)
controlSystemDesigner(views,plant,comp)
controlSystemDesigner(initdata)
controlSystemDesigner(sessiondata)
```

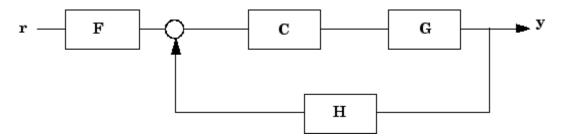
Description

controlSystemDesigner opens a SISO Design GUI (Control System Designer) for interactive compensator design. This GUI allows you to design a single-input/singleoutput (SISO) compensator using root locus, Bode diagram, Nichols and Nyquist techniques. You can also automatically design a compensator using this GUI.

By default, the SISO Design Tool:

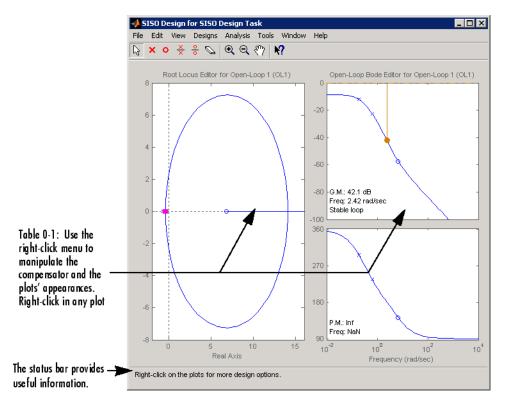
- Opens the Control and Estimation Tools Manager with a default SISO Design Task node.
- · Opens the Graphical Tuning editor with root locus and open-loop Bode diagrams.
- Places the compensator, C, in the forward path in series with the plant, G.
- Assumes the prefilter, **F**, and the sensor, **H**, are unity gains. Once you specify **G** and **H**, they are *fixed* in the feedback structure.

The default control architecture is shown in this figure.



There are six control architectures available. See sisoinit for more information.

This picture shows the SISO Design Graphical editor.



controlSystemDesigner(plant) opens the SISO Design Tool, imports plant, and initializes the plant model G to plant. plant can be any SISO LTI model created with ss, tf, zpk or frd, or a row or column array of LTI models.

controlSystemDesigner(plant,comp) initializes the plant model G to plant, the compensator C to comp. comp is an LTI object.

controlSystemDesigner(plant, comp, sensor, prefilt) initializes the plant G to plant, compensator C to comp, sensor H to sensor, and the prefilter F to prefilt. sensor is an LTI object or a row or column array of LTI objects. If plant is also an array of LTI objects, the lengths of sensor and plant must match. prefilt is an LTI object.

controlSystemDesigner(views) or

controlSystemDesigner(views,plant,comp) specifies the initial configuration of the SISO Design Tool. views can be any of the following strings (or combination thereof):

- 'rlocus' Root Locus plot
- 'bode' Bode diagrams of the open-loop response
- 'nichols' Nichols plot
- <code>'filter'</code> Bode diagrams of the prefilter F and the closed-loop response from the command into F to the output of the plant G .

For example

controlSystemDesigner('bode')

opens a SISO Design Tool with only the Bode Diagrams. If there is more than one view, the views are specified in a cell array.

controlSystemDesigner(initdata) initializes the SISO Design Tool with more general control system configurations. Use **sisoinit** to create the initialization data structure initdata.

controlSystemDesigner(sessiondata) opens the SISO Design Tool with a previously saved session where sessiondata is the MAT-file for the saved session.

Examples

Launch SISO Design Tool GUI in default configuration using LTI models:

```
% Create plant G.
G = tf(1, [1 1]);
% Create controller C.
C = tf(1,[1 2]);
```

```
% Launch the GUI.
controlSystemDesigner(G,C)
```

Launch SISO Design Tool GUI in default configuration using an array of LTI models:

```
% Specify model parameters.
m = 3;
b = 0.5;
k = 8:1:10;
T = 0.1:.05:.2;
% Create an LTI array to model variations in plant G.
for ct = 1:length(k);
    G(:,:,ct) = tf(1,[m,b,k(ct)]);
end
% Create an LTI array to model variations in sensor H.
for ct = 1:length(T);
    H(:,:,ct) = tf(1,[1/T(ct), 1]);
end
% Create a controller C.
C = tf(1, [1 2]);
% Launch the GUI.
controlSystemDesigner(G,C,H)
```

Alternatives

You can open the SISO Design GUI from the MATLAB desktop. In the **Apps** tab, in the **Control System Design and Analysis** section of the Apps gallery, click **Control System Designer**.

More About

"SISO Design Tool"

See Also

bode | linearSystemAnalyzer | | rlocus | nichols

Introduced in R2015a

covar

Output and state covariance of system driven by white noise

Syntax

P = covar(sys,W)
[P,Q] = covar(sys,W)

Description

covar calculates the stationary covariance of the output y of an LTI model sys driven by Gaussian white noise inputs w. This function handles both continuous- and discrete-time cases.

P = covar(sys,W) returns the steady-state output response covariance

$$P = E(yy^T)$$

given the noise intensity

$$\begin{split} E(w(t)w(\tau)^{T}) &= W\delta(t-\tau) \quad \text{(continuous time)} \\ E(w[k]w[l]^{T}) &= W\delta_{kl} \qquad \text{(discrete time)} \end{split}$$

[P,Q] = covar(sys,W) also returns the steady-state state covariance

$$Q = E(xx^T)$$

when sys is a state-space model (otherwise Q is set to []).

When applied to an N-dimensional LTI array sys, covar returns multidimensional arrays P, Q such that

P(:,:,i1,...iN) and Q(:,:,i1,...iN) are the covariance matrices for the model sys(:,:,i1,...iN).

Examples

Compute the output response covariance of the discrete SISO system

 $H(z) = \frac{2z+1}{z^2+0.2z+0.5}, \quad T_s = 0.1$

due to Gaussian white noise of intensity W = 5. Type

sys = tf([2 1],[1 0.2 0.5],0.1);
p = covar(sys,5)

These commands produce the following result.

p = 30.3167

You can compare this output of covar to simulation results.

The two covariance values ${\tt p}$ and ${\tt psim}$ do not agree perfectly due to the finite simulation horizon.

More About

Algorithms

Transfer functions and zero-pole-gain models are first converted to state space with ss.

For continuous-time state-space models

$$\dot{x} = Ax + Bw$$
$$y = Cx + Dw,$$

the steady-state state covariance Q is obtained by solving the Lyapunov equation

$$AQ + QA^T + BWB^T = 0.$$

In discrete time, the state covariance Q solves the discrete Lyapunov equation

$$AQA^T - Q + BWB^T = 0.$$

In both continuous and discrete time, the output response covariance is given by $P = CQC^T + DWD^T$. For unstable systems, P and Q are infinite. For continuous-time systems with nonzero feedthrough, covar returns Inf for the output covariance P.

References

[1] Bryson, A.E. and Y.C. Ho, *Applied Optimal Control*, Hemisphere Publishing, 1975, pp. 458-459.

See Also

dlyap | lyap

Introduced before R2006a

ctrb

Controllability matrix

Syntax

Co = ctrb(sys)

Description

ctrb computes the controllability matrix for state-space systems. For an n-by-n matrix A and an n-by-m matrix B, ctrb(A,B) returns the controllability matrix

 $Co = \begin{bmatrix} B & AB & A^2B & \dots & A^{n-1}B \end{bmatrix}$

where Co has n rows and nm columns.

Co = ctrb(sys) calculates the controllability matrix of the state-space LTI object sys. This syntax is equivalent to executing

Co = ctrb(sys.A,sys.B)

The system is controllable if Co has full rank n.

Examples

Check if the system with the following data

```
A = \frac{1 & 1}{4 & -2}B = \frac{1 & -1}{1 & -1}
```

is controllable. Type

```
Co=ctrb(A,B);
% Number of uncontrollable states
unco=length(A)-rank(Co)
```

These commands produce the following result.

unco = 1

Limitations

Estimating the rank of the controllability matrix is ill-conditioned; that is, it is very sensitive to roundoff errors and errors in the data. An indication of this can be seen from this simple example.

$$A = \begin{bmatrix} 1 & \delta \\ 0 & 1 \end{bmatrix}, B = \begin{bmatrix} 1 \\ \delta \end{bmatrix}$$

This pair is controllable if $\delta \neq 0$ but if $\delta < \sqrt{eps}$, where *eps* is the relative machine precision. ctrb(A,B) returns

$$\begin{bmatrix} B & AB \end{bmatrix} = \begin{bmatrix} 1 & 1 \\ \delta & \delta \end{bmatrix}$$

which is not full rank. For cases like these, it is better to determine the controllability of a system using ctrbf.

See Also ctrbf | obsv

Introduced before R2006a

ctrbf

Compute controllability staircase form

Syntax

```
[Abar,Bbar,Cbar,T,k] = ctrbf(A,B,C)
ctrbf(A,B,C,tol)
```

Description

If the controllability matrix of (A, B) has rank $r \le n$, where *n* is the size of *A*, then there exists a similarity transformation such that

 $\bar{A} = TAT^T, \quad \bar{B} = TB, \quad \bar{C} = CT^T$

where T is unitary, and the transformed system has a *staircase* form, in which the uncontrollable modes, if there are any, are in the upper left corner.

$$\bar{A} = \begin{bmatrix} A_{uc} & 0 \\ A_{21} & A_c \end{bmatrix}, \quad \bar{B} = \begin{bmatrix} 0 \\ B_c \end{bmatrix}, \quad \bar{C} = \begin{bmatrix} C_{nc}C_c \end{bmatrix}$$

where (A_c, B_c) is controllable, all eigenvalues of A_{uc} are uncontrollable, and $C_c(sI - A_c)^{-1}B_c = C(sI - A)^{-1}B$.

[Abar, Bbar, Cbar, T, k] = ctrbf(A, B, C) decomposes the state-space system represented by A, B, and C into the controllability staircase form, Abar, Bbar, and Cbar, described above. T is the similarity transformation matrix and k is a vector of length n, where n is the order of the system represented by A. Each entry of k represents the number of controllable states factored out during each step of the transformation matrix calculation. The number of nonzero elements in k indicates how many iterations were necessary to calculate T, and sum(k) is the number of states in A_c , the controllable portion of Abar. ctrbf(A,B,C,tol) uses the tolerance tol when calculating the controllable/ uncontrollable subspaces. When the tolerance is not specified, it defaults to 10*n*norm(A,1)*eps.

Examples

Compute the controllability staircase form for

 $A = \frac{1}{4} - \frac{1}{2}$ $B = \frac{1}{1} - \frac{1}{1}$ $C = \frac{1}{0} - \frac{1}{1}$

and locate the uncontrollable mode.

```
[Abar,Bbar,Cbar,T,k]=ctrbf(A,B,C)
Abar =
   -3.0000
                    0
   -3.0000
               2.0000
Bbar =
    0.0000
               0.0000
    1.4142
              -1.4142
Cbar =
   -0.7071
               0.7071
    0.7071
               0.7071
T =
   -0.7071
               0.7071
    0.7071
               0.7071
k =
     1
            0
```

More About

controllable mode located at 2.

Algorithms

ctrbf implements the Staircase Algorithm of [1].

References

[1] Rosenbrock, M.M., State-Space and Multivariable Theory, John Wiley, 1970.

See Also

ctrb | minreal

Introduced before R2006a

ctrlpref

Set Control System Toolbox preferences

Syntax

ctrlpref

Description

ctrlpref opens a Graphical User Interface (GUI) which allows you to change the Control System ToolboxTM preferences. Preferences set in this GUI affect future plots only (existing plots are not altered).

Your preferences are stored to disk (in a system-dependent location) and will be automatically reloaded in future MATLAB sessions using the Control System Toolbox software.

See Also

controlSystemDesigner | linearSystemAnalyzer

Introduced in R2006a

d2c

Convert model from discrete to continuous time

Syntax

```
sysc = d2c(sysd)
sysc = d2c(sysd,method)
sysc = d2c(sysd,opts)
[sysc,G] = d2c(sysd,method,opts)
```

Description

sysc = d2c(sysd) produces a continuous-time model sysc that is equivalent to the discrete-time dynamic system model sysd using zero-order hold on the inputs.

sysc = d2c(sysd,method) uses the specified conversion method method.

sysc = d2c(sysd,opts) converts sysd using the option set opts, specified using the d2cOptions command.

[sysc,G] = d2c(sysd,method,opts) returns a matrix G that maps the states xd[k] of the state-space model sysd to the states xc(t) of sysc.

Input Arguments

sysd

Discrete-time dynamic system model

You cannot directly use an idgrey model with FcnType='d' with d2c. Convert the model into idss form first.

Default:

method

String specifying a discrete-to-continuous time conversion method:

- 'zoh' Zero-order hold on the inputs. Assumes the control inputs are piecewise constant over the sampling period.
- 'foh' Linear interpolation of the inputs (modified first-order hold). Assumes the control inputs are piecewise linear over the sampling period.
- 'tustin' Bilinear (Tustin) approximation to the derivative.
- 'matched' Zero-pole matching method of [1] (for SISO systems only).

```
Default: 'zoh'
```

opts

Discrete-to-continuous time conversion options, created using d2cOptions.

Output Arguments

sysc

Continuous-time model of the same type as the input system sysd.

When sysd is an identified (IDLTI) model, sysc:

- Includes both the measured and noise components of sysd. If the noise variance is λ in sysd, then the continuous-time model sysc has an indicated level of noise spectral density equal to $Ts^*\lambda$.
- Does not include the estimated parameter covariance of sysd. If you want to translate the covariance while converting the model, use translatecov.

G

Matrix mapping the states xd[k] of the state-space model sysd to the states xc(t) of sysc:

$$x_c(kT_s) = G\begin{bmatrix} x_d[k] \\ u[k] \end{bmatrix}.$$

Given an initial condition x0 for sysd and an initial input u0 = u[0], the corresponding initial condition for sysc (assuming u[k] = 0 for k < 0 is given by:

$$x_{c}(0) = G\begin{bmatrix} x_{0} \\ u_{0} \end{bmatrix}.$$

Examples

Example 1

Consider the following discrete-time transfer function:

$$H(z) = \frac{z-1}{z^2 + z + 0.3}$$

Suppose the model has sample time $T_s = 0.1$ s. You can derive a continuous-time zeroorder-hold equivalent model with the following commands:

```
H = tf([1 -1], [1 1 0.3], 0.1);
Hc = d2c(H)
Hc =
121.7 s + 3.026e-12
s^2 + 12.04 s + 776.7
```

Continuous-time transfer function.

Discretizing the resulting model HC with the default zero-order hold method and sample time $T_s = 0.1$ s returns the original discrete model H(z):

To use the Tustin approximation instead of zero-order hold, type

Hc = d2c(H, 'tustin');

As with zero-order hold, the inverse discretization operation

```
c2d(Hc,0.1, 'tustin');
```

gives back the original H(z).

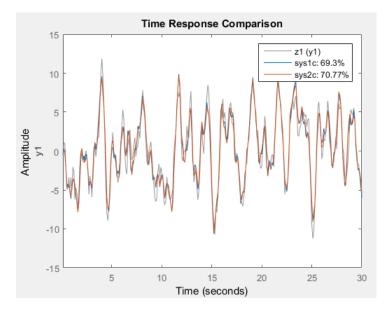
Example 2

Convert an identified transfer function and compare its performance against a directly estimated continuous-time model.

```
load iddata1
sys1d = tfest(z1,2,'Ts',0.1);
sys1c = d2c(sys1d,'zoh');
sys2c = tfest(z1,2);
```

compare(z1,sys1c,sys2c)

The two systems are virtually identical.



Example 3

Analyze the effect of parameter uncertainty on frequency response across d2c operation on an identified model.

```
load iddata1
sysd = tfest(z1, 2, 'Ts', 0.1);
sysc = d2c(sysd, 'zoh');
```

sys1c has no covariance information. Regenerate it using a zero iteration update with the same estimation command and estimation data:

```
opt = tfestOptions;
opt.SearchOption.MaxIter = 0;
sys1c = tfest(z1, sysc, opt);
h = bodeplot(sysd, sysc);
showConfidence(h)
```

The uncertainties of **sysc** and **sysd** are comparable up to the Nyquist frequency. However, **sysc** exhibits large uncertainty in the frequency range for which the estimation data does not provide any information.

If you do not have access to the estimation data, use translatecov which is a Gaussapproximation formula based translation of covariance across model type conversion operations.

Limitations

The Tustin approximation is not defined for systems with poles at z = -1 and is illconditioned for systems with poles near z = -1.

The zero-order hold method cannot handle systems with poles at z = 0. In addition, the 'zoh' conversion increases the model order for systems with negative real poles, [2]. The model order increases because the matrix logarithm maps real negative poles to complex poles. Single complex poles are not physically meaningful because of their complex time response.

Instead, to ensure that all complex poles of the continuous model come in conjugate pairs, d2c replaces negative real poles z = -a with a pair of complex conjugate poles near -a.

The conversion then yields a continuous model with higher order. For example, to convert the discrete-time transfer function

$$H(z) = \frac{z + 0.2}{(z + 0.5)(z^2 + z + 0.4)}$$

type:

Ts = 0.1 % sample time 0.1 s H = zpk(-0.2,-0.5,1,Ts) * tf(1,[1 1 0.4],Ts) Hc = d2c(H)

These commands produce the following result.

Warning: System order was increased to handle real negative poles.

Zero/pole/gain: -33.6556 (s-6.273) (s^2 + 28.29s + 1041) (s^2 + 9.163s + 637.3) (s^2 + 13.86s + 1035)

To convert Hc back to discrete time, type:

c2d(Hc,Ts)

yielding

Zero/pole/gain: (z+0.5) (z+0.2) (z+0.5)^2 (z^2 + z + 0.4)

Sample time: 0.1

This discrete model coincides with H(z) after canceling the pole/zero pair at z = -0.5.

More About

Tips

• Use the syntax sysc = d2c(sysd, 'method') to convert sysd using the default options for 'method'. To specify tustin conversion with a frequency prewarp (formerly the 'prewarp' method), use the syntax sysc = d2c(sysd,opts). See the d2cOptions reference page for more information.

Algorithms

d2c performs the 'zoh' conversion in state space, and relies on the matrix logarithm (see logm in the MATLAB documentation).

See "Continuous-Discrete Conversion Methods" for more details on the conversion methods.

References

- [1] Franklin, G.F., Powell,D.J., and Workman, M.L., *Digital Control of Dynamic Systems* (3rd Edition), Prentice Hall, 1997..
- [2] Kollár, I., G.F. Franklin, and R. Pintelon, "On the Equivalence of z-domain and s-domain Models in System Identification," *Proceedings of the IEEE Instrumentation and Measurement Technology Conference*, Brussels, Belgium, June, 1996, Vol. 1, pp. 14-19.

See Also

c2d | d2d | d2cOptions | translatecov | logm

Introduced before R2006a

d2cOptions

Create option set for discrete- to continuous-time conversions

Syntax

```
opts = d2cOptions
opts = d2cOptions(Name,Value)
```

Description

opts = d2cOptions returns the default options for d2c.

opts = d2cOptions(Name,Value) creates an option set with the options specified by
one or more Name,Value pair arguments.

Input Arguments

Name-Value Pair Arguments

'method'

Discretization method, specified as one of the following values:

'zoh'	Zero-order hold, where $d2c$ assumes the control inputs are piecewise constant over the sample time Ts.
'foh'	Linear interpolation of the inputs (modified first-order hold). Assumes the control inputs are piecewise linear over the sampling period.
'tustin'	Bilinear (Tustin) approximation. By default, d2c converts with no prewarp. To include prewarp, use the PrewarpFrequency option.
'matched'	Zero-pole matching method. (See [1], p. 224.)

Default: 'zoh'

'PrewarpFrequency'

Prewarp frequency for 'tustin' method, specified in rad/TimeUnit, where TimeUnit is the time units, specified in the TimeUnit property, of the discrete-time system. Specify the prewarp frequency as a positive scalar value. A value of 0 corresponds to the 'tustin' method without prewarp.

Default: 0

For additional information about conversion methods, see "Continuous-Discrete Conversion Methods".

Examples

Convert a discrete-time model to continuous-time using the 'tustin' method with frequency prewarping.

Create the discrete-time transfer function

$$\frac{z+1}{z^2+z+1}$$

hd = tf([1 1], [1 1 1], 0.1); % 0.1s sample time To convert to continuous-time, use d2cOptions to create the option set.

```
opts = d2cOptions('Method', 'tustin', 'PrewarpFrequency', 20);
hc = d2c(hd, opts);
```

You can use opts to resample additional models using the same options.

References

[1] Franklin, G.F., Powell,D.J., and Workman, M.L., *Digital Control of Dynamic Systems* (3rd Edition), Prentice Hall, 1997.

See Also

d2c

Introduced in R2010a

d2d

Resample discrete-time model

Syntax

```
sys1 = d2d(sys, Ts)
sys1 = d2d(sys, Ts, 'method')
sys1 = d2d(sys, Ts, opts)
```

Description

sys1 = d2d(sys, Ts) resamples the discrete-time dynamic system model sys to produce an equivalent discrete-time model sys1 with the new sample time Ts (in seconds), using zero-order hold on the inputs.

sys1 = d2d(sys, Ts, 'method') uses the specified resampling method 'method':

- 'zoh' Zero-order hold on the inputs
- 'tustin' Bilinear (Tustin) approximation

sys1 = d2d(sys, Ts, opts) resamples sys using the option set with d2dOptions.

Examples

Example 1

Consider the zero-pole-gain model

$$H\left(z\right) = \frac{z - 0.7}{z - 0.5}$$

with sample time 0.1 s. You can resample this model at 0.05 s by typing

H = zpk(0.7, 0.5, 1, 0.1)

d2d

```
H2 = d2d(H,0.05)
Zero/pole/gain:
(z-0.8243)
(z-0.7071)
```

```
Sample time: 0.05
```

The inverse resampling operation, performed by typing d2d(H2,0.1), yields back the initial model H(z).

```
Zero/pole/gain:
(z-0.7)
(z-0.5)
Sample time: 0.1
```

Example 2

Suppose you estimates a discrete-time model of a sample time commensurate with the estimation data (Ts = 0.1 seconds). However, your deployment application demands a faster sampling frequency (Ts = 0.01 seconds).

```
load iddata1
sys = oe(z1, [2 2 1]);
sysFast = d2d(sys, 0.01, 'zoh')
```

bode(sys, sysFast)

More About

Tips

- Use the syntax sys1 = d2d(sys, Ts, 'method') to resample sys using the default options for 'method'. To specify tustin resampling with a frequency prewarp (formerly the 'prewarp' method), use the syntax sys1 = d2d(sys, Ts, opts). See the d2dOptions reference page.
- When **sys** is an identified (IDLTI) model, **sys1** does not include the estimated parameter covariance of **sys**. If you want to translate the covariance while converting the model, use translatecov.

See Also

c2d | d2c | d2dOptions | upsample | translatecov

d2dOptions

Create option set for discrete-time resampling

Syntax

```
opts = d2dOptions
opts = d2dOptions('OptionName', OptionValue)
```

Description

opts = d2dOptions returns the default options for d2d.

opts = d2dOptions('OptionName', OptionValue) accepts one or more commaseparated name/value pairs that specify options for the d2d command. Specify OptionName inside single quotes.

This table summarizes the options that the d2d command supports.

Input Arguments

Name-Value Pair Arguments

'Method'

Discretization method, specified as one of the following values:

'zoh'	Zero-order hold, where $d2d$ assumes the control inputs are piecewise constant over the sample time Ts.
'tustin'	Bilinear (Tustin) approximation. By default, d2d resamples with no prewarp. To include prewarp, use the PrewarpFrequency option.

Default: 'zoh'

'PrewarpFrequency'

Prewarp frequency for 'tustin' method, specified in rad/TimeUnit, where TimeUnit is the time units, specified in the TimeUnit property, of the resampled system. Takes positive scalar values. The prewarp frequency must be smaller than the Nyquist frequency before and after resampling. A value of 0 corresponds to the standard 'tustin' method without prewarp.

Default: 0

Examples

Resample a discrete-time model using the 'tustin' method with frequency prewarping.

Create the discrete-time transfer function

$$\frac{z+1}{z^2+z+1}$$

h1 = tf([1 1], [1 1 1], 0.1); % 0.1s sample time
To resample to a different sample time, use d2dOptions to create the option set.
opts = d2dOptions('Method', 'tustin', 'PrewarpFrequency', 20);
h2 = d2d(h1, 0.05, opts);

You can use opts to resample additional models using the same options.

See Also

d2d

Introduced in R2010a

damp

Natural frequency and damping ratio

Syntax

damp(sys)
[Wn,zeta] = damp(sys)
[Wn,zeta,P] = damp(sys)

Description

damp(sys) displays a table of the damping ratio (also called *damping factor*), natural frequency, and time constant of the poles of the linear model sys. For a discrete-time model, the table also includes the magnitude of each pole. Frequencies are expressed in units of the reciprocal of the TimeUnit property of sys. Time constants are expressed in the same units as the TimeUnit property of sys.

[Wn,zeta] = damp(sys) returns the natural frequencies, Wn, and damping ratios,zeta, of the poles of sys.

[Wn,zeta,P] = damp(sys) returns the poles of sys.

Input Arguments

sys

Any linear dynamic system model.

Output Arguments

Wn

Vector containing the natural frequencies of each pole of **sys**, in order of increasing frequency. Frequencies are expressed in units of the reciprocal of the **TimeUnit** property of **sys**.

If sys is a discrete-time model with specified sample time, Wn contains the natural frequencies of the equivalent continuous-time poles (see "Algorithms" on page 1-148). If sys has an unspecified sample time (Ts = -1), then the software uses Ts = 1 and calculates Wn accordingly.

zeta

Vector containing the damping ratios of each pole of sys, in the same order as Wn.

If sys is a discrete-time model with specified sample time, zeta contains the damping ratios of the equivalent continuous-time poles (see "Algorithms" on page 1-148). If sys has an unspecified sample time (Ts = -1), then the software uses Ts = 1 and calculates zeta accordingly.

Ρ

Vector containing the poles of sys, in order of increasing natural frequency. P is the same as the output of pole(sys), except for the order.

Examples

Natural Frequency, Damping Ratio, and Poles of Continuous-Time System

Calculate the natural frequency, damping ratio, time constant, and poles of the continuous-time transfer function:

$$H(s) = \frac{2s^2 + 5s + 1}{s^2 + 2s + 3}.$$

H = tf([2 5 1], [1 2 3]);

Display the natural frequencies, damping ratios, time constants, and poles of H.

damp(H)

Pole	Damping	Frequency (rad/seconds)	Time Constant (seconds)
-1.00e+00 + 1.41e+00i	5.77e-01	1.73e+00	1.00e+00
-1.00e+00 - 1.41e+00i	5.77e-01	1.73e+00	1.00e+00

Obtain vectors containing the natural frequencies and damping ratios of the poles.

[Wn,zeta] = damp(H);

Calculate the associated time constants.

tau = 1./(zeta.*Wn);

Natural Frequency, Damping Ratio, and Poles of Discrete-Time System

Calculate the natural frequency, damping ratio, time constant, and poles of a discretetime transfer function.

H = tf([5 3 1], [1 6 4 4], 0.01);

Display information about the poles of H.

damp(H)

Pole	Magnitude	Damping	Frequency (rad/seconds)	Time Constant (seconds)
-3.02e-01 + 8.06e-01i	8.61e-01	7.74e-02	1.93e+02	6.68e-02
-3.02e-01 - 8.06e-01i	8.61e-01	7.74e-02	1.93e+02	6.68e-02
-5.40e+00	5.40e+00	-4.73e-01	3.57e+02	-5.93e-03

The Magnitude column displays the discrete-time pole magnitudes. The Damping, Frequency, and Time Constant columns display values calculated using the equivalent continuous-time poles.

Obtain vectors containing the natural frequencies and damping ratios of the poles.

[Wn,zeta] = damp(H);

Calculate the associated time constants.

tau = 1./(zeta.*Wn);

More About

Algorithms

The natural frequency, time constant, and damping ratio of the system poles are defined in the following table:

	Continuous Time	Discrete Time with Sample Time Ts
Pole Location	8	z
Equivalent Continuous- Time Pole	Not applicable	$s = \frac{ln(z)}{T_s}$
Natural Frequency	$\omega_n = s $	$\omega_n = s = \left \frac{ln(z)}{T_s} \right $
Damping Ratio	$\zeta = -cos(\angle s)$	$\zeta = -\cos(\angle s) = -\cos(\angle ln)$
Time Constant	$ au = rac{1}{\omega_n \zeta}$	$\tau = \frac{1}{\omega_n \zeta}$

See Also

eig | esort | dsort | pole | pzmap | zero

dare

Solve discrete-time algebraic Riccati equations (DAREs)

Syntax

```
[X,L,G] = dare(A,B,Q,R)
[X,L,G] = dare(A,B,Q,R,S,E)
[X,L,G,report] = dare(A,B,Q,...)
[X1,X2,L,report] = dare(A,B,Q,..., 'factor')
```

Description

[X,L,G] = dare(A,B,Q,R) computes the unique stabilizing solution X of the discrete-time algebraic Riccati equation

 $A^T X A - X - A^T X B (B^T X B + R)^{-1} B^T X A + Q = 0$

The dare function also returns the gain matrix, $G = (B^T XB + R)^{-1}B^T XA$, and the vector L of closed loop eigenvalues, where

L=eig(A-B*G,E)

[X,L,G] = dare(A,B,Q,R,S,E) solves the more general discrete-time algebraic Riccati equation,

$$A^T X A - E^T X E - (A^T X B + S)(B^T X B + R)^{-1}(B^T X A + S^T) + Q = 0$$

or, equivalently, if R is nonsingular,

$$\boldsymbol{E}^{T}\boldsymbol{X}\boldsymbol{E} = \boldsymbol{F}^{T}\boldsymbol{X}\boldsymbol{F} - \boldsymbol{F}^{T}\boldsymbol{X}\boldsymbol{B}(\boldsymbol{B}^{T}\boldsymbol{X}\boldsymbol{B} + \boldsymbol{R})^{-1}\boldsymbol{B}^{T}\boldsymbol{X}\boldsymbol{F} + \boldsymbol{Q} - \boldsymbol{S}\boldsymbol{R}^{-1}\boldsymbol{S}^{T}$$

where $F = A - BR^{-1}S^T$. When omitted, R, S, and E are set to the default values R=I, S=0, and E=I.

The dare function returns the corresponding gain matrix

 $G = (B^T X B + R)^{-1} (B^T X A + S^T)$

and a vector ${\sf L}$ of closed-loop eigenvalues, where

L= eig(A-B*G,E)

- [X,L,G,report] = dare(A,B,Q,...) returns a diagnosis report with value:
- $\boldsymbol{1}$ when the associated symplectic pencil has eigenvalues on or very near the unit circle
- · -2 when there is no finite stabilizing solution X
- The Frobenius norm if X exists and is finite

[X1, X2, L, report] = dare(A, B, Q, ..., 'factor') returns two matrices, X1 and X2, and a diagonal scaling matrix D such that $X = D^*(X2/X1)^*D$. The vector L contains the closed-loop eigenvalues. All outputs are empty when the associated Symplectic matrix has eigenvalues on the unit circle.

Limitations

The (A, B) pair must be stabilizable (that is, all eigenvalues of A outside the unit disk must be controllable). In addition, the associated symplectic pencil must have no eigenvalue on the unit circle. Sufficient conditions for this to hold are (Q, A) detectable when S = 0 and R > 0, or

$$\begin{bmatrix} Q & S \\ S^T & R \end{bmatrix} > 0$$

More About

Algorithms

dare implements the algorithms described in [1]. It uses the QZ algorithm to deflate the extended symplectic pencil and compute its stable invariant subspace.

References

[1] Arnold, W.F., III and A.J. Laub, "Generalized Eigenproblem Algorithms and Software for Algebraic Riccati Equations," *Proc. IEEE*, 72 (1984), pp. 1746-1754.

See Also

care | dlyap | gdare

db2mag

Convert decibels (dB) to magnitude

Syntax

y = db2mag(ydb)

Description

y = db2mag(ydb) returns the corresponding magnitude y for a given decibel (dB) value ydb. The relationship between magnitude and decibels is $ydb = 20 * \log_{10}(y)$.

See Also

mag2db

Introduced in R2008a

dcgain

Low-frequency (DC) gain of LTI system

Syntax

k = dcgain(sys)

Description

k = dcgain(sys) computes the DC gain k of the LTI model sys.

Continuous Time

The continuous-time DC gain is the transfer function value at the frequency s = 0. For state-space models with matrices (A, B, C, D), this value is $K = D - CA^{-1}B$

Discrete Time

The discrete-time DC gain is the transfer function value at z = 1. For state-space models with matrices (A, B, C, D), this value is $K = D + C (I - A)^{-1}B$

Examples

Example 1

To compute the DC gain of the MIMO transfer function

$$H(s) = \begin{bmatrix} 1 & \frac{s-1}{s^2 + s + 3} \\ \frac{1}{s+1} & \frac{s+2}{s-3} \end{bmatrix}$$

type
H = [1 tf([1 -1],[1 1 3]) ; tf(1,[1 1]) tf([1 2],[1 -3])];
dcgain(H)
to get the result:
ans =
 1.0000 -0.3333
 1.0000 -0.6667

Example 2

To compute the DC gain of an identified process model, type;

```
load iddata1
sys = idproc('p1d');
syse = procest(z1, sys)
```

```
dcgain(syse)
```

The DC gain is stored same as ${\tt syse.Kp}.$

More About

Tips

The DC gain is infinite for systems with integrators.

See Also norm | evalfr

delay2z

Replace delays of discrete-time TF, SS, or ZPK models by poles at z=0, or replace delays of FRD models by phase shift

Note: delay2z has been removed. Use absorbDelay instead.

delayss

Create state-space models with delayed inputs, outputs, and states

Syntax

```
sys=delayss(A,B,C,D,delayterms)
sys=delayss(A,B,C,D,ts,delayterms)
```

Description

sys=delayss(A,B,C,D,delayterms)constructs a continuous-time state-space model
of the form:

$$\frac{dx}{dt} = Ax(t) + Bu(t) + \sum_{j=1}^{N} (A_j x(t-t_j) + B_j u(t-t_j))$$
$$y(t) = Cx(t) + Du(t) + \sum_{j=1}^{N} (C_j x(t-t_j) + D_j u(t-t_j))$$

where t_j , j=1,..,N are time delays expressed in seconds. delayterms is a struct array with fields delay, a, b, c, d where the fields of delayterms(j) contain the values of tj, Aj, Bj, Cj, and Dj, respectively. The resulting model sys is a state-space (SS) model with internal delays.

sys=delayss(A,B,C,D,ts,delayterms)constructs the discrete-time counterpart:

$$x[k+1] = Ax[k] + Bu[k] + \sum_{j=1}^{N} \{A_{j}x[k-n_{j}] + B_{j}u[k-n_{j}]\}$$
$$y[k] = Cx[k] + Du[k] + \sum_{j=1}^{N} \{C_{j}x[k-n_{j}] + D_{j}u[k-n_{j}]\}$$

where Nj, j=1,..,N are time delays expressed as integer multiples of the sample time ts.

Examples

To create the model:

 $\frac{dx}{dt} = x(t) - x(t - 1.2) + 2u(t - 0.5)$ y(t) = x(t - 0.5) + u(t)

type

```
DelayT(1) = struct('delay',0.5,'a',0,'b',2,'c',1,'d',0);
DelayT(2) = struct('delay',1.2,'a',-1,'b',0,'c',0,'d',0);
sys = delayss(1,0,0,1,DelayT)
a =
       x1
        0
   x1
b =
       u1
        2
   x1
c =
       х1
   y1
       1
d =
       u1
   y1
       1
(values computed with all internal delays set to zero)
Internal delays: 0.5 0.5 1.2
Continuous-time model.
```

See Also

getdelaymodel | ss

Introduced in R2007a

dlqr

Linear-quadratic (LQ) state-feedback regulator for discrete-time state-space system

Syntax

[K,S,e] = dlqr(A,B,Q,R,N)

Description

[K,S,e] = dlqr(A,B,Q,R,N) calculates the optimal gain matrix K such that the state-feedback law

$$u[n] = -Kx[n]$$

minimizes the quadratic cost function

$$J(u) = \sum_{n=1}^{\infty} (x[n]^T Qx[n] + u[n]^T Ru[n] + 2x[n]^T Nu[n])$$

for the discrete-time state-space mode

$$x[n+1] = Ax[n] + Bu[n]$$

The default value N=0 is assumed when N is omitted.

In addition to the state-feedback gain K, dlqr returns the infinite horizon solution S of the associated discrete-time Riccati equation

$$A^{T}SA - S - (A^{T}SB + N)(B^{T}SB + R)^{-1}(B^{T}SA + N^{T}) + Q = 0$$

and the closed-loop eigenvalues e = eig(A-B*K). Note that K is derived from S by

$$K = (B^T S B + R)^{-1} (B^T S A + N^T)$$

Limitations

The problem data must satisfy:

- The pair (A, B) is stabilizable.
- R > 0 and $Q NR^{-1}N^T \ge 0$
- $(Q NR^{-1}N^T, A BR^{-1}N^T)$ has no unobservable mode on the unit circle.

See Also

dare | lqgreg | lqr | lqrd | lqry

dlyap

Solve discrete-time Lyapunov equations

Syntax

X = dlyap(A,Q) X = dlyap(A,B,C) X = dlyap(A,Q,[],E)

Description

X = dlyap(A,Q) solves the discrete-time Lyapunov equation $AXA^{T} - X + Q = 0$,

where A and Q are n-by-n matrices.

The solution X is symmetric when Q is symmetric, and positive definite when Q is positive definite and A has all its eigenvalues inside the unit disk.

X = dlyap(A,B,C) solves the Sylvester equation AXB - X + C = 0,

where A, B, and C must have compatible dimensions but need not be square.

X = dlyap(A,Q,[],E) solves the generalized discrete-time Lyapunov equation $AXA^{T} - EXE^{T} + Q = 0$,

where Q is a symmetric matrix. The empty square brackets, [], are mandatory. If you place any values inside them, the function will error out.

Diagnostics

The discrete-time Lyapunov equation has a (unique) solution if the eigenvalues $a_1, a_2, ..., a_N$ of A satisfy $a_i a_j \neq 1$ for all (i, j).

If this condition is violated, dlyap produces the error message

Solution does not exist or is not unique.

More About

Algorithms

dlyap uses SLICOT routines SB03MD and SG03AD for Lyapunov equations and SB04QD (SLICOT) for Sylvester equations.

References

- [1] Barraud, A.Y., "A numerical algorithm to solve A XA X = Q," *IEEE Trans. Auto. Contr.*, AC-22, pp. 883-885, 1977.
- [2] Bartels, R.H. and G.W. Stewart, "Solution of the Matrix Equation AX + XB = C," Comm. of the ACM, Vol. 15, No. 9, 1972.
- [3] Hammarling, S.J., "Numerical solution of the stable, non-negative definite Lyapunov equation," *IMA J. Num. Anal.*, Vol. 2, pp. 303-325, 1982.
- [4] Higham, N.J., "FORTRAN codes for estimating the one-norm of a real or complex matrix, with applications to condition estimation," A.C.M. Trans. Math. Soft., Vol. 14, No. 4, pp. 381-396, 1988.
- [5] Penzl, T., "Numerical solution of generalized Lyapunov equations," Advances in Comp. Math., Vol. 8, pp. 33-48, 1998.
- [6] Golub, G.H., Nash, S. and Van Loan, C.F. "A Hessenberg-Schur method for the problem AX + XB = C," *IEEE Trans. Auto. Contr.*, AC-24, pp. 909-913, 1979.
- [7] Sima, V. C, "Algorithms for Linear-quadratic Optimization," Marcel Dekker, Inc., New York, 1996.

See Also

covar | lyap

dlyapchol

Square-root solver for discrete-time Lyapunov equations

Syntax

R = dlyapchol(A,B) X = dlyapchol(A,B,E)

Description

R = dlyapchol(A,B) computes a Cholesky factorization X = R' * R of the solution X to the Lyapunov matrix equation:

A * X * A' - X + B * B' = 0

All eigenvalues of A matrix must lie in the open unit disk for R to exist.

X = dlyapchol(A,B,E) computes a Cholesky factorization X = R'*R of X solving the Sylvester equation

A*X*A' - E*X*E' + B*B' = 0

All generalized eigenvalues of (A,E) must lie in the open unit disk for R to exist.

More About

Algorithms

dlyapchol uses SLICOT routines SB03OD and SG03BD.

References

[1] Bartels, R.H. and G.W. Stewart, "Solution of the Matrix Equation AX + XB = C," Comm. of the ACM, Vol. 15, No. 9, 1972.

- [2] Hammarling, S.J., "Numerical solution of the stable, non-negative definite Lyapunov equation," *IMA J. Num. Anal.*, Vol. 2, pp. 303-325, 1982.
- [3] Penzl, T., "Numerical solution of generalized Lyapunov equations," Advances in Comp. Math., Vol. 8, pp. 33-48, 1998.

See Also

dlyap | lyapchol

drss

Generate random discrete test model

Syntax

```
sys = drss(n)
drss(n,p)
drss(n,p,m)
drss(n,p,m,s1,...sn)
```

Description

sys = drss(n) generates an *n*-th order model with one input and one output, and returns the model in the state-space object sys. The poles of sys are random and stable with the possible exception of poles at z = 1 (integrators).

drss(n,p) generates an *n*-th order model with one input and p outputs.

drss(n,p,m) generates an *n*-th order model with p outputs and m inputs.

drss(n,p,m,s1,...sn) generates a *s1*-by-*sn* array of *n*-th order models with m inputs and p outputs.

In all cases, the discrete-time state-space model or array returned by drss has an unspecified sample time. To generate transfer function or zero-pole-gain systems, convert sys using tf or zpk.

Examples

Generate a discrete LTI system with three states, four outputs, and two inputs.

x2 x3	0.1102 -0.7222	0.9115 0.1628	0.1628 -0.202
b =			
	u1	u2	
x1	-0.4326	0.2877	
x2	- 0	- 0	
х3	0	1.191	
с =			
	x1	x2	x3
y1	1.189	-0.1867	- 0
ý2	-0.03763	0.7258	0.1139
ý3	0.3273	-0.5883	1.067
y4	0.1746	2.183	0
d =			
	u1	u2	
y1	-0.09565	0	
ý2	-0.8323	1.624	
ý3	0.2944	-0.6918	
y4	- 0	0.858	
Samplo	timo: uno	posified	

Sample time: unspecified Discrete-time model.

See Also

rss | tf | zpk

dsort

Sort discrete-time poles by magnitude

Syntax

dsort
[s,ndx] = dsort(p)

Description

 ${\tt dsort}$ ${\tt sorts}$ the discrete-time poles contained in the vector p in descending order by magnitude. Unstable poles appear first.

When called with one lefthand argument, dsort returns the sorted poles in s.

```
[s,ndx] = dsort(p) also returns the vector ndx containing the indices used in the sort.
```

Examples

Sort the following discrete poles.

```
p =
  -0.2410 + 0.5573i
  -0.2410 - 0.5573i
  0.1503
  -0.0972
  -0.2590
s = dsort(p)
s =
  -0.2410 + 0.5573i
  -0.2410 - 0.5573i
  -0.2590
   0.1503
  -0.0972
```

Limitations

The poles in the vector \boldsymbol{p} must appear in complex conjugate pairs.

See Also

eig | esort | sort | pole | pzmap | zero

dss

Create descriptor state-space models

Syntax

sys = dss(A,B,C,D,E)
sys = dss(A,B,C,D,E,Ts)
sys = dss(A,B,C,D,E,ltisys)

Description

sys = dss(A,B,C,D,E) creates the continuous-time descriptor state-space model

$$E\frac{dx}{dt} = Ax + Bu$$
$$y = Cx + Du$$

The output sys is an SS model storing the model data (see "State-Space Models"). Note that ss produces the same type of object. If the matrix D = 0, you can simply set d to the scalar 0 (zero).

sys = dss(A,B,C,D,E,Ts) creates the discrete-time descriptor model

$$Ex[n+1] = Ax[n] + Bu[n]$$
$$y[n] = Cx[n] + Du[n]$$

with sample time Ts (in seconds).

sys = dss(A,B,C,D,E,ltisys) creates a descriptor model with properties inherited
from the LTI model ltisys (including the sample time).

Any of the previous syntaxes can be followed by property name/property value pairs

'Property',Value

Each pair specifies a particular LTI property of the model, for example, the input names or some notes on the model history. See **set** and the example below for details.

Examples

The command

creates the model

 $5\dot{x} = x + 2u$ y = 3x + 4u

with a 0.1 second input delay. The input is labeled 'voltage', and a note is attached to tell you that this is just an example.

See Also dssdata | get | set | ss

dssdata

Extract descriptor state-space data

Syntax

```
[A,B,C,D,E] = dssdata(sys)
[A,B,C,D,E,Ts] = dssdata(sys)
```

Description

[A,B,C,D,E] = dssdata(sys) returns the values of the A, B, C, D, and E matrices for the descriptor state-space model sys (see dss). dssdata equals ssdata for regular state-space models (i.e., when E=I).

If sys has internal delays, A, B, C, D are obtained by first setting all internal delays to zero (creating a zero-order Padé approximation). For some systems, setting delays to zero creates singular algebraic loops, which result in either improper or ill-defined, zero-delay approximations. For these systems, dssdata cannot display the matrices and returns an error. This error does not imply a problem with the model sys itself.

[A,B,C,D,E,Ts] = dssdata(sys) also returns the sample time Ts.

You can access other properties of **sys** using **get** or direct structure-like referencing (e.g., **sys.Ts**).

For arrays of SS models with variable order, use the syntax

[A,B,C,D,E] = dssdata(sys,'cell')

to extract the state-space matrices of each model as separate cells in the cell arrays A, B, C, D, and E.

See Also

dss | get | getdelaymodel | ssdata

esort

Sort continuous-time poles by real part

Syntax

s = esort(p)
[s,ndx] = esort(p)

Description

esort sorts the continuous-time poles contained in the vector p by real part. Unstable eigenvalues appear first and the remaining poles are ordered by decreasing real parts.

When called with one left-hand argument, s = esort(p) returns the sorted eigenvalues in s.

[s,ndx] = esort(p) returns the additional argument ndx, a vector containing the indices used in the sort.

Examples

Sort the following continuous eigenvalues.

```
p =
  -0.2410+ 0.5573i
  -0.2410- 0.5573i
   0.1503
  -0.0972
  -0.2590
esort(p)
ans =
   0.1503
  -0.0972
  -0.2410+ 0.5573i
```

esort

-0.2410- 0.5573i -0.2590

Limitations

The eigenvalues in the vector \boldsymbol{p} must appear in complex conjugate pairs.

See Also

dsort | sort | eig | pole | pzmap | zero

estim

Form state estimator given estimator gain

Syntax

```
est = estim(sys,L)
est = estim(sys,L,sensors,known)
```

Description

est = estim(sys,L) produces a state/output estimator est given the plant statespace model sys and the estimator gain L. All inputs w of sys are assumed stochastic (process and/or measurement noise), and all outputs y are measured. The estimator estis returned in state-space form (SS object).

For a continuous-time plant sys with equations

$$\dot{x} = Ax + Bw$$
$$y = Cx + Dw$$

estim uses the following equations to generate a plant output estimate \hat{y} and a state estimate \hat{x} , which are estimates of y(t)=C and x(t), respectively:

$$\dot{\hat{x}} = A\hat{x} + L(y - C\hat{x})$$
$$\begin{bmatrix} \hat{y} \\ \hat{x} \end{bmatrix} = \begin{bmatrix} C \\ I \end{bmatrix} \hat{x}$$

For a discrete-time plant **sys** with the following equations:

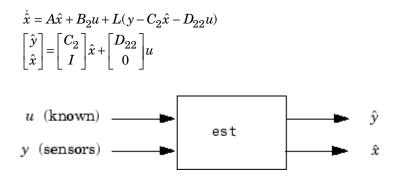
$$x[n+1] = Ax[n] + Bw[n]$$
$$y[n] = Cx[n] + Dw[n]$$

estim uses estimator equations similar to those for continuous-time to generate a plant output estimate y[n | n-1] and a state estimate x[n | n-1], which are estimates of y[n] and x[n], respectively. These estimates are based on past measurements up to y[n-1].

est = estim(sys,L,sensors,known) handles more general plants sys with both known (deterministic) inputs u and stochastic inputs w, and both measured outputs y and nonmeasured outputs z.

$$\dot{x} = Ax + B_1 w + B_2 u$$
$$\begin{bmatrix} z \\ y \end{bmatrix} = \begin{bmatrix} C_1 \\ C_2 \end{bmatrix} x + \begin{bmatrix} D_{11} \\ D_{21} \end{bmatrix} w + \begin{bmatrix} D_{12} \\ D_{22} \end{bmatrix} u$$

The index vectors sensors and known specify which outputs of sys are measured (y), and which inputs of sys are known (u). The resulting estimator est, found using the following equations, uses both u and y to produce the output and state estimates.



Examples

Consider a state-space model sys with seven outputs and four inputs. Suppose you designed a Kalman gain matrix L using outputs 4, 7, and 1 of the plant as sensor measurements and inputs 1, 4, and 3 of the plant as known (deterministic) inputs. You can then form the Kalman estimator by

```
sensors = [4,7,1];
known = [1,4,3];
est = estim(sys,L,sensors,known)
```

See the function kalman for direct Kalman estimator design.

More About

Tips

You can use the functions place (pole placement) or kalman (Kalman filtering) to design an adequate estimator gain L. Note that the estimator poles (eigenvalues of A-LC) should be faster than the plant dynamics (eigenvalues of A) to ensure accurate estimation.

See Also

```
kalman | ss | ssest | predict | place | reg | kalmd | lqgreg
```

Introduced before R2006a

evalfr

Evaluate frequency response at given frequency

Syntax

frsp = evalfr(sys,f)

Description

frsp = evalfr(sys,f) evaluates the transfer function of the TF, SS, or ZPK model sys at the complex number f. For state-space models with data (A, B, C, D), the result is $H(f) = D + C (fI - A)^{-1}B$

evalfr is a simplified version of freqresp meant for quick evaluation of the response at a single point. Use freqresp to compute the frequency response over a set of frequencies.

Examples

Example 1

To evaluate the discrete-time transfer function

$$H(z) = \frac{z-1}{z^2+z+1}$$

at z = 1 + j, type

to get the result:

ans =

2.3077e-01 + 1.5385e-01i

Example 2

To evaluate the frequency response of a continuous-time IDTF model at frequency W = 0.1 rad/s, type:

sys = idtf(1,[1 2 1]); w = 0.1; s = 1j*w; evalfr(sys, s)

The result is same as freqresp(sys, w).

Limitations

The response is not finite when f is a pole of sys.

See Also freqresp | bode | sigma

Introduced before R2006a

lti/exp

Create pure continuous-time delays

Syntax

d = exp(tau,s)

Description

d = exp(tau, s) creates pure continuous-time delays. The transfer function of a pure delay tau is:

d(s) = exp(-tau*s)

You can specify this transfer function using exp.

s = zpk('s') d = exp(-tau*s)

More generally, given a 2D array M,

s = zpk('s') D = exp(-M*s)

creates an array D of pure delays where $D(i,j) = \exp(-M(i,j)s)$.

All entries of ${\tt M}$ should be non negative for causality.

See Also

zpk | tf

Introduced in R2006a

fcat

Concatenate FRD models along frequency dimension

Syntax

```
sys = fcat(sys1,sys2,...)
```

Description

sys = fcat(sys1,sys2,...) takes two or more frd models and merges their frequency responses into a single frd model sys. The resulting frequency vector is sorted by increasing frequency. The frequency vectors of sys1, sys2,... should not intersect. If the frequency vectors do intersect, use fdel to remove intersecting data from one or more of the models.

See Also

fselect | interp | fdel | frd

Introduced in R2006a

fdel

Delete specified data from frequency response data (FRD) models

Syntax

sysout = fdel(sys, freq)

Description

sysout = fdel(sys, freq) removes from the frd model sys the data nearest to the frequency values specified in the vector freq.

Input Arguments

sys

frd model.

freq

Vector of frequency values.

Output Arguments

sysout

frd model containing the data remaining in sys after removing the frequency points closest to the entries of freq.

Examples

Remove selected data from a frd model. In this example, first obtain an frd model:

sys = frd(tf([1],[1 1]), logspace(0,1,10))

Frequency(rad/s)	Response
1.0000	0.5000 - 0.5000i
1.2915	0.3748 - 0.4841i
1.6681	0.2644 - 0.4410i
2.1544	0.1773 - 0.3819i
2.7826	0.1144 - 0.3183i
3.5938	0.0719 - 0.2583i
4.6416	0.0444 - 0.2059i
5.9948	0.0271 - 0.1623i
7.7426	0.0164 - 0.1270i
10.0000	0.0099 - 0.0990i

Continuous-time frequency response.

The following commands remove the data nearest 2, 3.5, and 6 rad/s from sys.

freq = [2, 3.5, 6]; sysout = fdel(sys,	
Frequency(rad/s)	Response
1.0000	0.5000 - 0.5000i
1.2915	0.3748 - 0.4841i
1.6681	0.2644 - 0.4410i
2.7826	0.1144 - 0.3183i
4.6416	0.0444 - 0.2059i
7.7426	0.0164 - 0.1270i
10.0000	0.0099 - 0.0990i

Continuous-time frequency response.

You do not have to specify the exact frequency of the data to remove. fdel removes the data nearest to the specified frequencies.

More About

Tips

• Use fdel to remove unwanted data (for example, outlier points) at specified frequencies.

- Use fdel to remove data at intersecting frequencies from frd models before merging them with fcat. fcat produces an error when you attempt to merge frd models that have intersecting frequency data.
- To remove data from an frd model within a range of frequencies, use fselect.

See Also

fcat | fselect | frd

Introduced in R2010a

feedback

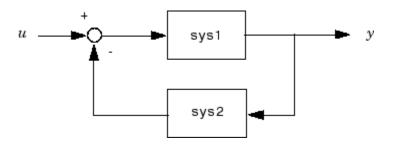
Feedback connection of two models

Syntax

```
sys = feedback(sys1,sys2)
```

Description

sys = feedback(sys1,sys2) returns a model object sys for the negative feedback
interconnection of model objects sys1 and sys2.



The closed-loop model sys has u as input vector and y as output vector. The models sys1 and sys2 must be both continuous or both discrete with identical sample times. Precedence rules are used to determine the resulting model type (see "Rules That Determine Model Type").

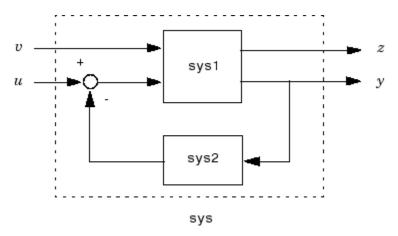
To apply positive feedback, use the syntax

```
sys = feedback(sys1,sys2,+1)
```

By default, feedback(sys1,sys2) assumes negative feedback and is equivalent to feedback(sys1,sys2,-1).

Finally,

sys = feedback(sys1,sys2,feedin,feedout)



computes a closed-loop model sys for the more general feedback loop.

The vector feedin contains indices into the input vector of sys1 and specifies which inputs u are involved in the feedback loop. Similarly, feedout specifies which outputs yof sys1 are used for feedback. The resulting model sys has the same inputs and outputs as sys1 (with their order preserved). As before, negative feedback is applied by default and you must use

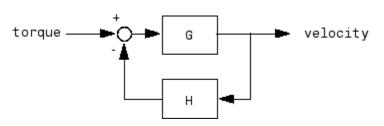
```
sys = feedback(sys1,sys2,feedin,feedout,+1)
```

to apply positive feedback.

For more complicated feedback structures, use append and connect.

Examples

Example 1



To connect the plant

$$G(s) = \frac{2s^2 + 5s + 1}{s^2 + 2s + 3}$$

with the controller

$$H(s) = \frac{5(s+2)}{s+10}$$

using negative feedback, type

G = tf([2 5 1],[1 2 3],'inputname','torque',... 'outputname','velocity'); H = zpk(-2,-10,5) Cloop = feedback(G,H)

These commands produce the following result.

Zero/pole/gain from input "torque" to output "velocity": 0.18182 (s+10) (s+2.281) (s+0.2192) (s+3.419) (s^2 + 1.763s + 1.064)

The result is a zero-pole-gain model as expected from the precedence rules. Note that Cloop inherited the input and output names from G.

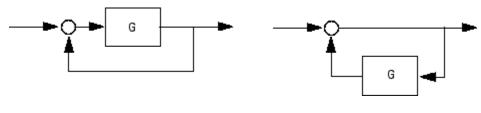
Example 2

Consider a state-space plant P with five inputs and four outputs and a state-space feedback controller K with three inputs and two outputs. To connect outputs 1, 3, and 4 of the plant to the controller inputs, and the controller outputs to inputs 4 and 2 of the plant, use

```
feedin = [4 2];
feedout = [1 3 4];
Cloop = feedback(P,K,feedin,feedout)
```

Example 3

You can form the following negative-feedback loops



by

Cloop = feedback(G,1) % left diagram Cloop = feedback(1,G) % right diagram

Limitations

The feedback connection should be free of algebraic loop. If D_1 and D_2 are the feedthrough matrices of **sys1** and **sys2**, this condition is equivalent to:

- $I + D_1 D_2$ nonsingular when using negative feedback
- $I D_1 D_2$ nonsingular when using positive feedback.

See Also series | parallel | connect

Introduced before R2006a

filt

Specify discrete transfer functions in DSP format

Syntax

sys = filt(num,den)
sys = filt(num,den,Ts)
sys = filt(M)

Description

In digital signal processing (DSP), it is customary to write transfer functions as rational expressions in z^{-1} and to order the numerator and denominator terms in *ascending* powers of z^{-1} . For example:

$$H\left(z^{-1}\right) = \frac{2 + z^{-1}}{1 + 0.4z^{-1} + 2z^{-2}}$$

The function filt is provided to facilitate the specification of transfer functions in DSP format.

sys = filt(num,den) creates a discrete-time transfer function sys with
numerator(s) num and denominator(s) den. The sample time is left unspecified (sys.Ts
= -1) and the output sys is a TF object.

sys = filt(num,den,Ts) further specifies the sample time Ts (in seconds).

sys = filt(M) specifies a static filter with gain matrix M.

Any of the previous syntaxes can be followed by property name/property value pairs of the form

'Property',Value

Each pair specifies a particular property of the model, for example, the input names or the transfer function variable. For information about the available properties and their values, see the tf reference page.

Arguments

For SISO transfer functions, num and den are row vectors containing the numerator and denominator coefficients ordered in ascending powers of z^{-1} . For example, den = [1 0.4 2] represents the polynomial $1 + 0.4z^{-1} + 2z^{-2}$.

MIMO transfer functions are regarded as arrays of SISO transfer functions (one per I/ O channel), each of which is characterized by its numerator and denominator. The input arguments num and den are then cell arrays of row vectors such that:

- num and den have as many rows as outputs and as many columns as inputs.
- Their (*i*, *j*) entries num{i,j} and den{i,j} specify the numerator and denominator of the transfer function from input j to output i.

If all SISO entries have the same denominator, you can also set **den** to the row vector representation of this common denominator.

Examples

Create a two-input digital filter with input names 'Channel1' and 'Channel2':

```
num = {1 , [1 0.3]};
den = {[1 1 2] ,[5 2]};
H = filt(num,den,'inputname',{'channel1' 'channel2'})
```

This syntax returns:

```
Transfer function from input "channel1" to output:

1

1 + z^{-1} + 2 z^{-2}

Transfer function from input "channel2" to output:

1 + 0.3 z^{-1}
```

5 + 2 z^-1

Sample time: unspecified

More About

Tips

filt behaves as tf with the Variable property set to $^\prime z^{\,\text{--}1\,^\prime}.$ See tf entry below for details.

See Also

tf | zpk | ss

Introduced before R2006a

fnorm

Pointwise peak gain of FRD model

Syntax

```
fnrm = fnorm(sys)
fnrm = fnorm(sys,ntype)
```

Description

fnrm = fnorm(sys) computes the pointwise 2-norm of the frequency response contained in the FRD model sys, that is, the peak gain at each frequency point. The output fnrm is an FRD object containing the peak gain across frequencies.

fnrm = fnorm(sys,ntype) computes the frequency response gains using the matrix
norm specified by ntype. See norm for valid matrix norms and corresponding NTYPE
values.

See Also

norm | abs

Introduced in R2006a

frd

Create frequency-response data model, convert to frequency-response data model

Syntax

```
sys = frd(response,frequency)
sys = frd(response,frequency,Ts)
sys = frd
sysfrd = frd(sys,frequency)
sysfrd = frd(sys,frequency,units)
```

Description

sys = frd(response, frequency) creates a frequency-response data (frd) model object sys from the frequency response data stored in the multidimensional array response. The vector frequency represents the underlying frequencies for the frequency response data. See Data Format for the Argument Response in FRD Models for a list of response data formats.

sys = frd(response, frequency, Ts) creates a discrete-time frd model object sys with scalar sample time Ts. Set Ts = -1 to create a discrete-time frd model object without specifying the sample time.

sys = frd creates an empty frd model object.

The input argument list for any of these syntaxes can be followed by property name/ property value pairs of the form

'PropertyName',PropertyValue

You can use these extra arguments to set the various properties the model. For more information about available properties of frd models, see "Properties" on page 1-193.

To force an FRD model **sys** to inherit all of its generic LTI properties from any existing LTI model **refsys**, use the syntax

sys = frd(response,frequency,ltisys)

sysfrd = frd(sys,frequency) converts a dynamic system model sys to frequency response data form. The frequency response is computed at the frequencies provided by the vector frequency, in rad/TimeUnit, where TimeUnit is the time units of the input dynamic system, specified in the TimeUnit property of sys.

sysfrd = frd(sys,frequency,units) converts a dynamic system model to an frd model and interprets frequencies in the frequency vector to have the units specified by the string units. For a list of values for the string units, see the FrequencyUnit property in "Properties" on page 1-193.

Arguments

When you specify a SISO or MIMO FRD model, or an array of FRD models, the input argument frequency is always a vector of length Nf, where Nf is the number of frequency data points in the FRD. The specification of the input argument response is summarized in the following table.

Model Form	Response Data Format
SISO model	Vector of length Nf for which response(i) is the frequency response at the frequency frequency(i)
MIMO model with Ny outputs and Nu inputs	Ny-by-Nu-by-Nf multidimensional array for which response(i,j,k) specifies the frequency response from input j to output i at frequency frequency(k)
S1-byby-Sn array of models with Ny outputs and Nu inputs	Multidimensional array of size [Ny Nu S1 Sn] for which response(i,j,k,:) specifies the array of frequency response data from input j to output i at frequency frequency(k)

Data Format for the Argument Response in FRD Models

Properties

frd objects have the following properties:

Frequency

Frequency points of the frequency response data. Specify Frequency values in the units specified by the FrequencyUnit property.

FrequencyUnit

Frequency units of the model.

FrequencyUnit is a string that specifies the units of the frequency vector in the Frequency property. Set FrequencyUnit to one of the following values:

- 'rad/TimeUnit'
- 'cycles/TimeUnit'
- 'rad/s'
- 'Hz'
- 'kHz'
- 'MHz'
- 'GHz'
- 'rpm'

The units 'rad/TimeUnit' and 'cycles/TimeUnit' are relative to the time units specified in the TimeUnit property.

Changing this property changes the overall system behavior. Use chgFreqUnit to convert between frequency units without modifying system behavior.

Default: 'rad/TimeUnit'

ResponseData

Frequency response data.

The 'ResponseData' property stores the frequency response data as a 3-D array of complex numbers. For SISO systems, 'ResponseData' is a vector of frequency response values at the frequency points specified in the 'Frequency' property. For MIMO systems with Nu inputs and Ny outputs, 'ResponseData' is an array of size [Ny Nu Nw], where Nw is the number of frequency points.

ioDelay

Transport delays. **ioDelay** is a numeric array specifying a separate transport delay for each input/output pair.

For continuous-time systems, specify transport delays in the time unit stored in the TimeUnit property. For discrete-time systems, specify transport delays in integer multiples of the sample time, TS.

For a MIMO system with Ny outputs and Nu inputs, set ioDelay to a Ny-by-Nu array. Each entry of this array is a numerical value that represents the transport delay for the corresponding input/output pair. You can also set ioDelay to a scalar value to apply the same delay to all input/output pairs.

Default: 0 for all input/output pairs

InputDelay

Input delay for each input channel, specified as a scalar value or numeric vector. For continuous-time systems, specify input delays in the time unit stored in the TimeUnit property. For discrete-time systems, specify input delays in integer multiples of the sample time Ts. For example, InputDelay = 3 means a delay of three sample times.

For a system with Nu inputs, set InputDelay to an Nu-by-1 vector. Each entry of this vector is a numerical value that represents the input delay for the corresponding input channel.

You can also set InputDelay to a scalar value to apply the same delay to all channels.

Default: 0

OutputDelay

Output delays. OutputDelay is a numeric vector specifying a time delay for each output channel. For continuous-time systems, specify output delays in the time unit stored in the TimeUnit property. For discrete-time systems, specify output delays in integer multiples of the sample time TS. For example, OutputDelay = 3 means a delay of three sampling periods.

For a system with Ny outputs, set OutputDelay to an Ny-by-1 vector, where each entry is a numerical value representing the output delay for the corresponding output channel. You can also set OutputDelay to a scalar value to apply the same delay to all channels.

Default: 0 for all output channels

Ts

Sample time. For continuous-time models, Ts = 0. For discrete-time models, Ts is a positive scalar representing the sampling period. This value is expressed in the unit specified by the TimeUnit property of the model. To denote a discrete-time model with unspecified sample time, set Ts = -1.

Changing this property does not discretize or resample the model. Use c2d and d2c to convert between continuous- and discrete-time representations. Use d2d to change the sample time of a discrete-time system.

Default: 0 (continuous time)

TimeUnit

String representing the unit of the time variable. This property specifies the units for the time variable, the sample time Ts, and any time delays in the model. Use any of the following values:

- 'nanoseconds'
- 'microseconds'
- 'milliseconds'
- 'seconds'
- 'minutes'
- 'hours'
- 'days'
- 'weeks'
- 'months'
- 'years'

Changing this property has no effect on other properties, and therefore changes the overall system behavior. Use chgTimeUnit to convert between time units without modifying system behavior.

Default: 'seconds'

InputName

Input channel names. Set InputName to a string for single-input model. For a multiinput model, set InputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign input names for multi-input models. For example, if **sys** is a two-input model, enter:

```
sys.InputName = 'controls';
```

The input names automatically expand to { 'controls(1) '; 'controls(2) '}.

You can use the shorthand notation u to refer to the InputName property. For example, sys.u is equivalent to sys.InputName.

Input channel names have several uses, including:

- · Identifying channels on model display and plots
- Extracting subsystems of MIMO systems
- Specifying connection points when interconnecting models

Default: Empty string ' ' for all input channels

InputUnit

Input channel units. Use InputUnit to keep track of input signal units. For a singleinput model, set InputUnit to a string. For a multi-input model, set InputUnit to a cell array of strings. InputUnit has no effect on system behavior.

Default: Empty string ' ' for all input channels

InputGroup

Input channel groups. The InputGroup property lets you assign the input channels of MIMO systems into groups and refer to each group by name. Specify input groups as a structure. In this structure, field names are the group names, and field values are the input channels belonging to each group. For example:

```
sys.InputGroup.controls = [1 2];
sys.InputGroup.noise = [3 5];
```

creates input groups named controls and noise that include input channels 1, 2 and 3, 5, respectively. You can then extract the subsystem from the controls inputs to all outputs using:

```
sys(:,'controls')
```

Default: Struct with no fields

OutputName

Output channel names. Set OutputName to a string for single-output model. For a multioutput model, set OutputName to a cell array of strings. Alternatively, use automatic vector expansion to assign output names for multi-output models. For example, if **sys** is a two-output model, enter:

```
sys.OutputName = 'measurements';
```

```
The output names automatically expand to { 'measurements(1) '; 'measurements(2) ' }.
```

You can use the shorthand notation y to refer to the OutputName property. For example, sys.y is equivalent to sys.OutputName.

Output channel names have several uses, including:

- · Identifying channels on model display and plots
- · Extracting subsystems of MIMO systems
- · Specifying connection points when interconnecting models

Default: Empty string ' ' for all output channels

OutputUnit

Output channel units. Use OutputUnit to keep track of output signal units. For a single-output model, set OutputUnit to a string. For a multi-output model, set OutputUnit to a cell array of strings. OutputUnit has no effect on system behavior.

Default: Empty string '' for all output channels

OutputGroup

Output channel groups. The OutputGroup property lets you assign the output channels of MIMO systems into groups and refer to each group by name. Specify output groups as a structure. In this structure, field names are the group names, and field values are the output channels belonging to each group. For example:

```
sys.OutputGroup.temperature = [1];
sys.InputGroup.measurement = [3 5];
```

creates output groups named temperature and measurement that include output channels 1, and 3, 5, respectively. You can then extract the subsystem from all inputs to the measurement outputs using:

```
sys('measurement',:)
```

Default: Struct with no fields

Name

System name. Set Name to a string to label the system.

Default: ' '

Notes

Any text that you want to associate with the system. Set **Notes** to a string or a cell array of strings.

Default: { }

UserData

Any type of data you want to associate with system. Set UserData to any MATLAB data type.

Default: []

SamplingGrid

Sampling grid for model arrays, specified as a data structure.

For model arrays that are derived by sampling one or more independent variables, this property tracks the variable values associated with each model in the array. This information appears when you display or plot the model array. Use this information to trace results back to the independent variables.

Set the field names of the data structure to the names of the sampling variables. Set the field values to the sampled variable values associated with each model in the array. All sampling variables should be numeric and scalar valued, and all arrays of sampled values should match the dimensions of the model array.

For example, suppose you create a 11-by-1 array of linear models, sysarr, by taking snapshots of a linear time-varying system at times t = 0:10. The following code stores the time samples with the linear models.

```
sysarr.SamplingGrid = struct('time',0:10)
```

Similarly, suppose you create a 6-by-9 model array, M, by independently sampling two variables, zeta and w. The following code attaches the (zeta,w) values to M.

```
[zeta,w] = ndgrid(<6 values of zeta>,<9 values of w>)
M.SamplingGrid = struct('zeta',zeta,'w',w)
```

When you display M, each entry in the array includes the corresponding zeta and w values.

For model arrays generated by linearizing a Simulink[®] model at multiple parameter values or operating points, the software populates SamplingGrid automatically with the variable values that correspond to each entry in the array. For example, the Simulink Control DesignTM commands linearize and slLinearizer populate SamplingGrid in this way.

Default: []

Examples

Create Frequency-Response Model

Create a SISO FRD model from a frequency vector and response data:

```
% generate a frequency vector and response data
freq = logspace(1,2);
resp = .05*(freq).*exp(i*2*freq);
% Create a FRD model
sys = frd(resp,freq);
```

More About

- "What Are Model Objects?"
- "Frequency Response Data (FRD) Models"

See Also

chgTimeUnit | chgFreqUnit | frdata | set | ss | tf | zpk | idfrd

Introduced before R2006a

frdata

Access data for frequency response data (FRD) object

Syntax

```
[response,freq] = frdata(sys)
[response,freq,covresp] = frdata(sys)
[response,freq,Ts,covresp] = frdata(sys,'v')
[response,freq,Ts] = frdata(sys)
```

Description

[response,freq] = frdata(sys) returns the response data and frequency samples of the FRD model sys. For an FRD model with Ny outputs and Nu inputs at Nf frequencies:

- response is an Ny-by-Nu-by-Nf multidimensional array where the (i, j) entry specifies the response from input j to output i.
- freq is a column vector of length Nf that contains the frequency samples of the FRD model.

See the ${\tt frd}$ reference page for more information on the data format for FRD response data.

[response, freq, covresp] = frdata(sys) also returns the covariance covresp of the response data resp for idfrd model sys. (Using idfrd models requires System Identification Toolbox software.) The covariance covresp is a 5D-array where covH(i, j, k, :, :) contains the 2-by-2 covariance matrix of the response resp(i, j, k). The (1,1) element is the variance of the real part, the (2,2) element the variance of the imaginary part and the (1,2) and (2,1) elements the covariance between the real and imaginary parts.

For SISO FRD models, the syntax

[response,freq] = frdata(sys,'v')

forces frdata to return the response data as a column vector rather than a 3dimensional array (see example below). Similarly [response,freq,Ts,covresp] = frdata(sys,'v') for an IDFRD model sys returns covresp as a 3-dimensional rather than a 5-dimensional array.

[response,freq,Ts] = frdata(sys) also returns the sample time Ts.

Other properties of sys can be accessed with get or by direct structure-like referencing (e.g., sys.Frequency).

Arguments

The input argument sys to frdata must be an FRD model.

Examples

Extract Data from Frequency Response Data Model

Create a frequency response data model and extract the frequency response data.

Create a frequency response data by computing the response of a transfer function on a grid of frequencies.

H = tf([-1.2,-2.4,-1.5],[1,20,9.1]); w = logspace(-2,3,101); sys = frd(H,w);

sys is a SISO frequency response data (frd) model containing the frequency response at 101 frequencies.

Extract the frequency response data from sys.

[response,freq] = frdata(sys);

response is a 1-by-1-by-101 array. response(1,1,k) is the complex frequency response at the frequency freq(k).

See Also frd | get | set | freqresp

Introduced before R2006a

freqresp

Frequency response over grid

Syntax

```
[H,wout] = freqresp(sys)
H = freqresp(sys,w)
H = freqresp(sys,w,units)
[H,wout,covH] = freqresp(idsys,...)
```

Description

[H,wout] = freqresp(sys) returns the frequency response of the dynamic system model sys at frequencies wout. The freqresp command automatically determines the frequencies based on the dynamics of sys.

H = freqresp(sys,w) returns the frequency response on the real frequency grid specified by the vector W.

H = freqresp(sys,w,units) explicitly specifies the frequency units of w with the string units.

[H,wout,covH] = freqresp(idsys,...) also returns the covariance covH of the frequency response of the identified model idsys.

Input Arguments

sys

Any dynamic system model or model array.

w

Vector of real frequencies at which to evaluate the frequency response. Specify frequencies in units of rad/TimeUnit, where TimeUnit is the time units specified in the TimeUnit property of sys.

units

String specifying the units of the frequencies in the input frequency vector w. Units can take the following values:

- <code>'rad/TimeUnit'</code> radians per the time unit specified in the <code>TimeUnit</code> property of <code>sys</code>
- 'cycles/TimeUnit' cycles per the time unit specified in the TimeUnit property of sys
- 'rad/s'
- 'Hz'
- 'kHz'
- 'MHz'
- 'GHz'
- 'rpm'

Default: 'rad/TimeUnit'

idsys

Any identified model.

Output Arguments

H

Array containing the frequency response values.

If sys is an individual dynamic system model having Ny outputs and Nu inputs, H is a 3D array with dimensions Ny-by-Nu-by-Nw, where Nw is the number of frequency points. Thus, H(:,:,k) is the response at the frequency w(k) or wout(k).

If sys is a model array of size [Ny Nu S1 \dots Sn], H is an array with dimensions Ny-by-Nu-by-Nu-by-S1-by-...-by-Sn] array.

If sys is a frequency response data model (such as frd, genfrd, or idfrd), freqresp(sys,w) evaluates to NaN for values of w falling outside the frequency

interval defined by sys.frequency. The freqresp command can interpolate between frequencies in sys.frequency. However, freqresp cannot extrapolate beyond the frequency interval defined by sys.frequency.

wout

Vector of frequencies corresponding to the frequency response values in H. If you omit w from the inputs to freqresp, the command automatically determines the frequencies of wout based on the system dynamics. If you specify w, then wout = w

covH

Covariance of the response H. The covariance is a 5D array where CovH(i, j, k, :, :) contains the 2-by-2 covariance matrix of the response from the ith input to the jth output at frequency W(k). The (1,1) element of this 2-by-2 matrix is the variance of the real part of the response. The (2,2) element is the variance of the imaginary part. The (1,2) and (2,1) elements are the covariance between the real and imaginary parts of the response.

Examples

Frequency Response

Compute the frequency response of the 2-input, 2-output system

$$sys = \begin{bmatrix} 0 & \frac{1}{s+1} \\ \frac{s-1}{s+2} & 1 \end{bmatrix}$$

```
sys11 = 0;
sys22 = 1;
sys12 = tf(1,[1 1]);
sys21 = tf([1 -1],[1 2]);
sys = [sys11,sys12;sys21,sys22];
[H,wout] = freqresp(sys);
```

H is a 2-by-2-by-45 array. Each entry H(:,:,k) in H is a 2-by-2 matrix giving the complex frequency response of all input-output pairs of sys at the corresponding frequency wout(k). The 45 frequencies in wout are automatically selected based on the dynamics of sys.

Response on Specified Frequency Grid

Compute the frequency response of the 2-input, 2-output system

$$sys = \begin{bmatrix} 0 & \frac{1}{s+1} \\ \frac{s-1}{s+2} & 1 \end{bmatrix}$$

on a logarithmically-spaced grid of 200 frequency points between 10 and 100 radians per second.

```
sys11 = 0;
sys22 = 1;
sys12 = tf(1,[1 1]);
sys21 = tf([1 -1],[1 2]);
sys = [sys11,sys12;sys21,sys22];
w = logspace(1,2,200);
H = freqresp(sys,w);
```

H is a 2-by-2-by-200 array. Each entry H(:,:,k) in H is a 2-by-2 matrix giving the complex frequency response of all input-output pairs of sys at the corresponding frequency W(k).

Frequency Response and Associated Covariance

Compute the frequency response and associated covariance for an identified model at its peak response frequency.

```
load iddata1 z1
model = procest(z1, 'P2UZ');
w = 4.26;
```

```
[H,~,covH] = freqresp(model, w)
```

Alternatives

Use evalfr to evaluate the frequency response at individual frequencies or small numbers of frequencies. freqresp is optimized for medium-to-large vectors of frequencies.

More About

Frequency Response

In continuous time, the *frequency response* at a frequency ω is the transfer function value at $s = j\omega$. For state-space models, this value is given by

$$H(j\omega) = D + C(j\omega I - A)^{-1}B$$

In discrete time, the frequency response is the transfer function evaluated at points on the unit circle that correspond to the real frequencies. freqresp maps the real

frequencies w(1),..., w(N) to points on the unit circle using the transformation $z = e^{j\omega T_s}$. T_s is the sample time. The function returns the values of the transfer function at the resulting z values. For models with unspecified sample time, freqresp uses $T_s = 1$.

Algorithms

For transfer functions or zero-pole-gain models, freqresp evaluates the numerator(s) and denominator(s) at the specified frequency points. For continuous-time state-space models (A, B, C, D), the frequency response is

 $D + C(j\omega - A)^{-1}B, \quad \omega = \omega_1, \dots, \omega_N$

For efficiency, *A* is reduced to upper Hessenberg form and the linear equation $(j\omega - A)X = B$ is solved at each frequency point, taking advantage of the Hessenberg structure. The reduction to Hessenberg form provides a good compromise between efficiency and reliability. See [1] for more details on this technique.

References

[1] Laub, A.J., "Efficient Multivariable Frequency Response Computations," *IEEE Transactions on Automatic Control*, AC-26 (1981), pp. 407-408.

See Also

bode | nyquist | interp | evalfr | nichols | sigma | linearSystemAnalyzer |
spectrum

Introduced before R2006a

freqsep

Slow-fast decomposition

Syntax

```
[Gs,Gf] = freqsep(G,fcut)
[Gs,Gf] = freqsep(G,fcut,options)
```

Description

[Gs,Gf] = freqsep(G,fcut) decomposes a linear dynamic system into slow and fast components around the specified cutoff frequency. The decomposition is such that G = Gs + Gf.

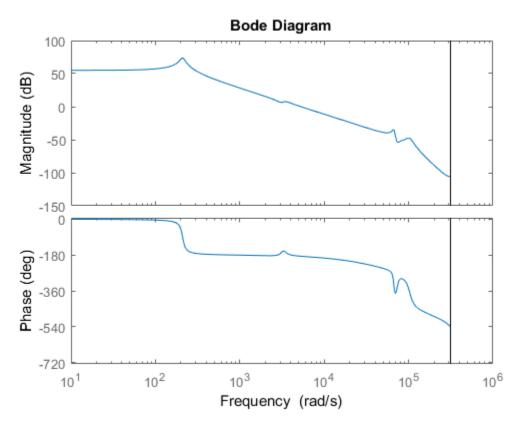
[Gs,Gf] = freqsep(G,fcut,options) specifies additional options for the decomposition.

Examples

Decompose Model into Fast and Slow Dynamics

Load a dynamic system model.

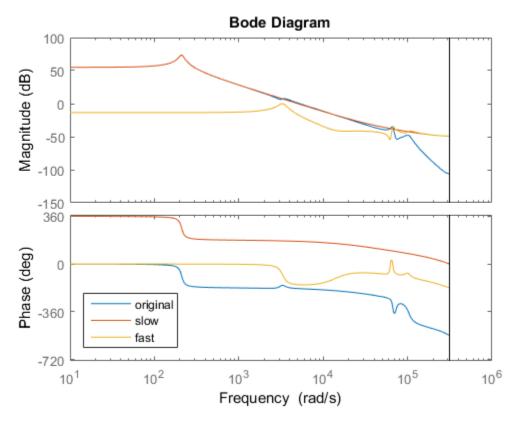
load numdemo Pd
bode(Pd)



Pd has four complex poles and one real pole. The Bode plot shows a resonance around 210 rad/s and a higher-frequency resonance below 10,000 rad/s.

Decompose this model around 1000 rad/s to separate these two resonances.

```
[Gs,Gf] = freqsep(Pd,10^3);
bode(Pd,Gs,Gf)
legend('original','slow','fast','Location','Southwest')
```



The Bode plot shows that the slow component, **Gs**, contains only the lower-frequency resonance. This component also matches the DC gain of the original model. The fast component, **Gf**, contains the higher-frequency resonances and matches the response of the original model at high frequencies. The sum of the two components **Gs+Gf** yields the original model.

Separate Nearby Modes by Adjusting Tolerance

Decompose a model into slow and fast components between poles that are closely spaced.

The following system includes a real pole and a complex pair of poles that are all close to s = -2.

G = zpk(-.5,[-1.9999 -2+1e-4i -2-1e-4i],10);

Try to decompose the model about 2 rad/s, so that the slow component cotains the real pole and the fast component contains the complex pair.

[Gs,Gf] = freqsep(G,2);

Warning: One or more fast modes could not be separated from the slow modes. To force separation, increase the absolute or relative tolerances ("AbsTol" and "RelTol" options). Type "help freqsepOptions" for more information.

These poles are too close together for freqsep to separate. Increase the relative tolerance to allow the separation.

```
options = freqsepOptions('RelTol',1e-4);
[Gs,Gf] = freqsep(G,2,options);
```

Now freqsep successfully separates the dynamics about 2 rad/s.

```
slowpole = pole(Gs)
fastpole = pole(Gf)
slowpole =
    -1.9999
fastpole =
    -2.0000 + 0.0001i
    -2.0000 - 0.0001i
```

Input Arguments

G — Dynamic system to decompose

numeric LTI model

Dynamic system to decompose, specified as a numeric LTI model, such as a **ss** or tf model.

fcut — Cutoff frequency

positive scalar

Cutoff frequency for fast-slow decomposition, specified as a positive scalar. The output Gs contains all poles with natural frequency less than fcut. The output Gf contains all poles with natural frequency greater than or equal to fcut.

options - Options for decomposition

freqsepOptions options set

Options for the decomposition, specified as an options set you create with freqsepOptions. Available options include absolute and relative tolerance for accuracy of the decomposed systems.

Output Arguments

Gs — **Slow dynamics** numeric LTI model

Slow dynamics of the decomposed system, returned as a numeric LTI model of the same type as G. Gs contains all poles of G with natural frequency less than fcut, and is such that G = Gs + Gf.

Gf — **Fast dynamics** numeric LTI model

Fast dynamics of the decomposed system, returned as a numeric LTI model of the same type as G. Gf contains all poles of G with natural frequency greater than or equal to fcut, and is such that G = Gs + Gf.

See Also freqsepOptions

Introduced in R2014a

freqsepOptions

Options for slow-fast decomposition

Syntax

opt = freqsepOptions
opt = freqsepOptions(Name,Value)

Description

opt = freqsepOptions returns the default options for freqsep.

opt = freqsepOptions(Name,Value) returns an options set with the options
specified by one or more Name,Value pair arguments.

Examples

Separate Nearby Modes by Adjusting Tolerance

Decompose a model into slow and fast components between poles that are closely spaced.

The following system includes a real pole and a complex pair of poles that are all close to s = -2.

G = zpk(-.5,[-1.9999 -2+1e-4i -2-1e-4i],10);

Try to decompose the model about 2 rad/s, so that the slow component cotains the real pole and the fast component contains the complex pair.

```
[Gs,Gf] = freqsep(G,2);
```

```
Warning: One or more fast modes could not be separated from the slow modes. To force separation, increase the absolute or relative tolerances ("AbsTol" and "RelTol" options). Type "help freqsepOptions" for more information.
```

These poles are too close together for freqsep to separate. Increase the relative tolerance to allow the separation.

```
options = freqsepOptions('RelTol',1e-4);
[Gs,Gf] = freqsep(G,2,options);
```

Now freqsep successfully separates the dynamics about 2 rad/s.

```
slowpole = pole(Gs)
fastpole = pole(Gf)
slowpole =
    -1.9999
fastpole =
    -2.0000 + 0.0001i
    -2.0000 - 0.0001i
```

Input Arguments

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside single quotes (' '). You can specify several name and value pair arguments in any order as Name1, Value1, ..., NameN, ValueN.

```
Example: 'AbsTol', 1e-4
```

'AbsTol' – Absolute tolerance for decomposition

0 (default) | nonnegative scalar

Absolute tolerance for slow-fast decomposition, specified as a nonnegative scalar value. freqresp ensures that the frequency responses of the original system, G, and the sum of the decomposed systems Gs+Gf, differ by no more than AbsTol + RelTol*abs(G). Increase AbsTol to help separate nearby modes, at the expense of the accuracy of the decomposition.

'RelTol' - Relative tolerance for decomposition

```
1e-8 (default) | nonnegative scalar
```

Relative tolerance for slow-fast decomposition, specified as a nonnegative scalar value. freqresp ensures that the frequency responses of the original system, G, and the sum of the decomposed systems Gs+Gf, differ by no more than AbsTol + RelTol*abs(G). Increase RelTol to help separate nearby modes, at the expense of the accuracy of the decomposition.

Output Arguments

opt - Options for freqsep

freqsepOptions options set

Options for freqsep, returned as a freqsepOptions options set. Use opt as the last argument to freqsep when computing slow-fast decomposition.

See Also

freqsep

Introduced in R2014a

fselect

Select frequency points or range in FRD model

Syntax

```
subsys = fselect(sys,fmin,fmax)
subsys = fselect(sys,index)
```

Description

subsys = fselect(sys,fmin,fmax) takes an FRD model sys and selects the portion
of the frequency response between the frequencies fmin and fmax. The selected range
[fmin,fmax] should be expressed in the FRD model units. For an IDFRD model
(requires System Identification Toolbox software), the SpectrumData, CovarianceData
and NoiseCovariance values, if non-empty, are also selected in the chosen range.

subsys = fselect(sys,index) selects the frequency points specified by the vector of
indices index. The resulting frequency grid is

```
sys.Frequency(index)
```

See Also

fcat | fdel | interp | frd

Introduced before R2006a

gcare

Generalized solver for continuous-time algebraic Riccati equation

Syntax

```
[X,L,report] = gcare(H,J,ns)
[X1,X2,D,L] = gcare(H,...,'factor')
```

Description

[X,L,report] = gcare(H,J,ns) computes the unique stabilizing solution X of the continuous-time algebraic Riccati equation associated with a Hamiltonian pencil of the form

H-tJ =	$\int A$	F	S1		$\left\lceil E \right ight angle$	0	0]
H - tJ =	G	-A'	-S2	-	0	E'	0
	S2'	S1'	R		0	0	0

The optional input ns is the row size of the *A* matrix. Default values for J and ns correspond to E = I and R = [].

Optionally, gcare returns the vector L of closed-loop eigenvalues and a diagnosis report with value:

- -1 if the Hamiltonian pencil has *jw*-axis eigenvalues
- -2 if there is no finite stabilizing solution X
- 0 if a finite stabilizing solution X exists

This syntax does not issue any error message when X fails to exist.

[X1, X2, D, L] = gcare(H, ..., 'factor') returns two matrices X1, X2 and a diagonal scaling matrix D such that $X = D^*(X2/X1)^*D$. The vector L contains the closed-loop eigenvalues. All outputs are empty when the associated Hamiltonian matrix has eigenvalues on the imaginary axis.

See Also care | gdare

Introduced before R2006a

gdare

Generalized solver for discrete-time algebraic Riccati equation

Syntax

```
[X,L,report] = gdare(H,J,ns)
[X1,X2,D,L] = gdare(H,J,NS,'factor')
```

Description

[X,L,report] = gdare(H,J,ns) computes the unique stabilizing solution X of the discrete-time algebraic Riccati equation associated with a Symplectic pencil of the form

	$\int A$	F	B		E	0	0]
H - tJ =	-Q	E'	-S	-	0	A'	0
H-tJ =	S'	0	R		0	B'	0

The third input ns is the row size of the A matrix.

Optionally, gdare returns the vector L of closed-loop eigenvalues and a diagnosis report with value:

- -1 if the Symplectic pencil has eigenvalues on the unit circle
- -2 if there is no finite stabilizing solution X
- 0 if a finite stabilizing solution X exists

This syntax does not issue any error message when X fails to exist.

[X1, X2, D, L] = gdare(H, J, NS, 'factor') returns two matrices X1, X2 and a diagonal scaling matrix D such that $X = D^*(X2/X1)^*D$. The vector L contains the closed-loop eigenvalues. All outputs are empty when the Symplectic pencil has eigenvalues on the unit circle.

See Also

dare | gcare

Introduced before R2006a

genfrd

Generalized frequency response data (FRD) model

Description

Generalized FRD (genfrd) models arise when you combine numeric FRD models with models containing tunable components (Control Design Blocks). genfrd models keep track of how the tunable blocks interact with the tunable components. For more information about Control Design Blocks, see "Generalized Models".

Construction

To construct a genfrd model, use series, parallel, lft, or connect, or the arithmetic operators +, -, *, /, \, and ^, to combine a numeric FRD model with control design blocks.

You can also convert any numeric LTI model or control design block sys to genfrd form.

frdsys = genfrd(sys,freqs,frequnits) converts any static model or dynamic system sys to a generalized FRD model. If sys is not an frd model object, genfrd computes the frequency response of each frequency point in the vector freqs. The frequencies freqs are in the units specified by the optional argument frequnits. If frequnits is omitted, the units of freqs are 'rad/TimeUnit'.

frdsys = genfrd(sys,freqs,frequnits,timeunits) further specifies the time
units for converting sys to genfrd form.

For more information about time and frequency units of genfrd models, see "Properties" on page 1-225.

Input Arguments

sys

A static model or dynamic system model object.

freqs

Vector of frequency points. Express frequencies in the unit specified in frequnits.

frequnits

String specifying the frequency units of the genfrd model. Set frequnits to one of the following values:

- 'rad/TimeUnit'
- 'cycles/TimeUnit'
- 'rad/s'
- 'Hz'
- 'kHz'
- 'MHz'
- 'GHz'
- 'rpm'

Default: 'rad/TimeUnit'

timeunits

String specifying the time units of the genfrd model. Set timeunits to one of the following values:

- 'nanoseconds'
- 'microseconds'
- 'milliseconds'
- 'seconds'
- 'minutes'
- 'hours'
- 'days'
- 'weeks'
- 'months'
- 'years'

Default: 'seconds'

Properties

Blocks

Structure containing the control design blocks included in the generalized LTI model or generalized matrix. The field names of **Blocks** are the **Name** property of each control design block.

You can change some attributes of these control design blocks using dot notation. For example, if the generalized LTI model or generalized matrix M contains a realp tunable parameter a, you can change the current value of a using:

M.Blocks.a.Value = -1;

Frequency

Frequency points of the frequency response data. Specify Frequency values in the units specified by the FrequencyUnit property.

FrequencyUnit

Frequency units of the model.

FrequencyUnit is a string that specifies the units of the frequency vector in the Frequency property. Set FrequencyUnit to one of the following values:

- 'rad/TimeUnit'
- 'cycles/TimeUnit'
- 'rad/s'
- 'Hz'
- 'kHz'
- 'MHz'
- 'GHz'
- 'rpm'

The units 'rad/TimeUnit' and 'cycles/TimeUnit' are relative to the time units specified in the TimeUnit property.

Changing this property changes the overall system behavior. Use chgFreqUnit to convert between frequency units without modifying system behavior.

Default: 'rad/TimeUnit'

InputDelay

Input delay for each input channel, specified as a scalar value or numeric vector. For continuous-time systems, specify input delays in the time unit stored in the TimeUnit property. For discrete-time systems, specify input delays in integer multiples of the sample time Ts. For example, InputDelay = 3 means a delay of three sample times.

For a system with Nu inputs, set InputDelay to an Nu-by-1 vector. Each entry of this vector is a numerical value that represents the input delay for the corresponding input channel.

You can also set InputDelay to a scalar value to apply the same delay to all channels.

Default: 0

OutputDelay

Output delays. OutputDelay is a numeric vector specifying a time delay for each output channel. For continuous-time systems, specify output delays in the time unit stored in the TimeUnit property. For discrete-time systems, specify output delays in integer multiples of the sample time Ts. For example, OutputDelay = 3 means a delay of three sampling periods.

For a system with Ny outputs, set OutputDelay to an Ny-by-1 vector, where each entry is a numerical value representing the output delay for the corresponding output channel. You can also set OutputDelay to a scalar value to apply the same delay to all channels.

Default: 0 for all output channels

Ts

Sample time. For continuous-time models, Ts = 0. For discrete-time models, Ts is a positive scalar representing the sampling period. This value is expressed in the unit specified by the TimeUnit property of the model. To denote a discrete-time model with unspecified sample time, set Ts = -1.

Changing this property does not discretize or resample the model. Use c2d and d2c to convert between continuous- and discrete-time representations. Use d2d to change the sample time of a discrete-time system.

Default: 0 (continuous time)

TimeUnit

String representing the unit of the time variable. This property specifies the units for the time variable, the sample time Ts, and any time delays in the model. Use any of the following values:

- 'nanoseconds'
- 'microseconds'
- 'milliseconds'
- 'seconds'
- 'minutes'
- 'hours'
- 'days'
- 'weeks'
- 'months'
- 'years'

Changing this property has no effect on other properties, and therefore changes the overall system behavior. Use chgTimeUnit to convert between time units without modifying system behavior.

Default: 'seconds'

InputName

Input channel names. Set InputName to a string for single-input model. For a multiinput model, set InputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign input names for multi-input models. For example, if **sys** is a two-input model, enter:

sys.InputName = 'controls';

The input names automatically expand to { 'controls(1) '; 'controls(2) '}.

You can use the shorthand notation u to refer to the InputName property. For example, sys.u is equivalent to sys.InputName.

Input channel names have several uses, including:

- · Identifying channels on model display and plots
- · Extracting subsystems of MIMO systems
- · Specifying connection points when interconnecting models

Default: Empty string ' ' for all input channels

InputUnit

Input channel units. Use InputUnit to keep track of input signal units. For a singleinput model, set InputUnit to a string. For a multi-input model, set InputUnit to a cell array of strings. InputUnit has no effect on system behavior.

Default: Empty string ' ' for all input channels

InputGroup

Input channel groups. The InputGroup property lets you assign the input channels of MIMO systems into groups and refer to each group by name. Specify input groups as a structure. In this structure, field names are the group names, and field values are the input channels belonging to each group. For example:

sys.InputGroup.controls = [1 2]; sys.InputGroup.noise = [3 5];

creates input groups named controls and noise that include input channels 1, 2 and 3, 5, respectively. You can then extract the subsystem from the controls inputs to all outputs using:

```
sys(:,'controls')
```

Default: Struct with no fields

OutputName

Output channel names. Set OutputName to a string for single-output model. For a multioutput model, set OutputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign output names for multi-output models. For example, if **sys** is a two-output model, enter:

```
sys.OutputName = 'measurements';
```

```
The output names automatically expand to { 'measurements(1)'; 'measurements(2)'}.
```

You can use the shorthand notation y to refer to the OutputName property. For example, sys.y is equivalent to sys.OutputName.

Output channel names have several uses, including:

- · Identifying channels on model display and plots
- Extracting subsystems of MIMO systems
- · Specifying connection points when interconnecting models

Default: Empty string ' ' for all output channels

OutputUnit

Output channel units. Use OutputUnit to keep track of output signal units. For a single-output model, set OutputUnit to a string. For a multi-output model, set OutputUnit to a cell array of strings. OutputUnit has no effect on system behavior.

Default: Empty string ' ' for all output channels

OutputGroup

Output channel groups. The OutputGroup property lets you assign the output channels of MIMO systems into groups and refer to each group by name. Specify output groups as a structure. In this structure, field names are the group names, and field values are the output channels belonging to each group. For example:

```
sys.OutputGroup.temperature = [1];
sys.InputGroup.measurement = [3 5];
```

creates output groups named temperature and measurement that include output channels 1, and 3, 5, respectively. You can then extract the subsystem from all inputs to the measurement outputs using:

```
sys('measurement',:)
```

Default: Struct with no fields

Name

System name. Set Name to a string to label the system.

Default: ' '

Notes

Any text that you want to associate with the system. Set **Notes** to a string or a cell array of strings.

Default: {}

UserData

Any type of data you want to associate with system. Set UserData to any MATLAB data type.

Default: []

SamplingGrid

Sampling grid for model arrays, specified as a data structure.

For model arrays that are derived by sampling one or more independent variables, this property tracks the variable values associated with each model in the array. This information appears when you display or plot the model array. Use this information to trace results back to the independent variables.

Set the field names of the data structure to the names of the sampling variables. Set the field values to the sampled variable values associated with each model in the array. All sampling variables should be numeric and scalar valued, and all arrays of sampled values should match the dimensions of the model array.

For example, suppose you create a 11-by-1 array of linear models, sysarr, by taking snapshots of a linear time-varying system at times t = 0:10. The following code stores the time samples with the linear models.

```
sysarr.SamplingGrid = struct('time',0:10)
```

Similarly, suppose you create a 6-by-9 model array, M, by independently sampling two variables, zeta and w. The following code attaches the (zeta,w) values to M.

```
[zeta,w] = ndgrid(<6 values of zeta>,<9 values of w>)
M.SamplingGrid = struct('zeta',zeta,'w',w)
```

When you display M, each entry in the array includes the corresponding ${\tt zeta}$ and w values.

For model arrays generated by linearizing a Simulink model at multiple parameter values or operating points, the software populates SamplingGrid automatically with the variable values that correspond to each entry in the array. For example, the Simulink Control Design commands linearize and slLinearizer populate SamplingGrid in this way.

Default: []

More About

Tips

- You can manipulate genfrd models as ordinary frd models. Frequency-domain analysis commands such as bode evaluate the model by replacing each tunable parameter with its current value.
- "Models with Tunable Coefficients"
- "Generalized Models"

See Also

frd | genss | getValue | chgFreqUnit

Introduced in R2011a

genmat

Generalized matrix with tunable parameters

Description

Generalized matrices (genmat) are matrices that depend on tunable parameters (see realp). You can use generalized matrices for parameter studies. You can also use generalized matrices for building generalized LTI models (see genss) that represent control systems having a mixture of fixed and tunable components.

Construction

Generalized matrices arise when you combine numeric values with static blocks such as realp objects. You create such combinations using any of the arithmetic operators +, -, *, /, \, and ^. For example, if a and b are tunable parameters, the expression M = a + b is represented as a generalized matrix.

The internal data structure of the genmat object M keeps track of how M depends on the parameters a and b. The Blocks property of M lists the parameters a and b.

M = genmat(A) converts the numeric array or tunable parameter A into a genmat object.

Input Arguments

A

Static control design block, such as a realp object.

If \boldsymbol{A} is a numeric array, \boldsymbol{M} is a generalized matrix of the same dimensions as $\boldsymbol{A},$ with no tunable parameters.

If A is a static control design block, M is a generalized matrix whose ${\tt Blocks}$ property lists A as the only block.

Properties

Blocks

Structure containing the control design blocks included in the generalized LTI model or generalized matrix. The field names of **Blocks** are the **Name** property of each control design block.

You can change some attributes of these control design blocks using dot notation. For example, if the generalized LTI model or generalized matrix M contains a realp tunable parameter a, you can change the current value of a using:

M.Blocks.a.Value = -1;

SamplingGrid

Sampling grid for model arrays, specified as a data structure.

For model arrays that are derived by sampling one or more independent variables, this property tracks the variable values associated with each model in the array. This information appears when you display or plot the model array. Use this information to trace results back to the independent variables.

Set the field names of the data structure to the names of the sampling variables. Set the field values to the sampled variable values associated with each model in the array. All sampling variables should be numeric and scalar valued, and all arrays of sampled values should match the dimensions of the model array.

For example, suppose you create a 11-by-1 array of linear models, sysarr, by taking snapshots of a linear time-varying system at times t = 0:10. The following code stores the time samples with the linear models.

```
sysarr.SamplingGrid = struct('time',0:10)
```

Similarly, suppose you create a 6-by-9 model array, M, by independently sampling two variables, zeta and w. The following code attaches the (zeta,w) values to M.

```
[zeta,w] = ndgrid(<6 values of zeta>,<9 values of w>)
M.SamplingGrid = struct('zeta',zeta,'w',w)
```

When you display M, each entry in the array includes the corresponding ${\tt zeta}$ and w values.

For model arrays generated by linearizing a Simulink model at multiple parameter values or operating points, the software populates SamplingGrid automatically with the variable values that correspond to each entry in the array. For example, the Simulink Control Design commands linearize and slLinearizer populate SamplingGrid in this way.

Default: []

Examples

Generalized Matrix With Two Tunable Parameters

This example shows how to use algebraic combinations of tunable parameters to create the generalized matrix:

$$M = \begin{bmatrix} 1 & a+b \\ 0 & ab \end{bmatrix},$$

where a and b are tunable parameters with initial values -1 and 3, respectively.

1 Create the tunable parameters using realp.

a = realp('a',-1); b = realp('b',3); **2** Define the generalized matrix using algebraic expressions of **a** and **b**.

 $M = [1 \ a+b; 0 \ a*b]$

M is a generalized matrix whose Blocks property contains a and b. The initial value of M is $M = [1 \ 2; 0 \ -3]$, from the initial values of a and b.

3 (Optional) Change the initial value of the parameter **a**.

M.Blocks.a.Value = -3;

4 (Optional) Use double to display the new value of M.

double(M)

The new value of M is $M = [1 \ 0; 0 \ -9]$.

More About

- "Models with Tunable Coefficients"
- "Dynamic System Models"

See Also

realp | genss | getValue

Introduced in R2011a

gensig

Generate test input signals for <code>lsim</code>

Syntax

```
[u,t] = gensig(type,tau)
[u,t] = gensig(type,tau,Tf,Ts)
```

Description

[u,t] = gensig(type,tau) generates a scalar signal u of class type and with
period tau (in seconds). The following types of signals are available.

'sin'	Sine wave.
'square'	Square wave.
'pulse'	Periodic pulse.

gensig returns a vector t of time samples and the vector u of signal values at these samples. All generated signals have unit amplitude.

[u,t] = gensig(type,tau,Tf,Ts) also specifies the time duration Tf of the signal
and the spacing Ts between the time samples t.

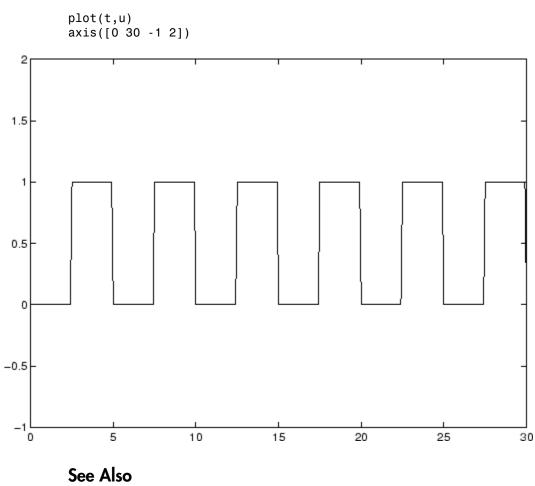
You can feed the outputs u and t directly to lsim and simulate the response of a singleinput linear system to the specified signal. Since t is uniquely determined by Tf and Ts, you can also generate inputs for multi-input systems by repeated calls to gensig.

Examples

Generate a square wave with period 5 seconds, duration 30 seconds, and sampling every 0.1 second.

[u,t] = gensig('square',5,30,0.1)

Plot the resulting signal.





Introduced before R2006a

genss

Generalized state-space model

Description

Generalized state-space (genss) models are state-space models that include tunable parameters or components. genss models arise when you combine numeric LTI models with models containing tunable components (control design blocks). For more information about numeric LTI models and control design blocks, see "Models with Tunable Coefficients".

You can use generalized state-space models to represent control systems having a mixture of fixed and tunable components. Use generalized state-space models for control design tasks such as parameter studies and parameter tuning with hinfstruct (requires Robust Control Toolbox).

Construction

To construct a genss model:

- Use series, parallel, lft, or connect, or the arithmetic operators +, -, *, /, \, and ^, to combine numeric LTI models with control design blocks.
- Use tf or ss with one or more input arguments that is a generalized matrix (genmat) instead of a numeric array
- Convert any numeric LTI model, control design block, or slTuner interface (requires Simulink Control Design), for example, sys, to genss form using:

```
gensys = genss(sys)
```

When sys is an slTuner interface, gensys contains all the tunable blocks and analysis points specified in this interface. To compute a tunable model of a particular I/O transfer function, call getIOTransfer(gensys, in,out). Here, in and out are the analysis points of interest. (Use getPoints(sys) to get the full list of analysis points.) Similarly, to compute a tunable model of a particular open-loop transfer function, use getLoopTransfer(gensys,loc). Here, loc is the analysis point of interest.

Properties

Blocks

Structure containing the control design blocks included in the generalized LTI model or generalized matrix. The field names of **Blocks** are the **Name** property of each control design block.

You can change some attributes of these control design blocks using dot notation. For example, if the generalized LTI model or generalized matrix M contains a realp tunable parameter a, you can change the current value of a using:

M.Blocks.a.Value = -1;

InternalDelay

Vector storing internal delays.

Internal delays arise, for example, when closing feedback loops on systems with delays, or when connecting delayed systems in series or parallel. For more information about internal delays, see "Closing Feedback Loops with Time Delays" in the *Control System Toolbox User's Guide*.

For continuous-time models, internal delays are expressed in the time unit specified by the TimeUnit property of the model. For discrete-time models, internal delays are expressed as integer multiples of the sample time Ts. For example, InternalDelay = 3 means a delay of three sampling periods.

You can modify the values of internal delays. However, the number of entries in **sys.InternalDelay** cannot change, because it is a structural property of the model.

InputDelay

Input delay for each input channel, specified as a scalar value or numeric vector. For continuous-time systems, specify input delays in the time unit stored in the TimeUnit property. For discrete-time systems, specify input delays in integer multiples of the sample time Ts. For example, InputDelay = 3 means a delay of three sample times.

For a system with Nu inputs, set InputDelay to an Nu-by-1 vector. Each entry of this vector is a numerical value that represents the input delay for the corresponding input channel.

You can also set InputDelay to a scalar value to apply the same delay to all channels.

Default: 0

OutputDelay

Output delays. OutputDelay is a numeric vector specifying a time delay for each output channel. For continuous-time systems, specify output delays in the time unit stored in the TimeUnit property. For discrete-time systems, specify output delays in integer multiples of the sample time Ts. For example, OutputDelay = 3 means a delay of three sampling periods.

For a system with Ny outputs, set OutputDelay to an Ny-by-1 vector, where each entry is a numerical value representing the output delay for the corresponding output channel. You can also set OutputDelay to a scalar value to apply the same delay to all channels.

Default: 0 for all output channels

Ts

Sample time. For continuous-time models, Ts = 0. For discrete-time models, Ts is a positive scalar representing the sampling period. This value is expressed in the unit specified by the TimeUnit property of the model. To denote a discrete-time model with unspecified sample time, set Ts = -1.

Changing this property does not discretize or resample the model. Use c2d and d2c to convert between continuous- and discrete-time representations. Use d2d to change the sample time of a discrete-time system.

Default: 0 (continuous time)

TimeUnit

String representing the unit of the time variable. This property specifies the units for the time variable, the sample time Ts, and any time delays in the model. Use any of the following values:

- 'nanoseconds'
- 'microseconds'
- 'milliseconds'
- 'seconds'

- 'minutes'
- 'hours'
- 'days'
- 'weeks'
- 'months'
- 'years'

Changing this property has no effect on other properties, and therefore changes the overall system behavior. Use chgTimeUnit to convert between time units without modifying system behavior.

Default: 'seconds'

InputName

Input channel names. Set InputName to a string for single-input model. For a multiinput model, set InputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign input names for multi-input models. For example, if **sys** is a two-input model, enter:

```
sys.InputName = 'controls';
```

The input names automatically expand to { 'controls(1) '; 'controls(2) '}.

You can use the shorthand notation u to refer to the InputName property. For example, sys.u is equivalent to sys.InputName.

Input channel names have several uses, including:

- · Identifying channels on model display and plots
- Extracting subsystems of MIMO systems
- Specifying connection points when interconnecting models

Default: Empty string ' ' for all input channels

InputUnit

Input channel units. Use InputUnit to keep track of input signal units. For a singleinput model, set InputUnit to a string. For a multi-input model, set InputUnit to a cell array of strings. InputUnit has no effect on system behavior. **Default:** Empty string ' ' for all input channels

InputGroup

Input channel groups. The InputGroup property lets you assign the input channels of MIMO systems into groups and refer to each group by name. Specify input groups as a structure. In this structure, field names are the group names, and field values are the input channels belonging to each group. For example:

```
sys.InputGroup.controls = [1 2];
sys.InputGroup.noise = [3 5];
```

creates input groups named controls and noise that include input channels 1, 2 and 3, 5, respectively. You can then extract the subsystem from the controls inputs to all outputs using:

sys(:,'controls')

Default: Struct with no fields

OutputName

Output channel names. Set OutputName to a string for single-output model. For a multioutput model, set OutputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign output names for multi-output models. For example, if **sys** is a two-output model, enter:

```
sys.OutputName = 'measurements';
```

The output names automatically expand to { 'measurements(1) '; 'measurements(2) ' }.

You can use the shorthand notation y to refer to the OutputName property. For example, sys.y is equivalent to sys.OutputName.

Output channel names have several uses, including:

- Identifying channels on model display and plots
- · Extracting subsystems of MIMO systems
- · Specifying connection points when interconnecting models

Default: Empty string ' ' for all output channels

OutputUnit

Output channel units. Use OutputUnit to keep track of output signal units. For a single-output model, set OutputUnit to a string. For a multi-output model, set OutputUnit to a cell array of strings. OutputUnit has no effect on system behavior.

Default: Empty string ' ' for all output channels

OutputGroup

Output channel groups. The OutputGroup property lets you assign the output channels of MIMO systems into groups and refer to each group by name. Specify output groups as a structure. In this structure, field names are the group names, and field values are the output channels belonging to each group. For example:

sys.OutputGroup.temperature = [1]; sys.InputGroup.measurement = [3 5];

creates output groups named temperature and measurement that include output channels 1, and 3, 5, respectively. You can then extract the subsystem from all inputs to the measurement outputs using:

```
sys('measurement',:)
```

Default: Struct with no fields

Name

System name. Set Name to a string to label the system.

Default: ' '

Notes

Any text that you want to associate with the system. Set **Notes** to a string or a cell array of strings.

Default: {}

UserData

Any type of data you want to associate with system. Set ${\tt UserData}$ to any MATLAB data type.

Default: []

SamplingGrid

Sampling grid for model arrays, specified as a data structure.

For model arrays that are derived by sampling one or more independent variables, this property tracks the variable values associated with each model in the array. This information appears when you display or plot the model array. Use this information to trace results back to the independent variables.

Set the field names of the data structure to the names of the sampling variables. Set the field values to the sampled variable values associated with each model in the array. All sampling variables should be numeric and scalar valued, and all arrays of sampled values should match the dimensions of the model array.

For example, suppose you create a 11-by-1 array of linear models, sysarr, by taking snapshots of a linear time-varying system at times t = 0:10. The following code stores the time samples with the linear models.

```
sysarr.SamplingGrid = struct('time',0:10)
```

Similarly, suppose you create a 6-by-9 model array, M, by independently sampling two variables, zeta and w. The following code attaches the (zeta,w) values to M.

```
[zeta,w] = ndgrid(<6 values of zeta>,<9 values of w>)
M.SamplingGrid = struct('zeta',zeta,'w',w)
```

When you display M, each entry in the array includes the corresponding zeta and w values.

М

```
s^2 + 3.5 s + 25
```

For model arrays generated by linearizing a Simulink model at multiple parameter values or operating points, the software populates SamplingGrid automatically with the variable values that correspond to each entry in the array. For example, the Simulink Control Design commands linearize and slLinearizer populate SamplingGrid in this way.

Default: []

Examples

Tunable Low-Pass Filter

This example shows how to create the low-pass filter F = a/(s + a) with one tunable parameter *a*.

You cannot use ltiblock.tf to represent F, because the numerator and denominator coefficients of an ltiblock.tf block are independent. Instead, construct F using the tunable real parameter object realp.

1 Create a tunable real parameter.

a = realp('a',10);

The realp object **a** is a tunable parameter with initial value 10.

2 Use tf to create the tunable filter F:

F = tf(a,[1 a]);

F is a genss object which has the tunable parameter a in its Blocks property. You can connect F with other tunable or numeric models to create more complex models of control systems. For an example, see "Control System with Tunable Components".

State-Space Model With Both Fixed and Tunable Parameters

This example shows how to create a state-space (genss) model having both fixed and tunable parameters.

Create a state-space model having the following state-space matrices:

$$A = \begin{bmatrix} 1 & a+b \\ 0 & ab \end{bmatrix}, \quad B = \begin{bmatrix} -3.0 \\ 1.5 \end{bmatrix}, \quad C = \begin{bmatrix} 0.3 & 0 \end{bmatrix}, \quad D = 0,$$

where a and b are tunable parameters, whose initial values are -1 and 3, respectively.

1 Create the tunable parameters using realp.

a = realp('a',-1); b = realp('b',3);

2 Define a generalized matrix using algebraic expressions of **a** and **b**.

 $A = [1 \ a+b; 0 \ a*b]$

A is a generalized matrix whose Blocks property contains a and b. The initial value of A is $M = [1 \ 2; 0 \ -3]$, from the initial values of a and b.

3 Create the fixed-value state-space matrices.

```
B = [-3.0;1.5];
C = [0.3 0];
D = 0;
```

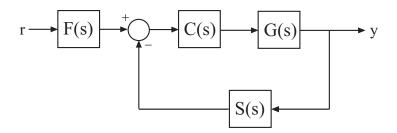
4 Use **ss** to create the state-space model.

sys = ss(A,B,C,D)

sys is a generalized LTI model (genss) with tunable parameters a and b.

Control System With Both Numeric and Tunable Components

This example shows how to create a tunable model of the control system in the following illustration.



The plant response $G(s) = 1/(s + 1)^2$. The model of sensor dynamics is S(s) = 5/(s + 4). The controller *C* is a tunable PID controller, and the prefilter F = a/(s + a) is a low-pass filter with one tunable parameter, *a*.

Create models representing the plant and sensor dynamics.

Because the plant and sensor dynamics are fixed, represent them using numeric LTI models zpk and tf.

G = zpk([],[-1,-1],1); S = tf(5,[1 4]);

Create a tunable representation of the controller C.

C is a ltiblock.pid object, which is a Control Design Block with a predefined proportional-integral-derivative (PID) structure.

Create a model of the filter F = a/(s + a) with one tunable parameter.

a = realp('a',10);
F = tf(a,[1 a]);

a is a realp (real tunable parameter) object with initial value 10. Using a as a coefficient in tf creates the tunable genss model object F.

Connect the models together to construct a model of the closed-loop response from r to y.

T = feedback(G*C,S)*F

T is a **genss** model object. In contrast to an aggregate model formed by connecting only Numeric LTI models, T keeps track of the tunable elements of the control system. The tunable elements are stored in the **Blocks** property of the **genss** model object. Display the tunable elements of T.

T.Blocks

```
ans =
C: [1x1 ltiblock.pid]
a: [1x1 realp]
```

If you have Robust Control Toolbox software, you can use tuning commands such as systume to tune the free parameters of T to meet design requirements you specify.

More About

Tips

- You can manipulate genss models as ordinary ss models. Analysis commands such as bode and step evaluate the model by replacing each tunable parameter with its current value.
- "Models with Tunable Coefficients"
- "Dynamic System Models"
- "Control Design Blocks"

See Also

realp | genmat | genfrd | tf | ss | getValue | ltiblock.pid | feedback |
connect

Introduced in R2011a

get

Access model property values

Syntax

```
Value = get(sys,'PropertyName')
Struct = get(sys)
```

Description

Value = get(sys, 'PropertyName') returns the current value of the property PropertyName of the model object sys. The string 'PropertyName' can be the full property name (for example, 'UserData') or any unambiguous case-insensitive abbreviation (for example, 'User'). See reference pages for the individual model object types for a list of properties available for that model.

Struct = get(sys) converts the TF, SS, or ZPK object sys into a standard MATLAB structure with the property names as field names and the property values as field values.

Without left-side argument,

get(sys)

displays all properties of sys and their values.

Examples

Consider the discrete-time SISO transfer function defined by

```
h = tf(1,[1 2],0.1,'inputname','voltage','user','hello')
```

You can display all properties of ${\sf h}$ with

get(h)

num: {[0 1]} den: {[1 2]}

```
ioDelay: 0
Variable: 'z'
Ts: 0.1
InputDelay: 0
OutputDelay: 0
InputName: {'voltage'}
OutputName: {''}
InputGroup: [1x1 struct]
OutputGroup: [1x1 struct]
Name: ''
Notes: {}
UserData: 'hello'
```

or query only about the numerator and sample time values by

```
get(h, 'num')
ans =
    [1x2 double]
and
get(h, 'ts')
ans =
```

Because the numerator data (num property) is always stored as a cell array, the first command evaluates to a cell array containing the row vector $\begin{bmatrix} 0 & 1 \end{bmatrix}$.

More About

0.1000

Tips

An alternative to the syntax

Value = get(sys,'PropertyName')

is the structure-like referencing

Value = sys.PropertyName

For example,

sys.Ts sys.a sys.user

return the values of the sample time, A matrix, and UserData property of the (state-space) model sys.

See Also

set | ssdata | tfdata | zpkdata | frdata | idssdata | polydata

Introduced before R2006a

getBlockValue

Current value of Control Design Block in Generalized Model

Syntax

```
val = getBlockValue(M,blockname)
[val1,val2,...] = getBlockValue(M,blockname1,blockname2,...)
S = getBlockValue(M)
```

Description

val = getBlockValue(M,blockname) returns the current value of the Control
Design Block blockname in the Generalized Model M. (For uncertain blocks, the "current
value" is the nominal value of the block.)

[val1,val2,...] = getBlockValue(M,blockname1,blockname2,...) returns the values of the specified Control Design Blocks.

S = getBlockValue(M) returns the values of all Control Design Blocks of the generalized model in a structure. This syntax lets you transfer the block values from one generalized model to another model that uses the same Control Design Blocks, as follows:

```
S = getBlockValue(M1);
setBlockValue(M2,S);
```

Input Arguments

М

Generalized LTI (genss) model or generalized matrix (genmat).

blockname

Name of the Control Design Block in the model M whose current value is evaluated.

To get a list of the Control Design Blocks in M, enter M.Blocks.

Output Arguments

val

Numerical LTI model or numerical value, equal to the current value of the Control Design Block blockname.

S

Current values of all Control Design Blocks in M, returned as a structure. The names of the fields in S are the names of the blocks in M. The values of the fields are numerical LTI models or numerical values equal to the current values of the corresponding Control Design Blocks.

Examples

Get Current Values of Single Blocks

Create a tunable **genss** model, and evaluate the current value of the Control Design Blocks of the model.

Typically, you use getBlockValue to retrieve the tuned values of control design blocks after tuning the genss model using a tuning command such as systume. For this example, create the model and retrieve the initial block values.

Cval is a numeric pid controller object.

```
aval = getBlockValue(T,'a')
aval =
10
```

aval is a numeric scalar, because a is a real scalar parameter.

Get All Current Values as Structure

Using the **genss** model of the previous example, get the current values of all blocks in the model.

```
G = zpk([],[-1,-1],1);
C = ltiblock.pid('C','PID');
a = realp('a',10);
F = tf(a,[1 a]);
T = feedback(G*C,1)*F;
S = getBlockValue(T)
S =
C: [1x1 pid]
a: 10
```

More About

- Generalized Model
- Control Design Block

See Also

getValue | setBlockValue | showBlockValue

Introduced in R2011b

getCompSensitivity

Complementary sensitivity function from generalized model of control system

Syntax

```
T = getCompSensitivity(CL,location)
```

T = getSensitivity(CL,location,opening)

Description

T = getCompSensitivity(CL, location) returns the complementary sensitivity measured at the specified location for a generalized model of a control system.

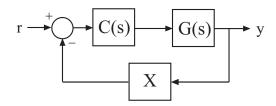
T = getSensitivity(CL, location, opening) specifies additional loop openings for the complementary sensitivity function calculation. Use an opening, for example, to calculate the complementary sensitivity function of an inner loop, with the outer loop open.

If **opening** and **location** list the same point, the software opens the loop after adding the disturbance signal at the point.

Examples

Complementary Sensitivity Function at a Location

Compute the complementary sensitivity at the plant output, X.



Create a model of the system by specifying and connecting a numeric LTI plant model G, a tunable controller C, and the AnalysisPoint block X. Use the AnalysisPoint block

to mark the location where you assess the complementary sensitivity (plant output in this example).

```
G = tf([1],[1 5]);
C = ltiblock.pid('C','p');
C.Kp.Value = 3;
X = AnalysisPoint('X');
CL = feedback(G*C,X);
```

 CL is a genss model that represents the closed-loop response of the control system from r to y. The model contains the AnalysisPoint block, X, that identifies the analysis-point location.

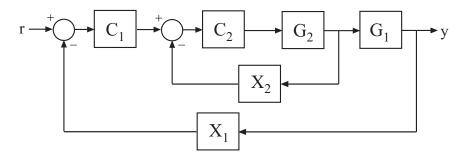
Calculate the complementary sensitivity, T, at X.

```
T = getCompSensitivity(CL,'X');
tf(T)
ans =
From input "X" to output "X":
    -3
    ----
s + 8
```

Continuous-time transfer function.

Specify Additional Loop Opening for Complementary Sensitivity Function Calculation

Calculate the inner-loop sensitivity at the output of G2, with the outer loop open.



Create a model of the system by specifying and connecting the numeric plant models, tunable controllers, and AnalysisPoint blocks. G1 and G2 are plant models, C1 and C2

are tunable controllers, and X1 and X2 are AnalysisPoint blocks that mark potential loop-opening locations.

```
G1 = tf(10,[1 10]);
G2 = tf([1 2],[1 0.2 10]);
C1 = ltiblock.pid('C','pi');
C2 = ltiblock.gain('G',1);
X1 = AnalysisPoint('X1');
X2 = AnalysisPoint('X2');
CL = feedback(G1*feedback(G2*C2,X2)*C1,X1);
```

Calculate the complementary sensitivity, T, at X2, with the outer loop open at X1.

Input Arguments

CL - Model of control system

generalized state-space model

Model of a control system, specified as a Generalized State-Space Model (genss).

Locations at which you can perform sensitivity analysis or open loops are marked by AnalysisPoint blocks in CL. Use getPoints(CL) to get the list of such locations.

location – **Location** string | cell array of strings

Location at which you calculate the complementary sensitivity function, specified as a string or cell array of strings. To extract the complementary sensitivity function at multiple locations, use a cell array of strings. Each string in location must match an analysis point in CL. Analysis points are marked using AnalysisPoint blocks. Use getPoints(CL) to get the list of available analysis points in CL.

Example: 'u' or $\{'u', 'y'\}$

opening — Additional loop opening

string | cell array of strings

Additional loop opening used to calculate the complementary sensitivity function, specified as a string or cell array of strings. To open the loop at multiple locations, use a cell array of strings.

Each string in opening must match an analysis point in CL. Analysis points are marked using AnalysisPoint blocks. Use getPoints(CL) to get the list of available analysis points in CL.

Use an opening, for example, to calculate the complementary sensitivity function of an inner loop, with the outer loop open.

If **opening** and **location** list the same point, the software opens the loop after adding the disturbance signal at the point.

Example: 'y_outer' or {'y_outer', 'y_outer2'}

Output Arguments

T – Complementary sensitivity function

generalized state-space model

Complementary sensitivity function of the control system, T, measured at location, returned as a Generalized State-Space Model (genss).

- If location specifies a single analysis point, then T is a SISO genss model.
- If location is a string specifying a vector signal, or a cell array identifying multiple analysis points, then T is a MIMO genss model.

More About

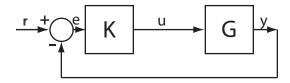
Complementary Sensitivity

The complementary sensitivity function, T, at a point is the closed-loop transfer function around the feedback loop measured at the specified location. It is related to the open-loop transfer function, L, and the sensitivity function, S, at the same point as follows:

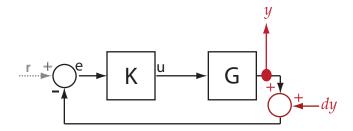
$$T = \frac{L}{1-L} = S - 1.$$

Use getLoopTransfer and getSensitivity to compute L and S.

Consider the following model:



The complementary sensitivity, T, at y is defined as the transfer function from dy to y.



Observe that, in contrast to the sensitivity function, the disturbance, dy, is added *after* the measurement, y.

$$y = -GK(y + dy)$$

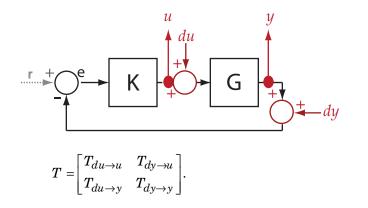
$$\rightarrow y = -GKy - GKdy$$

$$\rightarrow (I + GK)y = -GKdy$$

$$\rightarrow y = \underbrace{-(I + GK)^{-1}GK}_{T} dy.$$

Here, *I* is an identity matrix of the same size as *GK*. The complementary sensitivity transfer function at y is equal to -1 times the closed-loop transfer function from r to y.

Complementary sensitivity at multiple locations, for example, u and y, is defined as the MIMO transfer function from the disturbances to measurements:



See Also

| AnalysisPoint | genss | getCompSensitivity | getIOTransfer | getLoopTransfer | getPoints | getSensitivity | getValue | systume

Introduced in R2014a

getComponents

Extract SISO control components from a 2-DOF PID controller

Syntax

[C,X] = getComponents(C2,looptype)

Description

[C,X] = getComponents(C2,looptype) decomposes the 2-DOF PID controller C2 into two SISO control components. One of the control components, C, is a 1-DOF PID controller. The other, X, is a SISO dynamic system. When C and X are connected in the loop structure specified by looptype, the resulting closed-loop system is equivalent to the 2-DOF control loop.

For more information about 2-DOF PID control architectures, see "Two-Degree-of-Freedom PID Controllers".

Examples

Extract SISO Components from 2-DOF PID Controller

Decompose a 2-DOF PID controller into SISO control components, using each of the feedforward, feedback, and filter configurations.

To start, obtain a 2-DOF PID controller. For this example, create a plant model and tune a 2-DOF PID controller for it.

```
G = tf(1,[1 0.5 0.1]);
C2 = pidtune(G,'pidf2',1.5)
C2 =
u = Kp (b*r-y) + Ki --- (r-y) + Kd ---- (c*r-y)
s Tf*s+1
```

with Kp = 1.12, Ki = 0.23, Kd = 1.3, Tf = 0.122, b = 0.664, c = 0.0136 Continuous-time 2-DOF PIDF controller in parallel form.

C2 is a pid2 controller object, with two inputs and one output. Decompose C2 into SISO control components using the feedforward configuration.

As the display shows, this command returns the SISO PID controller Cff as a pid object. The feedforward compensator X is returned as a zpk object.

Decompose C2 using the feedback configuration. In this case as well, Cfb is a pid controller object, and the feedback compensator X is a zpk model.

[Cfb,Xfb] = getComponents(C2, 'feedback');

Decompose C2 using the filter configuration. Again, the components are a SISO pid controller and a zpk model representing the prefilter.

[Cfr,Xfr] = getComponents(C2, 'filter');

"Decompose a 2-DOF PID Controller into SISO Components"

Input Arguments

C2 - 2-DOF PID controller

pid2 object | pidstd2 object

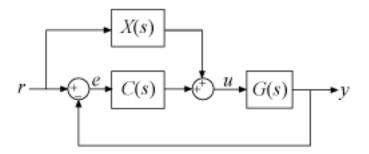
2-DOF PID controller to decompose, specified as a pid2 or pidstd2 controller object.

looptype - Loop structure

```
'feedforward' (default) | 'feedback' | 'filter'
```

Loop structure for decomposing the 2-DOF controller, specified as 'feedforward', 'feedback', or 'filter'. These correspond to the following control decompositions and architectures:

• 'feedforward' — C is a conventional SISO PID controller that takes the error signal as its input. X is a feedforward controller, as shown:



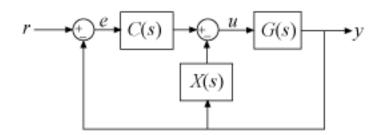
If C2 is a continuous-time, parallel-form controller, then the components are given by:

$$\begin{split} C(s) &= K_p + \frac{K_i}{s} + \frac{K_d s}{T_f s + 1}, \\ X(s) &= (b-1)K_p + \frac{(c-1)K_d s}{T_f s + 1}. \end{split}$$

The following command constructs the closed-loop system from r to y for the feedforward configuration.

 $T = G^{*}(C+X)^{*}feedback(1,G^{*}C);$

• 'feedback' — C is a conventional SISO PID controller that takes the error signal as its input. X is a feedback controller from *y* to *u*, as shown:

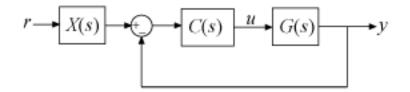


If C2 is a continuous-time, parallel-form controller, then the components are given by:

$$\begin{split} C(s) &= bK_p + \frac{K_i}{s} + \frac{cK_ds}{T_fs+1}, \\ X(s) &= (1-b)K_p + \frac{(1-c)K_ds}{T_fs+1}. \end{split}$$

The following command constructs the closed-loop system from r to y for the feedback configuration.

- T = G*C*feedback(1,G*(C+X));
- 'filter' X is a prefilter on the reference signal. C is a conventional SISO PID controller that takes as its input the difference between the filtered reference and the output, as shown:



If C2 is a continuous-time, parallel-form controller, then the components are given by:

$$\begin{split} C(s) &= K_p + \frac{K_i}{s} + \frac{K_d s}{T_f s + 1}, \\ X(s) &= \frac{\left(bK_p T_f + cK_d\right) s^2 + \left(bK_p + K_i T_f\right) s + K_i}{\left(K_p T_f + K_d\right) s^2 + \left(K_p + K_i T_f\right) s + K_i}. \end{split}$$

The following command constructs the closed-loop system from r to y for the filter configuration.

T = X*feedback(G*C,1);

The formulas shown above pertain to continuous-time, parallel-form controllers. Standard-form controllers and controllers in discrete time can be decomposed into analogous configurations. The getComponents command works on all 2-DOF PID controller objects.

Output Arguments

C - SISO PID controller

pid object | pidstd object

SISO PID controller, returned as a pid or pidstd controller object. The form of C corresponds to the form of the input controller C2. For example, if C2 is a standard-form pidstd2 controller, then C is a pidstd object.

The precise functional form of C depends on the loop structure you specify with the looptype argument, as described in "Input Arguments" on page 1-263.

X - SISO control component

zpk model

SISO control component, specified as a zero-pole-gain (zpk) model. The precise functional form of X depends on the loop structure you specify with the looptype argument, as described in "Input Arguments" on page 1-263.

More About

• "Two-Degree-of-Freedom PID Controllers"

See Also

make1DOF | make2DOF | pid2 | pidstd2

Introduced in R2015b

getDelayModel

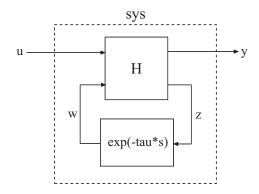
State-space representation of internal delays

Syntax

```
[H,tau] = getDelayModel(sys)
[A,B1,B2,C1,C2,D11,D12,D21,D22,E,tau] = getDelayModel(sys)
```

Description

[H,tau] = getDelayModel(sys) decomposes a state-space model sys with internal delays into a delay-free state-space model, H, and a vector of internal delays, tau. The relationship among sys, H, and tau is shown in the following diagram.



[A,B1,B2,C1,C2,D11,D12,D21,D22,E,tau] = getDelayModel(sys) returns the set of state-space matrices and internal delay vector, tau, that explicitly describe the state-space model sys. These state-space matrices are defined by the state-space equations:

• Continuous-time sys:

$$E \frac{dx(t)}{dt} = Ax(t) + B_1u(t) + B_2w(t)$$

$$y(t) = C_1x(t) + D_{11}u(t) + D_{12}w(t)$$

$$z(t) = C_2x(t) + D_{21}u(t) + D_{22}w(t)$$

$$w(t) = z(t - \tau)$$

• Discrete-time sys:

$$\begin{aligned} Ex[k+1] &= Ax[k] + B_1u[k] + B_2w[k] \\ y[k] &= C_1x[k] + D_{11}u[k] + D_{12}w[k] \\ z[k] &= C_2x[k] + D_{21}u[k] + D_{22}w[k] \\ w[k] &= z[k-\tau] \end{aligned}$$

Input Arguments

sys

Any state-space (ss) model.

Output Arguments

Н

Delay-free state-space model (ss). H results from decomposing sys into a delay-free component and a component exp(-tau*s) that represents all internal delays.

If sys has no internal delays, H is equal to sys.

tau

Vector of internal delays of sys, expressed in the time units of sys. The vector tau results from decomposing sys into a delay-free state-space model H and a component exp(-tau*s) that represents all internal delays.

If sys has no internal delays, tau is empty.

A, B1, B2, C1, C2, D11, D12, D21, D22, E

Set of state-space matrices that, with the internal delay vector tau, explicitly describe the state-space model sys.

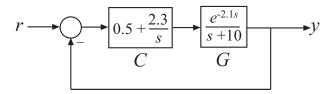
For explicit state-space models (E = I, or sys.e = []), the output E = [].

If sys has no internal delays, the outputs B2, C2, D12, D21, and D22 are all empty ([]).

Examples

Get Delay-Free State-Space Model and Internal Delay

Decompose the following closed-loop system with internal delay into a delay-free component and a component representing the internal delay.



Create the closed-loop model sys from r to y.

```
G = tf(1,[1 10],'InputDelay',2.1);
C = pid(0.5,2.3);
sys = feedback(C*G,1);
```

sys is a state-space (ss) model with an internal delay arising from the feedback loop.

Decompose sys into a delay-free state-space model and the value of the internal delay.

```
[H,tau] = getDelayModel(sys);
```

More About

• "Internal Delays"

See Also setDelayModel Introduced in R2006a

getGainCrossover

Crossover frequencies for specified gain

Syntax

```
wc = getGainCrossover(sys,gain)
```

Description

wc = getGainCrossover(sys,gain) returns the vector wc of frequencies at which the frequency response of the dynamic system model, sys, has principal gain of gain. For SISO systems, the principal gain is the frequency response. For MIMO models, the principal gain is the largest singular value of sys.

Examples

Unity Gain Crossover

Find the 0dB crossover of a single-loop control system with plant

$$G(s) = \frac{1}{\left(s+1\right)^3}$$

and PI controller

$$C(s) = 1.14 + \frac{0.454}{s}.$$

G = zpk([],[-1,-1,-1],1);
C = pid(1.14,0.454);
sys = G*C;
wc = getGainCrossover(sys,1)
wc =

0.5214

The 0 dB crossovers are the frequencies at which the open-loop response sys = G*C has unity gain. Because this system only crosses unity gain once, getGainCrossover returns a single value.

Notch Filter Stopband

Find the 20 dB stopband of

 $sys = \frac{s^2 + 0.05s + 100}{s^2 + 5s + 100}.$

sys is a notch filter centered at 10 rad/s.

The db2mag command converts the gain value of -20 dB to absolute units. The getGainCrossover command returns the two frequencies that define the stopband.

Input Arguments

sys — Input dynamic system

dynamic system model

Input dynamic system, specified as any SISO or MIMO dynamic system model.

gain — Input gain

positive real scalar

Input gain in absolute units, specified as a positive real scalar.

• If sys is a SISO model, the gain is the frequency response magnitude of sys.

• If sys is a MIMO model, gain means the largest singular value of sys.

Output Arguments

wc - Crossover frequencies

column vector

Crossover frequencies, returned as a column vector. This vector lists the frequencies at which the gain or largest singular value of **sys** is **gain**.

More About

Algorithms

getGainCrossover computes gain crossover frequencies using structure-preserving eigensolvers from the SLICOT library. For more information about the SLICOT library, see http://slicot.org.

• "Dynamic System Models"

See Also

bandwidth | bode | freqresp | getPeakGain | sigma

Introduced in R2012a

getlOTransfer

Closed-loop transfer function from generalized model of control system

Syntax

```
H = getIOTransfer(T,in,out)
H = getIOTransfer(T,in,out,openings)
```

Description

H = getIOTransfer(T, in, out) returns the transfer function from specified inputs to specified outputs of a control system, computed from a closed-loop generalized model of the control system.

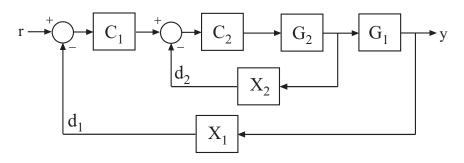
H = getIOTransfer(T, in, out, openings) returns the transfer function calculated with one or more loops open.

Examples

Closed-Loop Responses of Control System Model

Analyze responses of a control system by using getIOTransfer to compute responses between various inputs and outputs of a closed-loop model of the system.

Consider the following control system.



Create a genss model of the system by specifying and connecting the numeric plant models G1 and G2, the tunable controllers C1, and the AnalysisPoint blocks X1 and X2 that mark potential loop-opening or signal injection sites.

```
G1 = tf(10,[1 10]);
G2 = tf([1 2],[1 0.2 10]);
C1 = ltiblock.pid('C','pi');
C2 = ltiblock.gain('G',1);
X1 = AnalysisPoint('X1');
X2 = AnalysisPoint('X2');
T = feedback(G1*feedback(G2*C2,X2)*C1,X1);
T.InputName = 'r';
T.OutputName = 'y';
```

If you tuned the free parameters of this model (for example, using the Robust Control Toolbox tuning command systume), you might want to analyze the tuned system performance by examining various system responses.

For example, examine the response at the output, y, to a disturbance injected at the point d_1 .

```
H1 = getIOTransfer(T, 'X1', 'y');
```

H1 represents the closed-loop response of the control system to a disturbance injected at the implicit input associated with the AnalysisPoint block X1, which is the location of d_1 :



H1 is a genss model that includes the tunable blocks of T. If you have tuned the free parameters of T, H1 allows you to validate the disturbance response of your tuned system. For example, you can use analysis commands such as bodeplot or stepplot to analyze H1. You can also use getValue to obtain the current value of H1, in which all the tunable blocks are evaluated to their current numeric values.

Similarly, examine the response at the output to a disturbance injected at the point d_2 .

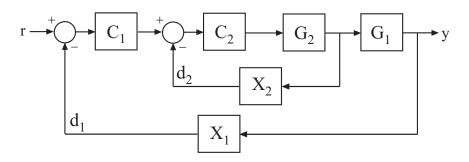
```
H2 = getIOTransfer(T, X2', y');
```

You can also generate a two-input, one-output model representing the response of the control system to simultaneous disturbances at both d_1 and d_2 . To do so, provide getI0Transfer with a cell array that specifies the multiple input locations.

```
H = getIOTransfer(T,{'X1','X2'},'y');
```

Responses with Some Loops Open and Others Closed

Compute the response from r to y of the following cascaded control system, with the inner loop open, and the outer loop closed.



Create a genss model of the system by specifying and connecting the numeric plant models G1 and G2, the tunable controllers C1, and the AnalysisPoint blocks X1 and X2 that mark potential loop-opening or signal injection sites.

```
G1 = tf(10,[1 10]);
G2 = tf([1 2],[1 0.2 10]);
C1 = ltiblock.pid('C','pi');
C2 = ltiblock.gain('G',1);
X1 = AnalysisPoint('X1');
X2 = AnalysisPoint('X2');
T = feedback(G1*feedback(G2*C2,X2)*C1,X1);T.InputName = 'r';
T.OutputName = 'y';
```

If you tuned the free parameters of this model (for example, using the Robust Control Toolbox tuning command systume), you might want to analyze the tuned system performance by examining various system responses.

For example, compute the response of the system with the inner loop open, and the outer loop closed.

```
H = getIOTransfer(T, 'r', 'y', 'X2');
```

By default, the loops are closed at the analysis points X1 and X2. Specifying 'X2' for the **openings** argument causes **getIOTransfer** to open the loop at X2 for the purposes of computing the requested transfer from r to y. The switch at X1 remains closed for this computation.

Input Arguments

T - Model of control system

generalized state-space model

Model of a control system, specified as a Generalized State-Space (genss) Model.

in — Input to extracted transfer function

string | cell array of strings

Input to extracted transfer function, specified as a string or cell array of strings. To extract a multiple-input transfer function from the control system, use a cell array of strings. Each string in in must match either:

- An input of the control system model T (in other words, a string contained in T.InputName).
- An analysis point in T, corresponding to a channel of an AnalysisPoint block in T. Use getpoints(T) to get a full list of available analysis points in T.

When you specify an analysis point as an input in, getIOTransfer uses the input implicitly associated with the AnalysisPoint channel, arranged as follows.



This input signal models a disturbance entering at the output of the switch.

If an analysis point has the same name as an input of T, then ${\tt getIOTransfer}$ uses the input of T.

```
Example: { 'r', 'X1' }
```

out - Output of extracted transfer function

string | cell array of strings

Output of extracted transfer function, specified as a string or cell array of strings. To extract a multiple-output transfer function from the control system, use a cell array of strings. Each string in **out** must match either:

- An output of the control system model T (in other words, a string contained in T.OutputName).
- An analysis point in T, corresponding to a channel of an AnalysisPoint block in T. Use getPoints(T) to get a full list of available analysis points in T.

When you specify an analysis point as an output **out**, **getIOTransfer** uses the output implicitly associated with the **AnalysisPoint** channel, arranged as follows.



If an analysis point has the same name as an output of T, then getIOTransfer uses the output of T.

Example: { 'y', 'X2' }

openings — Locations for opening feedback loops

string | cell array of strings

Locations for opening feedback loops for computation of the response from in to out, specified as string or cell array of strings that identify analysis points in T. Analysis points are marked by AnalysisPoint blocks in T. Use getPoints(T) to get a full list of available loop-opening sites in T.

Use **openings** when you want to compute the response from **in** to **out** with some loops in the control system open. For example, in a cascaded loop configuration, you can calculate the response from the system input to the system output with the inner loop open.

Output Arguments

H - Closed-loop transfer function

generalized state-space model

Closed-loop transfer function of the control system ${\tt T}$ from in to out, returned as a Generalized State-Space (genss) model.

- If both in and out specify a single signal, then T is a SISO genss model.
- If in or out identifies multiple signals, then T is a MIMO genss model.

More About

Tips

• You can use getIOTransfer to extract various subsystem responses, given a generalized model of the overall control system. This is useful for validating responses of a control system that you tune with the Robust Control Toolbox tuning command systume.

For example, in addition to evaluating the overall response of a tuned control system from inputs to outputs, you can use getIOTransfer to extract the transfer function from a disturbance input to a system output. Evaluate the responses of that transfer function (such as with step or bode) to confirm that the tuned system meets your disturbance rejection requirements.

• getIOTransfer is the genss equivalent to the Simulink Control Design getIOTransfer command, which works with the slTuner and slLinearizer interfaces. Use the Simulink Control Design command when your control system is modeled in Simulink.

See Also

| AnalysisPoint | genss | getIOTransfer | getLoopTransfer | getPoints | systume

Introduced in R2012b

getLFTModel

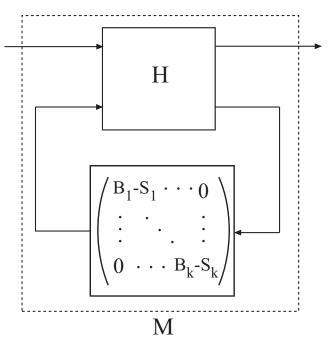
Decompose generalized LTI model

Syntax

[H,B,S] = getLFTModel(M)

Description

[H,B,S] = getLFTModel(M) extracts the components H, B, and S that make up the Generalized matrix or Generalized LTI model M. The model M decomposes into H, B, and S. These components are related to M as shown in the following illustration.



The cell array B contains the Control Design Blocks of M. The component H is a numeric matrix, ss model, or frd model that describes the fixed portion of M and the

interconnections between the blocks of B. The matrix S = blkdiag(S1,...,Sk) contains numerical offsets that ensure that the interconnection is well-defined when the current (nominal) value of M is finite.

You can recombine H, B, and S into M using lft, as follows:

```
M = lft(H,blkdiag(B{:})-S);
```

Input Arguments

М

Generalized LTI model (genss or genfrd) or Generalized matrix (genmat).

Output Arguments

H

Matrix, ss model, or frd model describing the numeric portion of M and how it the numeric portion is connected to the Control Design Blocks of M.

В

Cell array of Control Design Blocks (for example, realp or ltiblock.ss) of M.

S

Matrix of offset values. The software might introduce offsets when you build a Generalized model to ensure that H is finite when the current (nominal) value of M is finite.

More About

Tips

• getLFTModel gives you access to the internal representation of Generalized LTI models and Generalized Matrices. For more information about this representation, see "Internal Structure of Generalized Models".

- "Generalized Matrices"
- "Generalized and Uncertain LTI Models"
- "Models with Tunable Coefficients"
- "Internal Structure of Generalized Models"

See Also

genfrd | genss | genmat | lft | getValue | nblocks

Introduced in R2011a

getLoopTransfer

Open-loop transfer function of control system

Syntax

```
L = getLoopTransfer(T,Locations)
```

- L = getLoopTransfer(T,Locations,sign)
- L = getLoopTransfer(T,Locations,sign,openings)

Description

L = getLoopTransfer(T,Locations) returns the point-to-point open-loop transfer function of a control system measured at specified analysis points. The point-to-point open-loop transfer function is the open-loop response obtained by injecting signals at the specified locations and measuring the return signals at the same locations.

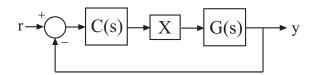
L = getLoopTransfer(T,Locations,sign) specifies the feedback sign for calculating the open-loop response. The relationship between the closed-loop response T and the open-loop response L is T = feedback(L,1,sign).

L = getLoopTransfer(T,Locations,sign,openings) specifies additional loopopening locations to open for computing the open-loop response at Locations.

Examples

Open-Loop Transfer Function at Analysis Point

Compute the open-loop response of the following control system model at an analysis point specified by an AnalysisPoint block, X.



Create a model of the system by specifying and connecting a numeric LTI plant model G, a tunable controller C, and the AnalysisPoint block X.

```
G = tf([1 2],[1 0.2 10]);
C = ltiblock.pid('C','pi');
X = AnalysisPoint('X');
T = feedback(G*X*C,1);
```

T is a genss model that represents the closed-loop response of the control system from r to y. The model contains the AnalysisPoint block X that identifies the potential loop-opening location.

Calculate the open-loop point-to-point loop transfer at the location X.

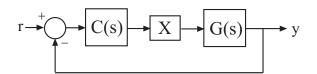
L = getLoopTransfer(T, 'X');

This command computes the positive-feedback transfer function you would obtain by opening the loop at X, injecting a signal into G, and measuring the resulting response at the output of C. By default, getLoopTransfer computes the positive feedback transfer function. In this example, the positive feedback transfer function is L(s) = -G(s)C(s)

The output L is a genss model that includes the tunable block C. You can use getValue to obtain the current value of L, in which all the tunable blocks of L are evaluated to their current numeric value.

Negative-Feedback Open-Loop Transfer Function

Compute the negative-feedback open-loop transfer of the following control system model at an analysis point specified by an AnalysisPoint block, X.



Create a model of the system by specifying and connecting a numeric LTI plant model G, a tunable controller C, and the AnalysisPoint block X.

```
G = tf([1 2],[1 0.2 10]);
C = ltiblock.pid('C','pi');
X = AnalysisPoint('X');
T = feedback(G*X*C,1);
```

T is a genss model that represents the closed-loop response of the control system from r to y. The model contains the AnalysisPoint block X that identifies the potential loop-opening location.

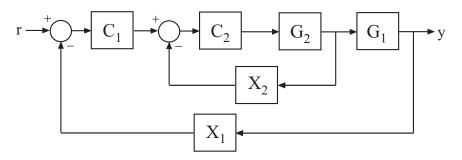
Calculate the open-loop point-to-point loop transfer at the location X.

L = getLoopTransfer(T, 'X', -1);

This command computes the open-loop transfer function from the input of G to the output of C, assuming that the loop is closed with negative feedback. That is, the relationships between L and T is given by T = feedback(L,1). In this example, the positive feedback transfer function is L(s) = G(s)C(s)

Transfer Function with Additional Loop Openings

Compute the open-loop response of the inner loop of the following cascaded control system, with the outer loop open.



Create a model of the system by specifying and connecting the numeric plant models G1 and G2, the tunable controllers C1, and the AnalysisPoint blocks X1 and X2 that mark potential loop-opening locations.

```
G1 = tf(10,[1 10]);
G2 = tf([1 2],[1 0.2 10]);
C1 = ltiblock.pid('C','pi');
C2 = ltiblock.gain('G',1);
X1 = AnalysisPoint('X1');
X2 = AnalysisPoint('X2');
T = feedback(G1*feedback(G2*C2,X2)*C1,X1);
```

Compute the negative-feedback open-loop response of the inner loop, at the location X2, with the outer loop opened at X1.

```
L = getLoopTransfer(T, 'X2', -1, 'X1');
```

By default, the loop is closed at the analysis-point location marked by the AnalysisPoint block X1. Specifying 'X1' for the openings argument causes getLoopTransfer to open the loop at X1 for the purposes of computing the requested loop transfer at X2. In this example, the negative-feedback open-loop response $L(s) = G_2(s)C_2(s)$.

Input Arguments

T - Model of control system

generalized state-space model

Model of a control system, specified as a Generalized State-Space (genss) Model. Locations at which you can open loops and perform open-loop analysis are marked by AnalysisPoint blocks in T.

Locations - Analysis-point locations

string | cell array of strings

Analysis-point locations in the control system model at which to compute the openloop point-to-point response, specified as a string or a cell array of strings that identify analysis-point locations in T.

Analysis-point locations are marked by AnalysisPoint blocks in T. An AnalysisPoint block can have single or multiple channels. The Location property of an AnalysisPoint block gives names to these feedback channels.

The name of any channel in a AnalysisPoint block in T is a valid entry for the Locations argument to getLoopTransfer. Use getPoints(T) to get a full list of available analysis points in T.

getLoopTransfer computes the open-loop response you would obtain by injecting a signal at the implicit input associated with an AnalysisPoint channel, and measuring the response at the implicit output associated with the channel. These implicit inputs and outputs are arranged as follows.



L is the open-loop transfer function from in to out.

sign — Feedback sign

+1 (default) | -1

Feedback sign, specified as +1 or -1 The feedback sign determines the sign of the open-loop transfer function.

- +1 Compute the positive-feedback loop transfer. In this case, the relationship between the closed-loop response T and the open-loop response L is T = feedback(L,1,+1).
- -1 Compute the negative-feedback loop transfer. In this case, the relationship between the closed-loop response T and the open-loop response L is T = feedback(L,1).

Choose a feedback sign that is consistent with the conventions of the analysis you intend to perform with the loop transfer function. For example, consider the following system, where T is the closed-loop transfer function from r to y.

$$r \xrightarrow{+} C(s) \xrightarrow{} X \xrightarrow{} G(s) \xrightarrow{} y$$

To compute the stability margins of this system with the margin command, which assumes negative feedback, you need to use the negative-feedback open-loop response. Therefore, you can use L = getLoopTransfer(T, 'X', -1) to obtain the negative-feedback transfer function L = GC.

openings - Additional locations for opening feedback loops

string | cell array of strings

Additional locations for opening feedback loops for computation of the open-loop response, specified as string or cell array of strings that identify analysis-point locations in T. Analysis-point locations are marked by AnalysisPoint blocks in T. Any channel name contained in the Location property of an AnalysisPoint block in T is a valid entry for openings.

Use **openings** when you want to compute the open-loop response at one analysis-point location with other loops also open at other locations. For example, in a cascaded loop

configuration, you can calculate the inner loop open-loop response with the outer loop also open. Use getPoints(T) to get a full list of available analysis-point locations in T.

Output Arguments

L - Point-to-point open-loop response

generalized state-space model

Point-to-point open-loop response of the control system T measured at the analysis points specified by Locations, returned as a Generalized State-Space (genss) Model.

- If Locations is a string specifying a single analysis point, then L is a SISO genss model. In this case, L represents the response obtained by opening the loop at Locations, injecting signals and measuring the return signals at the same location.
- If Locations is a string specifying a vector signal, or a cell array identifying multiple analysis points, then L is a MIMO genss model. In this case, L represents the open-loop MIMO response obtained by opening loops at all locations listed in Locations, injecting signals and measuring the return signals at those locations.

More About

Tips

- You can use getLoopTransfer to extract open-loop responses given a generalized model of the overall control system. This is useful, for example, for validating open-loop responses of a control system that you tune with the Robust Control Toolbox tuning command systume.
- getLoopTransfer is the genss equivalent to the Simulink Control Design command getLoopTransfer, which works with the slTuner and slLinearizer interfaces. Use the Simulink Control Design command when your control system is modeled in Simulink.

See Also

AnalysisPoint | genss | getIOTransfer | getLoopTransfer | getPoints | systune

Introduced in R2012b

getoptions

Return @PlotOptions handle or plot options property

Syntax

```
p = getoptions(h)
p = getoptions(h,propertyname)
```

Description

p = getoptions(h) returns the plot options handle associated with plot handle h. p contains all the settable options for a given response plot.

p = getoptions(h,propertyname) returns the specified options property, propertyname, for the plot with handle h. You can use this to interrogate a plot handle. For example,

```
p = getoptions(h, 'Grid')
```

returns 'On' if a grid is visible, and 'Off' when it is not.

For a list of the properties and values available for each plot type, see "Properties and Values Reference".

See Also setoptions

Introduced before R2006a

getPeakGain

Peak gain of dynamic system frequency response

Syntax

```
gpeak = getPeakGain(sys)
gpeak = getPeakGain(sys,tol)
gpeak = getPeakGain(sys,tol,fband)
[gpeak,fpeak] = getPeakGain(____)
```

Description

gpeak = getPeakGain(sys) returns the peak input/output gain in absolute units of the dynamic system model, sys.

- If sys is a SISO model, then the peak gain is the largest value of the frequency response magnitude.
- If sys is a MIMO model, then the peak gain is the largest value of the frequency response 2-norm (the largest singular value across frequency) of sys. This quantity is also called the L_{∞} norm of sys, and coincides with the H_{∞} norm for stable systems.
- If sys is a model that has tunable or uncertain parameters, getPeakGain evaluates the peak gain at the current or nominal value of sys.
- If sys is a model array, getPeakGain returns an array of the same size as sys, where gpeak(k) = getPeakGain(sys(:,:,k)).

```
gpeak = getPeakGain(sys,tol) returns the peak gain of sys with relative accuracy
tol.
```

gpeak = getPeakGain(sys,tol,fband) returns the peak gain in the frequency
interval fband.

[gpeak,fpeak] = getPeakGain(____) also returns the frequency fpeak at which the gain achieves the peak value gpeak, and can include any of the input arguments in previous syntaxes.

Examples

Peak Gain of Transfer Function

Compute the peak gain of the resonance in the transfer function

$$sys = \frac{90}{s^2 + 1.5s + 90}$$

sys = tf(90,[1,1.5,90]);
gpeak = getPeakGain(sys);

The getPeakGain command returns the peak gain in absolute units.

Peak Gain with Specified Accuracy

Compute the peak gain of the resonance in the transfer function $sys = \frac{90}{s^2 + 1.5s + 90}$.

with a relative accuracy of 0.01%.

sys = tf(90,[1,1.5,90]);
gpeak = getPeakGain(sys,0.0001);

The second argument specifies a relative accuracy of 0.0001. The getPeakGain command returns a value that is within 0.01% of the true peak gain of the transfer function.

Peak Gain Within Specified Band

Compute the peak gain of the second resonance in the transfer function

$$sys = \left(\frac{1}{s^2 + 0.2s + 1}\right) \left(\frac{100}{s^2 + s + 100}\right).$$

sys is the product of resonances at 1 rad/s and 10 rad/s.

```
sys = tf(1,[1,.2,1])*tf(100,[1,1,100]);
fband = [8,12];
gpeak = getPeakGain(sys,0.01,fband);
```

The fband argument causes getPeakGain to return the local peak gain between 8 and 12 rad/s.

Frequency of Peak Gain

Identify which of the two resonances has higher gain in the transfer function

$$sys = \left(\frac{1}{s^2 + 0.2s + 1}\right) \left(\frac{100}{s^2 + s + 100}\right).$$

sys is the product of resonances at 1 rad/s and 10 rad/s.

```
sys = tf(1,[1,.2,1])*tf(100,[1,1,100]);
[gpeak,fpeak] = getPeakGain(sys)
```

```
gpeak =
```

5.0502

fpeak =

1.0000

fpeak is the frequency corresponding to the peak gain gpeak. The peak at 1 rad/s is the overall peak gain of sys.

Input Arguments

sys - Input dynamic system

dynamic system model | model array

Input dynamic system, specified as any dynamic system model or model array. **Sys** can be SISO or MIMO.

to1 - Relative accuracy

0.01 (default) | positive real scalar

Relative accuracy of the peak gain, specified as a positive real scalar value. getPeakGain calculates gpeak such that the fractional difference between gpeak and the true peak gain of sys is no greater than tol.

fband — Frequency interval

[0, Inf] (default) | 1-by-2 vector of positive real values

Frequency interval in which to calculate the peak gain, specified as a 1-by-2 vector of positive real values. Specify fband as a row vector of the form [fmin,fmax].

Output Arguments

gpeak - Peak gain of dynamic system

scalar | array

Peak gain of the dynamic system model or model array **sys**, returned as a scalar value or an array.

- If sys is a single model, then gpeak is a scalar value.
- If sys is a model array, then gpeak is an array of the same size as sys, where gpeak(k) = getPeakGain(sys(:,:,k)).

fpeak — Frequency of peak gain

nonnegative real scalar | array of nonnegative real values

Frequency at which the gain achieves the peak value gpeak, returned as a nonnegative real scalar value or an array of nonnegative real values. The frequency is expressed in units of rad/TimeUnit, relative to the TimeUnit property of sys.

- If sys is a single model, then fpeak is a scalar.
- If sys is a model array, then fpeak is an array of the same size as sys, where fpeak(k) is the peak gain frequency of the *k*th model in the array.

More About

Algorithms

getPeakGain uses the algorithm of [1]. All eigenvalue computations are performed using structure-preserving algorithms from the SLICOT library. For more information about the SLICOT library, see http://slicot.org.

"Dynamic System Models"

References

[1] Bruisma, N.A. and M. Steinbuch, "A Fast Algorithm to Compute the H_{∞} -Norm of a Transfer Function Matrix," *System Control Letters*, 14 (1990), pp. 287-293.

See Also

bode | freqresp | getGainCrossover | sigma

Introduced in R2012a

getSensitivity

Sensitivity function from generalized model of control system

Syntax

```
S = getSensitivity(T,location)
```

```
S = getSensitivity(T,location,opening)
```

Description

S = getSensitivity(T,location) returns the sensitivity function at the specified location for a generalized model of a control system.

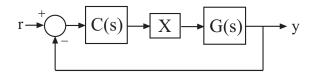
S = getSensitivity(T,location,opening) specifies additional loop openings for the sensitivity function calculation. Use an opening, for example, to calculate the sensitivity function of an inner loop, with the outer loop open.

If **opening** and **location** list the same point, the software opens the loop after measuring the signal at the point.

Examples

Sensitivity Function at a Location

Compute the sensitivity at the plant input, marked by the analysis point X.



Create a model of the system by specifying and connecting a numeric LTI plant model G, a tunable controller C, and the AnalysisPoint block X. Use the AnalysisPoint block to mark the location where you assess the sensitivity (plant input in this example).

G = tf([1],[1 5]); C = ltiblock.pid('C','p'); C.Kp.Value = 3; X = AnalysisPoint('X'); T = feedback(G*X*C,1);

T is a **genss** model that represents the closed-loop response of the control system from r to y. The model contains the AnalysisPoint block, X, that identifies the analysis point.

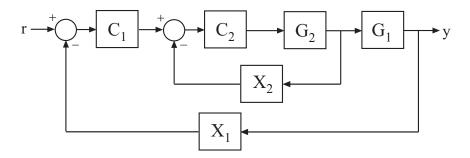
Calculate the sensitivity, S, at X.

```
S = getSensitivity(T, 'X');
tf(S)
ans =
  From input "X" to output "X":
    s + 5
    ....
    s + 8
```

Continuous-time transfer function.

Specify Additional Loop Opening for Sensitivity Function Calculation

Calculate the inner-loop sensitivity at the output of G2, with the outer loop open.



Create a model of the system by specifying and connecting the numeric plant models, tunable controllers, and AnalysisPoint blocks. G1 and G2 are plant models, C1 and C2 are tunable controllers, and X1 and X2 are AnalysisPoint blocks that mark potential loop-opening locations.

 $G1 = tf(10, [1 \ 10]);$

```
G2 = tf([1 2],[1 0.2 10]);
C1 = ltiblock.pid('C','pi');
C2 = ltiblock.gain('G',1);
X1 = AnalysisPoint('X1');
X2 = AnalysisPoint('X2');
T = feedback(G1*feedback(G2*C2,X2)*C1,X1);
```

Calculate the sensitivity, S, at X2, with the outer loop open at X1.

```
S = getSensitivity(T, 'X2', 'X1');
tf(S)
ans =
    From input "X2" to output "X2":
    s^2 + 0.2 s + 10
    ....
    s^2 + 1.2 s + 12
```

Continuous-time transfer function.

Input Arguments

T — Model of control system

generalized state-space model

Model of a control system, specified as a Generalized State-Space Model (genss).

Locations at which you can perform sensitivity analysis or open loops are marked by AnalysisPoint blocks in T. Use getPoints(T) to get the list of such locations.

location – **Location** string | cell array of strings

Location at which you calculate the sensitivity function, specified as a string or cell array of strings. To extract the sensitivity function at multiple locations, use a cell array of strings.

Each string in location must match an analysis point in T. Analysis points are marked using AnalysisPoint blocks. Use getPoints(T) to get the list of available analysis points in T.

```
Example: 'u' or { 'u', 'y' }
```

opening - Additional loop opening

string | cell array of strings

Additional loop opening used to calculate the sensitivity function, specified as a string or cell array of strings. To open the loop at multiple locations, use a cell array of strings.

Each string in opening must match an analysis point in T. Analysis points are marked using AnalysisPoint blocks. Use getPoints(T) to get the list of available analysis points in T.

Use an opening, for example, to calculate the sensitivity function of an inner loop, with the outer loop open.

If **opening** and **location** list the same point, the software opens the loop after measuring the signal at the point.

Example: 'y_outer' or {'y_outer', 'y_outer2'}

Output Arguments

S - Sensitivity function

generalized state-space model

Sensitivity function of the control system, T, measured at location, returned as a Generalized State-Space Model (genss).

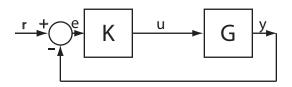
- If location specifies a single analysis point, then S is a SISO genss model.
- If location is a string specifying a vector signal, or a cell array identifying multiple analysis points, then S is a MIMO genss model.

More About

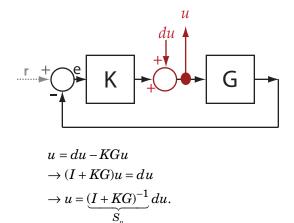
Sensitivity Function

The *sensitivity function*, also referred to simply as *sensitivity*, measures how sensitive a signal is to an added disturbance. Feedback reduces the sensitivity in the frequency band where the open-loop gain is greater than 1.

Consider the following model:

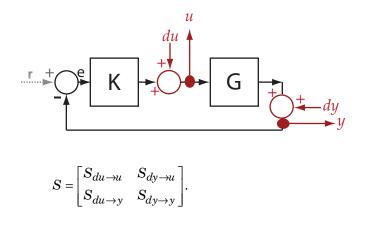


The sensitivity, S_u , at **u** is defined as the transfer function from du to **u**:



Here, *I* is an identity matrix of the same size as *KG*.

Sensitivity at multiple locations, for example, u and y, is defined as the MIMO transfer function from the disturbances to sensitivity measurements:



See Also

| AnalysisPoint | genss | getCompSensitivity | getIOTransfer | getLoopTransfer | getPoints | getSensitivity | getValue | systume

Introduced in R2014a

getPoints

Get list of analysis points in generalized model of control system

Syntax

```
points = getPoints(T)
```

Description

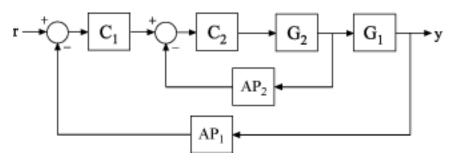
points = getPoints(T) returns the names of all analysis-point locations in a generalized state-space model of a control system. Use this function to query the list of available analysis points in the model for control system analysis or tuning. You can refer to the analysis-point locations by name to create design goals control system tuning or to compute open-loop and closed-loop responses using analysis commands such as getLoopTransfer and getIOTransfer.

Examples

Analysis-Point Locations in Control System Model

Build a closed-loop model of a cascaded feedback loop system, and get a list of analysis point locations in the model.

Create a model of the following cascaded feedback loop. C_1 and C_2 are tunable controllers. AP_1 and AP_2 are points of interest for analysis, which you mark with AnalysisPoint blocks.



```
G1 = tf(10,[1 10]);
G2 = tf([1 2],[1 0.2 10]);
C1 = ltiblock.pid('C','pi');
C2 = ltiblock.gain('G',1);
AP1 = AnalysisPoint('AP1');
AP2 = AnalysisPoint('AP2');
T = feedback(G1*feedback(G2*C2,AP2)*C1,AP1);
```

 ${\sf T}$ is a genss model whose Control Design Blocks include the tunable controllers and the switches AP1 and AP2.

Get a list of the loop-opening sites in T.

getPoints returns a cell array listing loop-opening sites in the model.

For more complicated closed-loop models, you can use getPoints to keep track of a larger number of analysis points.

Input Arguments

T - Model of control system

generalized state-space model

Model of a control system, specified as a generalized state-space (genss) model. Locations in the model at which you can calculate system responses or specify design goals for tuning are marked by AnalysisPoint blocks in T.

Output Arguments

points — Analysis-points locations

cell array of strings

Analysis-point locations in the control system model, returned as a cell array of strings. This output is obtained by concatenating the Location properties of all AnalysisPoint blocks in the control system model.

More About

• "Generalized Models"

See Also

AnalysisPoint | genss | getIOTransfer | getLoopTransfer

Introduced in R2014b

getValue

Current value of Generalized Model

Syntax

```
curval = getValue(M)
curval = getValue(M,blockvalues)
curval = getValue(M,Mref)
```

Description

curval = getValue(M) returns the current value curval of the Generalized LTI
model or Generalized matrix M. The current value is obtained by replacing all Control
Design Blocks in M by their current value. (For uncertain blocks, the "current value" is
the nominal value of the block.)

curval = getValue(M,blockvalues) uses the block values specified in the structure blockvalues to compute the current value. The field names and values of blockvalues specify the block names and corresponding values. Blocks of M not specified in blockvalues are replaced by their current values.

curval = getValue(M,Mref) inherits block values from the generalized model Mref. This syntax is equivalent to curval = getValue(M,Mref.Blocks). Use this syntax to evaluate the current value of M using block values computed elsewhere (for example, tuned values obtained with Robust Control Toolbox tuning commands such as systume, looptune, or hinfstruct).

Input Arguments

М

Generalized LTI model or Generalized matrix.

blockvalues

Structure specifying blocks of ${\tt M}$ to replace and the values with which to replace those blocks.

The field names of **blockvalues** match names of Control Design Blocks of M. Use the field values to specify the replacement values for the corresponding blocks of M. The field values can be numeric values, dynamic system models, or static models. If some field values are Control Design Blocks or Generalized LTI models, the current values of those models are used to compute curval.

Mref

Generalized LTI model. If you provide Mref, getValue computes curval using the current values of the blocks in Mref whose names match blocks in M.

Output Arguments

curval

Numeric array or Numeric LTI model representing the current value of M.

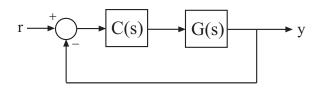
If you do not specify a replacement value for a given Control Design Block of M, getValue uses the current value of that block.

Examples

Evaluate Model for Specified Values of its Blocks

This example shows how to replace a Control Design Block in a Generalized LTI model with a specified replacement value using getValue.

Consider the following closed-loop system:



The following code creates a genss model of this system with $G(s) = \frac{(s-1)}{(s+1)^3}$ and a

tunable PI controller C.

```
G = zpk(1,[-1,-1,-1],1);
C = ltiblock.pid('C','pi');
Try = feedback(G*C,1)
```

The genss model Try has one Control Design Block, C. The block C is initialized to default values, and the model Try has a current value that depends on the current value of C. Use getValue to evaluate C and Try to examine the current values.

1 Evaluate C to obtain its current value.

Cnow = getValue(C)

This command returns a numeric **pid** object whose coefficients reflect the current values of the tunable parameters in **C**.

2 Evaluate Try to obtain its current value.

```
Tnow = getValue(Try)
```

This command returns a numeric model that is equivalent to feedback(G*Cnow, 1).

Access Values of Tuned Models and Blocks

Propagate changes in block values from one model to another using getValue.

This technique is useful for accessing values of models and blocks tuned with Robust Control Toolbox tuning commands such as systume, looptune, or hinfstruct. For example, if you have a closed-loop model of your control system TO, with two tunable blocks, C1 and C2, you can tune it using:

[T,fSoft] = systume(T0,SoftReqs);

You can then access the tuned values of C1 and C2, as well as any closed-loop model H that depends on C1 and C2, using the following:

```
C1t = getValue(C1,T);
C2t = getValue(C2,T);
Ht = getValue(H,T);
```

See Also

genss | replaceBlock | systune | looptune | hinfstruct

Introduced in R2011b

gram

Controllability and observability gramians

Syntax

```
Wc = gram(sys,'c')
Wc = gram(sys,'o')
```

Description

Wc = gram(sys, 'c') calculates the controllability gramian of the state-space (ss) model sys.

Wc = gram(sys, 'o') calculates the observability gramian of the ss model sys.

You can use gramians to study the controllability and observability properties of statespace models and for model reduction [1]. They have better numerical properties than the controllability and observability matrices formed by ctrb and obsv.

Given the continuous-time state-space model

$$\dot{x} = Ax + Bu$$
$$y = Cx + Du$$

the controllability gramian is defined by

$$W_{c} = \int_{0}^{\infty} e^{A\tau} B B^{T} e^{A^{T}\tau} d\tau$$

The controllability gramian is positive definite if and only if (A, B) is controllable.

The observability gramian is defined by

$$W_o = \int_0^\infty e^{A^T \tau} C^T C e^{A \tau} d\tau$$

The observability gramian is positive definite if and only if (A, C) is observable.

The discrete-time counterparts of the controllability and observability gramians are

$$W_c = \sum_{k=0}^{\infty} A^k B B^T (A^T)^k, \quad W_o = \sum_{k=0}^{\infty} (A^T)^k C^T C A^k$$

respectively.

Limitations

The *A* matrix must be stable (all eigenvalues have negative real part in continuous time, and magnitude strictly less than one in discrete time).

More About

Algorithms

The controllability gramian W_c is obtained by solving the continuous-time Lyapunov equation

$$AW_c + W_c A^T + BB^T = 0$$

or its discrete-time counterpart

$$AW_cA^T - W_c + BB^T = 0$$

Similarly, the observability gramian W_o solves the Lyapunov equation

$$A^T W_o + W_o A + C^T C = 0$$

in continuous time, and the Lyapunov equation

$$A^T W_o A - W_o + C^T C = 0$$

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in discrete time.

References

[1] Kailath, T., Linear Systems, Prentice-Hall, 1980.

See Also

balreal | ctrb | lyap | dlyap | obsv

Introduced before R2006a

hasdelay

True for linear model with time delays

Syntax

```
B = hasdelay(sys)
B = hasdelay(sys,'elem')
```

Description

B = hasdelay(sys) returns 1 (true) if the model sys has input delays, output delays, I/O delays, or internal delays, and 0 (false) otherwise. If sys is a model array, then B is true if least one model in sys has delays.

B = hasdelay(sys, 'elem') returns a logical array of the same size as the model array sys. The logical array indicates which models in sys have delays.

See Also totaldelay | absorbDelay

Introduced before R2006a

hasInternalDelay

Determine if model has internal delays

Syntax

```
B = hasInternalDelay(sys)
B = hasInternalDelay(sys, 'elem')
```

Description

B = hasInternalDelay(sys) returns 1 (true) if the model sys has internal delays, and 0 (false) otherwise. If sys is a model array, then B is true if least one model in sys has delays.

B = hasInternalDelay(sys, 'elem') checks each model in the model array sys and returns a logical array of the same size as sys. The logical array indicates which models in sys have internal delays.

Examples

Check model for internal delays

Build a dynamic system model of the following closed-loop system and check the model for internal delays.

$$s = tf('s');$$

$$G = exp(-2.4*s)/(s-5);$$

$$C = pid(5,0.1);$$

$$sys = feedback(G*C,1);$$

$$B = hasInternalDelay(sys)$$

$$B = 0$$

1

The model **sys** has an internal delay because of the transfer delay in the plant **G**. Therefore, **hasInternalDelay** returns 1.

Input Arguments

sys — Model or array to check

dynamic system model | model array

Model or array to check for internal delays, specified as a dynamic system model or array of dynamic system models.

Output Arguments

B - Flag indicating presence of internal delays

logical | logical array

Flag indicating presence of internal delays in input model or array, returned as a logical value or logical array.

See Also

getDelayModel | hasdelay

Introduced in R2013a

hsvd

Hankel singular values of dynamic system

Syntax

```
hsv = hsvd(sys)
hsv = hsvd(sys, 'AbsTol', ATOL, 'RelTol', RTOL, 'Offset', ALPHA)
hsv = hsvd(sys, opts)
hsvd(sys)
[hsv,baldata] = hsvd(sys)
```

Description

hsv = hsvd(sys) computes the Hankel singular values hsv of the dynamic system sys. In state coordinates that equalize the input-to-state and state-to-output energy transfers, the Hankel singular values measure the contribution of each state to the input/ output behavior. Hankel singular values are to model order what singular values are to matrix rank. In particular, small Hankel singular values signal states that can be discarded to simplify the model (see balred).

For models with unstable poles, hsvd only computes the Hankel singular values of the stable part and entries of hsv corresponding to unstable modes are set to Inf.

hsv = hsvd(sys, 'AbsTol', ATOL, 'RelTol', RTOL, 'Offset', ALPHA) specifies
additional options for the stable/unstable decomposition. See the stabsep reference page
for more information about these options. The default values are ATOL = 0, RTOL =
1e-8, and ALPHA = 1e-8.

hsv = hsvd(sys, opts) computes the Hankel singular values using the options
specified in the hsvdOptions object opts.

hsvd(sys) displays a Hankel singular values plot.

[hsv,baldata] = hsvd(sys) returns additional data to speed up model order reduction with balred. For example

```
sys = rss(20); % 20-th order model
[hsv,baldata] = hsvd(sys);
rsys = balred(sys,8:10,'Balancing',baldata);
bode(sys,'b',rsys,'r--')
```

computes three approximations of sys of orders 8, 9, 10.

There is more than one hsvd available. Type

help lti/hsvd

for more information.

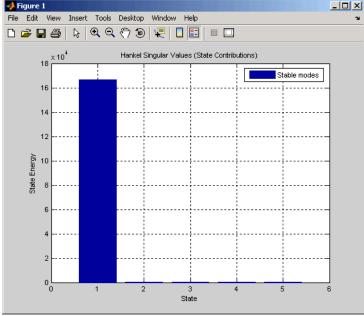
Examples

Compute Hankel Singular Values

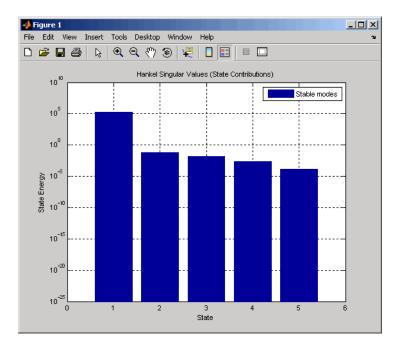
This example illustrates how to compute Hankel singular values.

First, create a system with a stable pole very near to 0, then calculate the Hankel singular values.

hsvd

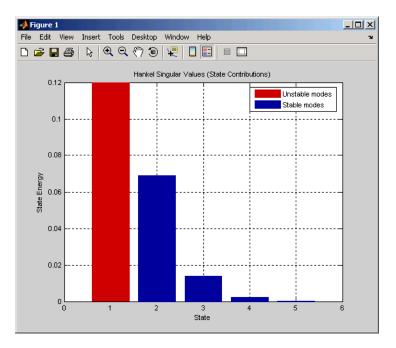


For a better view of the Hankel singular values, switch the plot to log scale by selecting Y Scale > Log from the right-click menu.



Notice the dominant Hankel singular value with 1e5 magnitude, due to the mode s=-1e-7 near the imaginary axis. Set the offset=1e-6 to treat this mode as unstable

```
hsvd(sys,'Offset',1e-7)
```



The dominant Hankel singular value is now shown as unstable.

More About

Tips

You can change the properties of your plot, for example the units. For information on the ways to change properties of your plots, see "Ways to Customize Plots".

Algorithms

The AbsTol, RelTol, and ALPHA parameters are only used for models with unstable or marginally stable dynamics. Because Hankel singular values are only meaningful for stable dynamics, hsvd must first split such models into the sum of their stable and unstable parts:

 $G = G_s + G_ns$

This decomposition can be tricky when the model has modes close to the stability boundary (e.g., a pole at s=-1e-10), or clusters of modes on the stability boundary (e.g.,

double or triple integrators). While hsvd is able to overcome these difficulties in most cases, it sometimes produces unexpected results such as

1 Large Hankel singular values for the stable part.

This happens when the stable part G_s contains some poles very close to the stability boundary. To force such modes into the unstable group, increase the 'Offset' option to slightly grow the unstable region.

2 Too many modes are labeled "unstable." For example, you see 5 red bars in the HSV plot when your model had only 2 unstable poles.

The stable/unstable decomposition algorithm has built-in accuracy checks that reject decompositions causing a significant loss of accuracy in the frequency response. Such loss of accuracy arises, e.g., when trying to split a cluster of stable and unstable modes near s=0. Because such clusters are numerically equivalent to a multiple pole at s=0, it is actually desirable to treat the whole cluster as unstable. In some cases, however, large relative errors in low-gain frequency bands can trip the accuracy checks and lead to a rejection of valid decompositions. Additional modes are then absorbed into the unstable part G_ns , unduly increasing its order.

Such issues can be easily corrected by adjusting the AbsTol and RelTol tolerances. By setting AbsTol to a fraction of smallest gain of interest in your model, you tell the algorithm to ignore errors below a certain gain threshold. By increasing RelTol, you tell the algorithm to sacrifice some relative model accuracy in exchange for keeping more modes in the stable part G_S.

See Also

hsvdOptions | balred | balreal

Introduced before R2006a

hsvdOptions

Create option set for computing Hankel singular values and input/output balancing

Syntax

```
opts = hsvdOptions
opts = hsvdOptions('OptionName', OptionValue)
```

Description

opts = hsvdOptions returns the default options for the hsvd and balreal
commands.

opts = hsvdOptions('OptionName', OptionValue) accepts one or more commaseparated name/value pairs. Specify OptionName inside single quotes.

Input Arguments

Name-Value Pair Arguments

'AbsTol, RelTol'

Absolute and relative error tolerance for stable/unstable decomposition. Positive scalar values. For an input model G with unstable poles, hsvd and balreal first extract the stable dynamics by computing the stable/unstable decomposition $G \rightarrow GS + GU$. The AbsTol and RelTol tolerances control the accuracy of this decomposition by ensuring that the frequency responses of G and GS + GU differ by no more than AbsTol + RelTol*abs(G). Increasing these tolerances helps separate nearby stable and unstable modes at the expense of accuracy. See stabsep for more information.

Default: AbsTol = 0; RelTol = 1e-8

'Offset'

Offset for the stable/unstable boundary. Positive scalar value. In the stable/unstable decomposition, the stable term includes only poles satisfying:

- Re(s) < -Offset * max(1, |Im(s)|) (Continuous time)
- |z| < 1 Offset (Discrete time)

Increase the value of Offset to treat poles close to the stability boundary as unstable.

Default: 1e-8

For additional information on the options and how to use them, see the hsvd and balreal reference pages.

Examples

Compute the Hankel singular values of the system given by:

$$sys = \frac{(s+0.5)}{(s+10^{-6})(s+2)}$$

Use the **Offset** option to force hsvd to exclude the pole at $s = 10^{-6}$ from the stable term of the stable/unstable decomposition.

sys = zpk(-.5,[-1e-6 -2],1);
opts = hsvdOptions('Offset',.001); % create option set
hsvd(sys,opts) % treats -1e-6 as unstable

See Also

hsvd|balreal

Introduced in R2010a

hsvoptions

Create list of Hankel singular value plot options

Syntax

```
P = hsvoptions
P = HSVOPTIONS('cstpref')
```

Description

P = hsvoptions returns a list of available options for Hankel singular value (HSV) plots with default values set. You can use these options to customize the Hankel singular value plot appearance using the command line.

P = HSVOPTIONS('cstpref') initializes the plot options you selected in the Control System Toolbox Preferences Editor dialog box. For more information about the editor, see "Toolbox Preferences Editor" in the User's Guide documentation.

This table summarizes the Hankel singular value plot options.

Option	Description	
Title, XLabel, YLabel	Label text and style	
TickLabel	Tick label style	
Grid [off on]	Show or hide the grid	
GridColor [Vector of RGB values in the range [0,1] color string 'none']	Color of the grid lines	
XlimMode, YlimMode	Limit modes	
Xlim, Ylim	Axes limits	
YScale [linear log]	Scale for Y-axis	
AbsTol, RelTol, Offset	Parameters for the Hankel singular value computation (used only for models	

Option	Description	
	with unstable dynamics). See hsvd and stabsep for details.	

Examples

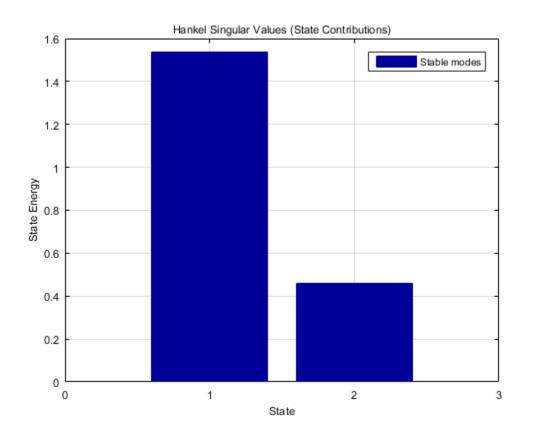
Set Scale for Y-Axis in HSV Plot

Create an options set, and set the **Yscale** property.

P = hsvoptions; P.YScale = 'linear';

Use the options set to generate an HSV plot. Note the linear y-axis scale in the plot.

h = hsvplot(rss(2,2,3),P);



See Also

hsvd | hsvplot | getoptions | setoptions | stabsep

Introduced in R2008a

hsvplot

Plot Hankel singular values and return plot handle

Syntax

```
h = hsvplot(sys)
hsvplot(sys)
hsvplot(sys, AbsTol',ATOL,'RelTol',RTOL,'Offset',ALPHA)
hsvplot(AX,sys,...)
```

Description

h = hsvplot(sys) plots the Hankel singular values of an LTI system sys and returns the plot handle h. You can use this handle to customize the plot with the getoptions and setoptions commands. Type

help hsvoptions

for a list of available plot options.

hsvplot(sys) plots the Hankel singular values of the LTI model sys. See hsvd for details on the meaning and purpose of Hankel singular values. The Hankel singular values for the stable and unstable modes of sys are shown in blue and red, respectively.

hsvplot(sys, AbsTol',ATOL, 'RelTol',RTOL, 'Offset',ALPHA) specifies additional options for computing the Hankel singular values.

hsvplot(AX, sys,...) attaches the plot to the axes with handle AX.

Examples

Use the plot handle to change plot options in the Hankel singular values plot.

```
sys = rss(20);
h = hsvplot(sys,'AbsTol',1e-6);
% Switch to log scale and modify Offset parameter
```

```
setoptions(h,'Yscale','log','Offset',0.3)
```

More About

Tips

You can change the properties of your plot, for example the units. For information on the ways to change properties of your plots, see "Ways to Customize Plots".

See Also

getoptions | hsvd | hsvoptions | setoptions

imp2exp

Convert implicit linear relationship to explicit input-output relation

Syntax

```
B = imp2exp(A,yidx,uidx)
```

Description

B = imp2exp(A, yidx, uidx) transforms a linear constraint between variables Y and U of the form A(:,[yidx;uidx])*[Y;U] = 0 into an explicit input/output relationship Y = B*U. The vectors yidx and uidx refer to the columns (inputs) of A as referenced by the explicit relationship for B.

The constraint matrix A can be a double, ss, tf, zpk and frd object as well as an uncertain object, including umat, uss and ufrd. The result B will be of the same class.

Examples

Scalar Algebraic Constraint

Consider the constraint 4y + 7u = 0. Solving for y gives y = 1.75u. You form the equation using imp2exp:

```
A = [4 7];
Yidx = 1;
Uidx = 2;
and then
B = imp2exp(A,Yidx,Uidx)
B =
-1.7500
```

yields B equal to -1.75.

Matrix Algebraic Constraint

```
Consider two motor/generator constraints among 4 variables [V;I;T;W], namely [1 -1

0 -2e-3;0 -2e-3 1 0]*[V;I;T;W] = 0. You can find the 2-by-2 matrix B so that

[V;T] = B*[W;I] using imp2exp.

A = [1 -1 0 -2e-3;0 -2e-3 1 0];

Yidx = [1 3];

Uidx = [4 2];

B = imp2exp(A,Yidx,Uidx)

B =

0.0020 1.0000

0 0.0020

You can find the 2-by-2 matrix C so that [I;W] = C*[T;V]

Yidx = [2 4];

Uidx = [3 1];
```

```
C = imp2exp(A, Yidx, Uidx)

C = 500 0

-250000 500
```

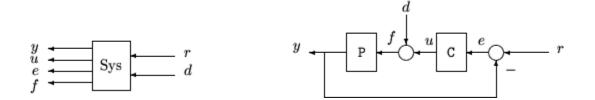
Uncertain Matrix Algebraic Constraint

Consider two uncertain motor/generator constraints among 4 variables [V;I;T;W], namely $[1 - R \ 0 - K; 0 - K \ 1 \ 0]^{*}[V;I;T;W] = 0$. You can find the uncertain 2-by-2 matrix B so that $[V;T] = B^{*}[W;I]$.

```
R = ureal('R',1,'Percentage',[-10 40]);
K = ureal('K',2e-3,'Percentage',[-30 30]);
A = [1 -R 0 -K;0 -K 1 0];
Yidx = [1 3];
Uidx = [4 2];
B = imp2exp(A,Yidx,Uidx)
UMAT: 2 Rows, 2 Columns
K: real, nominal = 0.002, variability = [-30 30]%, 2 occurrences
R: real, nominal = 1, variability = [-10 40]%, 1 occurrence
```

Scalar Dynamic System Constraint

Consider a standard single-loop feedback connection of controller C and an uncertain plant P, described by the equations e = r - y; u = Ce; f = d+u; y = Pf.



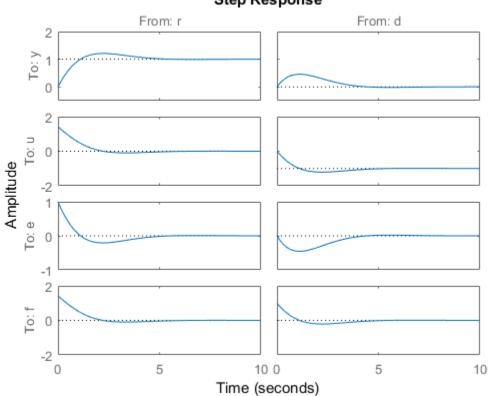
```
P = tf([1],[1 0]);
C = tf([2*.707*1 1^2],[1 0]);
A = [1 -1 0 0 0 -1;0 -C 1 0 0 0;0 0 -1 -1 1 0;0 0 0 0 -P 1];
OutputIndex = [6;3;2;5]; % [y;u;e;f]
InputIndex = [1;4]; % [r;d]
Sys = imp2exp(A,OutputIndex,InputIndex);
Sys.InputName = { 'r';'d' };
Sys.OutputName = { 'y';'u';'e';'f' };
```

pole(Sys)

ans =

-0.7070	+	0.7072i
-0.7070	-	0.7072i
-0.7070	+	0.7072i
-0.7070	-	0.7072i

stepplot(Sys)



Step Response

More About

Algorithms

The number of rows of A must equal the length of yidx.

See Also

iconnect | inv

Introduced in R2011b

impulse

Impulse response plot of dynamic system; impulse response data

Syntax

```
impulse(sys)
impulse(sys,Tfinal)
impulse(sys,t)
impulse(sys1,sys2,...,sysN)
impulse(sys1,sys2,...,sysN,Tfinal)
impulse(sys1,sys2,...,sysN,t)
[y,t] = impulse(sys)
[y,t] = impulse(sys,Tfinal)
y = impulse(sys,t)
[y,t,x] = impulse(sys)
[y,t,x,ysd] = impulse(sys)
```

Description

impulse calculates the unit impulse response of a dynamic system model. For continuous-time dynamic systems, the impulse response is the response to a Dirac input $\delta(t)$. For discrete-time systems, the impulse response is the response to a unit area pulse of length Ts and height 1/Ts, where Ts is the sample time of the system. (This pulse approaches $\delta(t)$ as Ts approaches zero.) For state-space models, impulse assumes initial state values are zero.

impulse(sys) plots the impulse response of the dynamic system model sys. This model can be continuous or discrete, and SISO or MIMO. The impulse response of multi-input systems is the collection of impulse responses for each input channel. The duration of simulation is determined automatically to display the transient behavior of the response.

impulse(sys,Tfinal) simulates the impulse response from t = 0 to the final time t = Tfinal. Express Tfinal in the system time units, specified in the TimeUnit property of sys. For discrete-time systems with unspecified sample time (Ts = -1), impulse interprets Tfinal as the number of sampling periods to simulate. impulse(sys,t) uses the user-supplied time vector t for simulation. Express t in the system time units, specified in the TimeUnit property of sys. For discrete-time models, t should be of the form Ti:Ts:Tf, where Ts is the sample time. For continuoustime models, t should be of the form Ti:dt:Tf, where dt becomes the sample time of a discrete approximation to the continuous system (see "Algorithms" on page 1-335). The impulse command always applies the impulse at t=0, regardless of Ti.

To plot the impulse responses of several models sys1,..., sysN on a single figure, use:

impulse(sys1,sys2,...,sysN)
impulse(sys1,sys2,...,sysN,Tfinal)
impulse(sys1,sys2,...,sysN,t)

As with **bode** or **plot**, you can specify a particular color, linestyle, and/or marker for each system, for example,

impulse(sys1,'y:',sys2,'g--')

See "Plotting and Comparing Multiple Systems" and the **bode** entry in this section for more details.

When invoked with output arguments:

[y,t] = impulse(sys)
[y,t] = impulse(sys,Tfinal)

y = impulse(sys,t)

impulse returns the output response y and the time vector t used for simulation (if not supplied as an argument to impulse). No plot is drawn on the screen. For single-input systems, y has as many rows as time samples (length of t), and as many columns as outputs. In the multi-input case, the impulse responses of each input channel are stacked up along the third dimension of y. The dimensions of y are then

For state-space models only:

[y,t,x] = impulse(sys)
(length of t) × (number of outputs) × (number of inputs)

and y(:,:,j) gives the response to an impulse disturbance entering the jth input channel. Similarly, the dimensions of x are (length of t) × (number of states) × (number of inputs)

[y,t,x,ysd] = impulse(sys) returns the standard deviation YSD of the response Y of an identified system SYS. YSD is empty if SYS does not contain parameter covariance information.

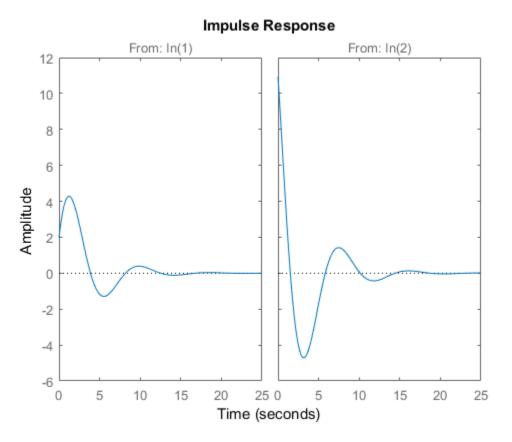
Examples

Impulse Response Plot of Second-Order State-Space Model

Plot the impulse response of the second-order state-space model

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} -0.5572 & -0.7814 \\ 0.7814 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 1 & -1 \\ 0 & 2 \end{bmatrix} \begin{bmatrix} u_1 \\ u_2 \end{bmatrix}$$
$$y = \begin{bmatrix} 1.9691 & 6.4493 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$

```
a = [-0.5572 -0.7814;0.7814 0];
b = [1 -1;0 2];
c = [1.9691 6.4493];
sys = ss(a,b,c,0);
impulse(sys)
```



The left plot shows the impulse response of the first input channel, and the right plot shows the impulse response of the second input channel.

You can store the impulse response data in MATLAB arrays by

[y,t] = impulse(sys);

Because this system has two inputs, y is a 3-D array with dimensions

size(y)
ans =
 139 1 2

(the first dimension is the length of t). The impulse response of the first input channel is then accessed by

```
ch1 = y(:,:,1);
size(ch1)
ans =
```

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Impulse Data from Identified System

Fetch the impulse response and the corresponding 1 std uncertainty of an identified linear system .

```
load(fullfile(matlabroot, 'toolbox', 'ident', 'iddemos', 'data', 'dcmotordata'));
z = iddata(y, u, 0.1, 'Name', 'DC-motor');
set(z, 'InputName', 'Voltage', 'InputUnit', 'V');
set(z, 'OutputName', {'Angular position', 'Angular velocity'});
set(z, 'OutputUnit', {'rad', 'rad/s'});
set(z, 'Tstart', 0, 'TimeUnit', 's');
model = tfest(z,2);
[y,t,~,ysd] = impulse(model,2);
% Plot 3 std uncertainty
subplot(211)
plot(t,y(:,1), t,y(:,1)+3*ysd(:,1),'k:', t,y(:,1)-3*ysd(:,1),'k:')
subplot(212)
plot(t,y(:,2), t,y(:,2)+3*ysd(:,2),'k:', t,y(:,2)-3*ysd(:,2),'k:')
```

Limitations

The impulse response of a continuous system with nonzero D matrix is infinite at t = 0. impulse ignores this discontinuity and returns the lower continuity value Cb at t = 0.

More About

Tips

You can change the properties of your plot, for example the units. For information on the ways to change properties of your plots, see "Ways to Customize Plots".

Algorithms

Continuous-time models are first converted to state space. The impulse response of a single-input state-space model

$$\dot{x} = Ax + bu$$
$$y = Cx$$

is equivalent to the following unforced response with initial state b.

$$\dot{x} = Ax, \quad x(0) = b$$

 $y = Cx$

To simulate this response, the system is discretized using zero-order hold on the inputs. The sample time is chosen automatically based on the system dynamics, except when a time vector t = 0:dt:Tf is supplied (dt is then used as sample time).

See Also

linearSystemAnalyzer | initial | step | lsim

impulseplot

Plot impulse response and return plot handle

Syntax

```
impulseplot(sys)
impulseplot(sys,Tfinal)
impulseplot(sys,t)
impulseplot(sys1,sys2,...,sysN)
impulseplot(sys1,sys2,...,sysN,Tfinal)
impulseplot(AX,...)
impulseplot(..., plotoptions)
h = impulseplot(...)
```

Description

impulseplot plots the impulse response of the dynamic system model sys. For multiinput models, independent impulse commands are applied to each input channel. The time range and number of points are chosen automatically. For continuous systems with direct feedthrough, the infinite pulse at t=0 is disregarded. impulseplot can also return the plot handle, h. You can use this handle to customize the plot with the getoptions and setoptions commands. Type

help timeoptions

for a list of available plot options.

impulseplot(sys) plots the impulse response of the LTI model without returning the
plot handle.

impulseplot(sys,Tfinal) simulates the impulse response from t = 0 to the final time t = Tfinal. Express Tfinal in the system time units, specified in the TimeUnit property of sys. For discrete-time systems with unspecified sample time (Ts = -1), impulseplot interprets Tfinal as the number of sampling intervals to simulate.

impulseplot(sys,t) uses the user-supplied time vector t for simulation. Express t
in the system time units, specified in the TimeUnit property of sys. For discrete-time

models, t should be of the form Ti:Ts:Tf, where Ts is the sample time. For continuoustime models, t should be of the form Ti:dt:Tf, where dt becomes the sample time of a discrete approximation to the continuous system (see impulse). The impulseplot command always applies the impulse at t=0, regardless of Ti.

To plot the impulse response of multiple LTI models sys1,sys2,... on a single plot, use:

```
impulseplot(sys1,sys2,...,sysN)
```

```
impulseplot(sys1,sys2,...,sysN,Tfinal)
```

```
impulseplot(sys1,sys2,...,sysN,t)
```

You can also specify a color, line style, and marker for each system, as in

```
impulseplot(sys1,'r',sys2,'y--',sys3,'gx')
```

impulseplot(AX,...) plots into the axes with handle AX.

impulseplot(..., plotoptions) plots the impulse response with the options
specified in plotoptions. Type

```
help timeoptions
```

for more detail.

h = impulseplot(...) plots the impulse response and returns the plot handle h.

Examples

Example 1

Normalize the impulse response of a third-order system.

```
sys = rss(3);
h = impulseplot(sys);
% Normalize responses
setoptions(h,'Normalize','on');
```

Example 2

Plot the impulse response and the corresponding 1 std "zero interval" of an identified linear system.

```
load(fullfile(matlabroot, 'toolbox', 'ident', 'iddemos', 'data', 'dcmotordata'));
z = iddata(y, u, 0.1, 'Name', 'DC-motor');
set(z, 'InputName', 'Voltage', 'InputUnit', 'V');
set(z, 'OutputName', {'Angular position', 'Angular velocity'});
set(z, 'OutputUnit', {'rad', 'rad/s'});
set(z, 'Tstart', 0, 'TimeUnit', 's');
model = n4sid(z,4,n4sidOptions('Focus', 'simulation'));
h = impulseplot(model,2);
showConfidence(h);
```

More About

Tips

You can change the properties of your plot, for example the units. For information on the ways to change properties of your plots, see "Ways to Customize Plots".

See Also

impulse | setoptions | getoptions

initial

initial

Initial condition response of state-space model

Syntax

```
initial(sys,x0)
initial(sys,x0,Tfinal)
initial(sys,x0,t)
initial(sys1,sys2,...,sysN,x0)
initial(sys1,sys2,...,sysN,x0,Tfinal)
initial(sys1,sys2,...,sysN,x0,t)
[y,t,x] = initial(sys,x0)
[y,t,x] = initial(sys,x0,Tfinal)
[y,t,x] = initial(sys,x0,t)
```

Description

initial(sys,x0) calculates the unforced response of a state-space (ss) model sys with an initial condition on the states specified by the vector x0:

 $\dot{x} = Ax, \quad x(0) = x_0$ y = Cx

This function is applicable to either continuous- or discrete-time models. When invoked without output arguments, initial plots the initial condition response on the screen.

initial(sys,x0,Tfinal) simulates the response from t = 0 to the final time t = Tfinal. Express Tfinal in the system time units, specified in the TimeUnit property of sys. For discrete-time systems with unspecified sample time (Ts = -1), initial interprets Tfinal as the number of sampling periods to simulate.

initial(sys,x0,t) uses the user-supplied time vector t for simulation. Express t
in the system time units, specified in the TimeUnit property of sys. For discrete-time
models, t should be of the form 0:Ts:Tf, where Ts is the sample time. For continuous
time models, t should be of the form 0:dt:Tf, where dt becomes the sample time of a
discrete approximation to the continuous system (see impulse).

To plot the initial condition responses of several LTI models on a single figure, use

```
initial(sys1,sys2,...,sysN,x0)
```

```
initial(sys1,sys2,...,sysN,x0,Tfinal)
```

```
initial(sys1,sys2,...,sysN,x0,t)
```

(see impulse for details).

When invoked with output arguments,

[y,t,x] = initial(sys,x0)
[y,t,x] = initial(sys,x0,Tfinal)
[y,t,x] = initial(sys,x0,t)

return the output response y, the time vector t used for simulation, and the state trajectories x. No plot is drawn on the screen. The array y has as many rows as time samples (length of t) and as many columns as outputs. Similarly, x has length(t) rows and as many columns as states.

Examples

Response of State-Space Model to Initial Condition

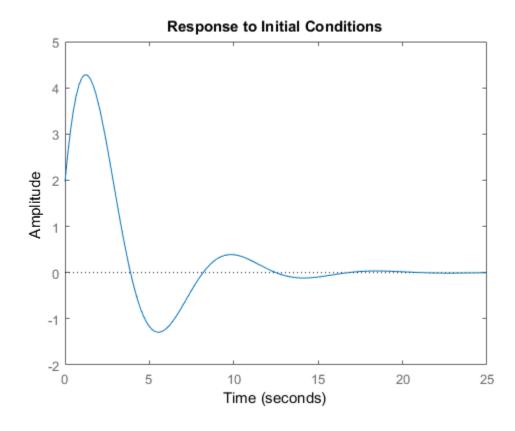
Plot the response of the following state-space model:

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} -0.5572 & -0.7814 \\ 0.7814 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$
$$y = \begin{bmatrix} 1.9691 & 6.4493 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}.$$

Take the following initial condition:

$$x(0) = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$
.
a = [-0.5572, -0.7814; 0.7814, 0];

```
c = [1.9691 6.4493];
x0 = [1 ; 0];
sys = ss(a,[],c,[]);
initial(sys,x0)
```



More About

Tips

You can change the properties of your plot, for example the units. For information on the ways to change properties of your plots, see "Ways to Customize Plots".

See Also

impulse | lsim | linearSystemAnalyzer | step

initialplot

Plot initial condition response and return plot handle

Syntax

```
initialplot(sys,x0)
initialplot(sys,x0,Tfinal)
initialplot(sys,x0,t)
initialplot(sys1,sys2,...,sysN,x0)
initialplot(sys1,sys2,...,sysN,x0,Tfinal)
initialplot(sys1,sys2,...,sysN,x0,t)
initialplot(AX,...)
initialplot(..., plotoptions)
h = initialplot(...)
```

Description

initialplot(sys,x0) plots the undriven response of the state-space (ss) model sys
with initial condition x0 on the states. This response is characterized by these equations:

Continuous time: x = A x, y = C x, x(0) = x0

Discrete time: x[k+1] = A x[k], y[k] = C x[k], x[0] = x0

The time range and number of points are chosen automatically. initialplot also returns the plot handle h. You can use this handle to customize the plot with the getoptions and setoptions commands. Type

help timeoptions

for a list of available plot options.

initialplot(sys,x0,Tfinal) simulates the response from t = 0 to the final time t = Tfinal. Express Tfinal in the system time units, specified in the TimeUnit property of sys. For discrete-time systems with unspecified sample time (Ts = -1), initialplot interprets Tfinal as the number of sampling periods to simulate. initialplot(sys,x0,t) uses the user-supplied time vector t for simulation. Express
t in the system time units, specified in the TimeUnit property of sys. For discrete-time
models, t should be of the form 0:Ts:Tf, where Ts is the sample time. For continuoustime models, t should be of the form 0:dt:Tf, where dt becomes the sample time of a
discrete approximation to the continuous system (see impulse).

To plot the initial condition responses of several LTI models on a single figure, use

initialplot(sys1,sys2,...,sysN,x0)

initialplot(sys1,sys2,...,sysN,x0,Tfinal)

initialplot(sys1,sys2,...,sysN,x0,t)

You can also specify a color, line style, and marker for each system, as in

initialplot(sys1,'r',sys2,'y--',sys3,'gx',x0).

initialplot(AX,...) plots into the axes with handle AX.

initialplot(..., plotoptions) plots the initial condition response with the options specified in plotoptions. Type

help timeoptions

for more detail.

h = initialplot(...) plots the system response and returns the plot handle h.

Examples

Plot a third-order system's response to initial conditions and use the plot handle to change the plot's title.

```
sys = rss(3);
h = initialplot(sys,[1,1,1])
p = getoptions(h); % Get options for plot.
p.Title.String = 'My Title'; % Change title in options.
setoptions(h,p); % Apply options to the plot.
```

More About

Tips

You can change the properties of your plot, for example the units. For information on the ways to change properties of your plots, see "Ways to Customize Plots".

See Also

getoptions | initial | setoptions

interp

Interpolate FRD model

Syntax

isys = interp(sys,freqs)

Description

isys = interp(sys,freqs) interpolates the frequency response data contained in the FRD model sys at the frequencies freqs. interp, which is an overloaded version of the MATLAB function interp, uses linear interpolation and returns an FRD model isys containing the interpolated data at the new frequencies freqs. If sys is an IDFRD model (requires System Identification Toolbox software), the noise spectrum, if nonempty, is also interpolated. The response and noise covariance data, if available, are also interpolated.

You should express the frequency values freqs in the same units as sys.frequency. The frequency values must lie between the smallest and largest frequency points in sys (extrapolation is not supported).

See Also freqresp | frd

inv

Invert models

Syntax

inv

Description

inv inverts the input/output relation

y = G(s)u

to produce the model with the transfer matrix $H(s) = G(s)^{-1}$.

u = H(s)y

This operation is defined only for square systems (same number of inputs and outputs) with an invertible feedthrough matrix D. inv handles both continuous- and discrete-time systems.

Examples

Consider

$$H(s) = \begin{bmatrix} 1 & \frac{1}{s+1} \\ 0 & 1 \end{bmatrix}$$

At the MATLAB prompt, type

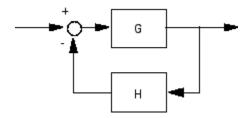
H = [1 tf(1,[1 1]);0 1] Hi = inv(H) to invert it. These commands produce the following result.

```
Transfer function from input 1 to output...
#1: 1
#2: 0
Transfer function from input 2 to output...
_1
#1: ----
s + 1
#2: 1
You can verify that
H * Hi
```

is the identity transfer function (static gain I).

Limitations

Do not use inv to model feedback connections such as



While it seems reasonable to evaluate the corresponding closed-loop transfer function

```
(I+GH)^{-1}G as
```

inv(1+g*h) * g

this typically leads to nonminimal closed-loop models. For example,

g = zpk([],1,1) h = tf([2 1],[1 0]) cloop = inv(1+g*h) * g yields a third-order closed-loop model with an unstable pole-zero cancellation at s = 1.

cloop

```
Zero/pole/gain:
s (s-1)
(s-1) (s^2 + s + 1)
```

Use feedback to avoid such pitfalls.

iopzmap

Plot pole-zero map for I/O pairs of model

Syntax

```
iopzmap(sys)
iopzmap(sys1,sys2,...)
```

Description

iopzmap(sys) computes and plots the poles and zeros of each input/output pair of the dynamic system model sys. The poles are plotted as x's and the zeros are plotted as o's.

```
iopzmap(sys1,sys2,...) shows the poles and zeros of multiple models
sys1,sys2,... on a single plot. You can specify distinctive colors for each model, as in
iopzmap(sys1,'r',sys2,'y',sys3,'g').
```

The functions **sgrid** or **zgrid** can be used to plot lines of constant damping ratio and natural frequency in the *s* or *z* plane.

For model arrays, iopzmap plots the poles and zeros of each model in the array on the same diagram.

Examples

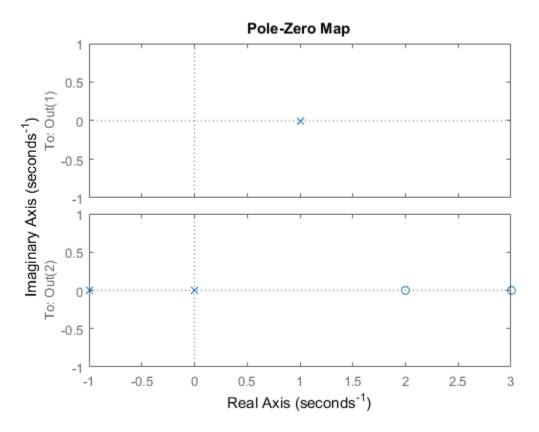
Pole-Zero Map for MIMO System

Create a one-input, two-output dynamic system.

```
H = [tf(-5, [1 - 1]); tf([1 - 5 6], [1 1 0])];
```

Plot a pole-zero map.

iopzmap(H)

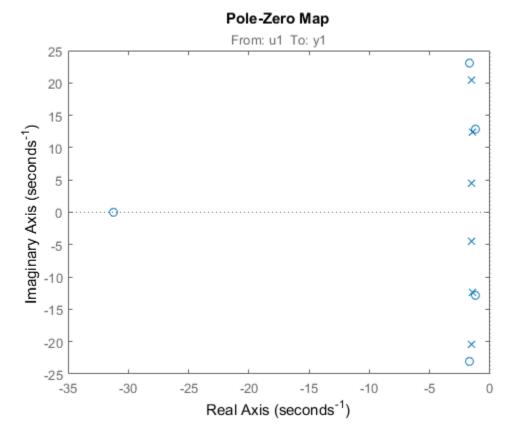


iopzmap generates a separate map for each I/O pair in the system.

Pole-Zero Map of Identified Model

View the poles and zeros of an over-parameterized state-space model estimated from input-output data. (Requires System Identification ToolboxTM).

```
load iddata1
sys = ssest(z1,6,ssestOptions('focus','simulation'));
iopzmap(sys)
```



The plot shows that there are two pole-zero pairs that almost overlap, which hints are their potential redundancy.

More About

Tips

You can change the properties of your plot, for example the units. For information on the ways to change properties of your plots, see "Ways to Customize Plots".

See Also

pole | zero | sgrid | zgrid | iopzplot | pzmap

iopzplot

Plot pole-zero map for I/O pairs and return plot handle

Syntax

```
h = iopzplot(sys)
iopzplot(sys1,sys2,...)
iopzplot(AX,...)
iopzplot(..., plotoptions)
```

Description

h = iopzplot(sys) computes and plots the poles and zeros of each input/output pair of the LTI model SYS. The poles are plotted as x's and the zeros are plotted as o's. It also returns the plot handle h. You can use this handle to customize the plot with the getoptions and setoptions commands. Type

help pzoptions

for a list of available plot options.

iopzplot(sys1,sys2,...) shows the poles and zeros of multiple LTI models SYS1,SYS2,... on a single plot. You can specify distinctive colors for each model, as in

iopzplot(sys1,'r',sys2,'y',sys3,'g')

iopzplot(AX,...) plots into the axes with handle AX.

iopzplot(..., plotoptions) plots the poles and zeros with the options specified in
plotoptions. Type

help pzoptions

for more detail.

The function sgrid or zgrid can be used to plot lines of constant damping ratio and natural frequency in the s or z plane.

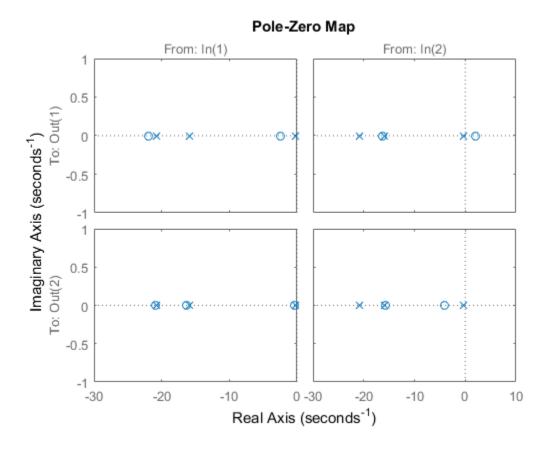
For arrays **sys** of LTI models, **iopzplot** plots the poles and zeros of each model in the array on the same diagram.

Examples

Change I/O Grouping on Pole/Zero Map

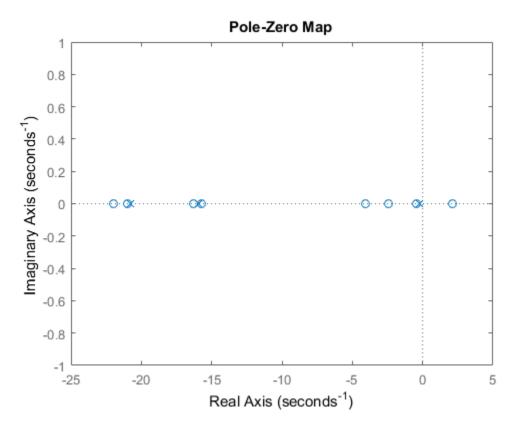
Create a pole/zero map of a two-input, two-output dynamic system.

sys = rss(3,2,2); h = iopzplot(sys);



By default, the plot displays the poles and zeros of each I/O pair on its own axis. Use the plot handle to view all I/Os on a single axis.

```
setoptions(h,'IOGrouping','all')
```

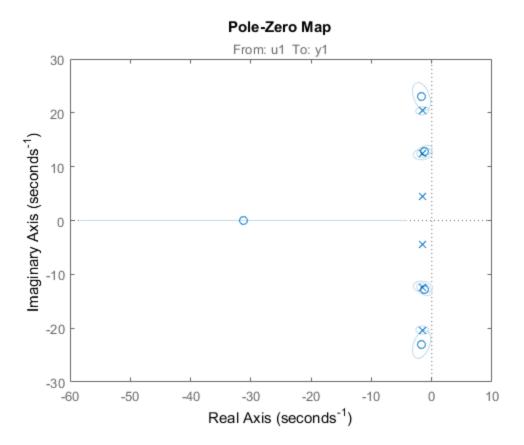


Use Pole-Zero Map to Examine Identified Model

View the poles and zeros of a sixth-order state-space model estimated from input-output data. Use the plot handle to display the confidence intervals of the identified model's pole and zero locations.

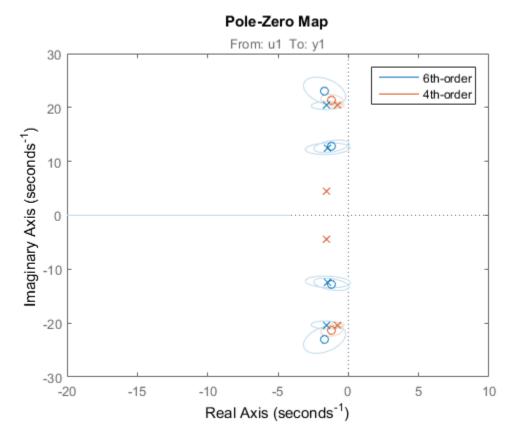
```
load iddata1
sys = ssest(z1,6,ssestOptions('focus','simulation'));
```

h = iopzplot(sys); showConfidence(h)



There is at least one pair of complex-conjugate poles whose locations overlap with those of a complex zero, within the 1-o confidence region. This suggests their redundancy. Hence, a lower (4th) order model might be more robust for the given data.

```
sys2 = ssest(z1,4,ssestOptions('focus','simulation'));
h = iopzplot(sys,sys2);
showConfidence(h)
legend('6th-order','4th-order')
axis([-20, 10 -30 30])
```



The fourth-order model sys2 shows less variability in the pole-zero locations.

More About

Tips

You can change the properties of your plot, for example the units. For information on the ways to change properties of your plots, see "Ways to Customize Plots".

See Also

iopzmap | setoptions | getoptions

Introduced before R2006a

isct

Determine if dynamic system model is in continuous time

Syntax

bool = isct(sys)

Description

bool = isct(sys) returns a logical value of 1 (true) if the dynamic system model sys
is a continuous-time model. The function returns a logical value of 0 (false) otherwise.

Input Arguments

sys

Dynamic system model or array of such models.

Output Arguments

bool

Logical value indicating whether sys is a continuous-time model.

bool = 1 (true) if sys is a continuous-time model (sys.Ts = 0). If sys is a discretetime model, bool = 0 (false).

For a static gain, both isct and isdt return true unless you explicitly set the sample time to a nonzero value. If you do so, isdt returns true and isct returns false.

For arrays of models, bool is true if the models in the array are continuous.

See Also

isdt | isstable

Introduced in R2007a

isdt

Determine if dynamic system model is in discrete time

Syntax

bool = isdt(sys)

Description

bool = isdt(sys) returns a logical value of 1 (true) if the dynamic system model sys
is a discrete-time model. The function returns a logical value of 0 (false) otherwise.

Input Arguments

sys

Dynamic system model or array of such models.

Output Arguments

bool

Logical value indicating whether **sys** is a discrete-time model.

bool = 1 (true) if sys is a discrete-time model (sys.Ts \neq 0). If sys is a continuous-time model, bool = 0 (false).

For a static gain, both isct and isdt return true unless you explicitly set the sample time to a nonzero value. If you do so, isdt returns true and isct returns false.

For arrays of models, bool is true if the models in the array are discrete.

See Also

isct | isstable

Introduced in R2007a

isempty

Determine whether dynamic system model is empty

Syntax

isempty(sys)

Description

isempty(sys) returns TRUE (logical 1) if the dynamic system model sys has no input or no output, and FALSE (logical 0) otherwise. Where sys is a FRD model, isempty(sys) returns TRUE when the frequency vector is empty. Where sys is a model array, isempty(sys) returns TRUE when the array has empty dimensions or when the LTI models in the array are empty.

Examples

Both commands

isempty(tf) % tf by itself returns an empty transfer function isempty(ss(1,2,[],[]))

return TRUE (logical 1) while

isempty(ss(1,2,3,4))

returns FALSE (logical 0).

See Also

size | issiso

Introduced before R2006a

isfinite

Determine if model has finite coefficients

Syntax

```
B = isfinite(sys)
B = isfinite(sys,'elem')
```

Description

B = isfinite(sys) returns 1 (true) if the model sys has finite coefficients, and 0 (false) otherwise. If sys is a model array, then B is true if all models in sys have finite coefficients.

B = isfinite(sys, 'elem') checks each model in the model array sys and returns a logical array of the same size as sys. The logical array indicates which models in sys have finite coefficients.

Examples

Check Model for Finite Coefficients

Create model and check whether its coefficients are all finite.

```
sys = rss(3);
B = isfinite(sys)
B =
1
```

Check Each Model in Array

Create a 1-by-5 array of models and check each model for finite coefficients.

sys = rss(2,2,2,1,5); B = isfinite(sys,'elem') B = 1 1 1 1 1

When you use the 'elem' input, isfinite checks each model individually and returns a logical array indicating which models have all finite coefficients.

Input Arguments

sys — **Model or array to check** input-output model | model array

Model or array to check, specified as an input-output model or model array. Input-output models include dynamic system models such as numeric LTI models and generalized models. Input-output models also include static models such as tunable parameters or generalized matrices.

Output Arguments

B - Flag indicating whether model has finite coefficients

logical | logical array

Flag indicating whether model has finite coefficients, returned as a logical value or logical array.

See Also

isreal

Introduced in R2013a

isParametric

Determine if model has tunable parameters

Syntax

bool = isParametric(M)

Description

bool = isParametric(M) returns a logical value of 1 (true) if the model M contains parametric (tunable) "Control Design Blocks". The function returns a logical value of 0 (false) otherwise.

Input Arguments

М

A Dynamic System model or Static model, or an array of such models.

Output Arguments

bool

Logical value indicating whether M contains tunable parameters.

bool = 1 (true) if the model M contains parametric (tunable) "Control Design Blocks"
such as realp or ltiblock.ss. If M does not contain parametric Control Design Blocks,
bool = 0 (false).

More About

- "Control Design Blocks"
- "Dynamic System Models"

"Static Models"

See Also

nblocks

Introduced in R2011a

isproper

Determine if dynamic system model is proper

Syntax

```
B = isproper(sys)
B = isproper(sys,'elem')
[B, sysr] = isproper(sys)
```

Description

B = isproper(sys) returns TRUE (logical 1) if the dynamic system model sys is proper and FALSE (logical 0) otherwise.

A proper model has relative degree ≤ 0 and is causal. SISO transfer functions and zeropole-gain models are proper if the degree of their numerator is less than or equal to the degree of their denominator (in other words, if they have at least as many poles as zeroes). MIMO transfer functions are proper if all their SISO entries are proper. Regular state-space models (state-space models having no E matrix) are always proper. A descriptor state-space model that has an invertible E matrix is always proper. A descriptor state-space model having a singular (non-invertible) E matrix is proper if the model has at least as many poles as zeroes.

If sys is a model array, then B is TRUE if all models in the array are proper.

B = isproper(sys, 'elem') checks each model in a model array sys and returns a logical array of the same size as sys. The logical array indicates which models in sys are proper.

If sys is a proper descriptor state-space model with a non-invertible E matrix, [B, sysr] = isproper(sys) also returns an equivalent model sysr with fewer states (reduced order) and a non-singular E matrix. If sys is not proper, sysr = sys.

Examples

Examine Whether Models are Proper

The following commands

```
B1 = isproper(tf([1 0],1)) % transfer function s
B2 = isproper(tf([1 0],[1 1])) % transfer function s/(s+1)
```

return FALSE (logical 0) and TRUE (logical 1), respectively.

Compute Equivalent Lower-Order Model

Combining state-space models sometimes yields results that include more states than necessary. Use *isproper* to compute an equivalent lower-order model.

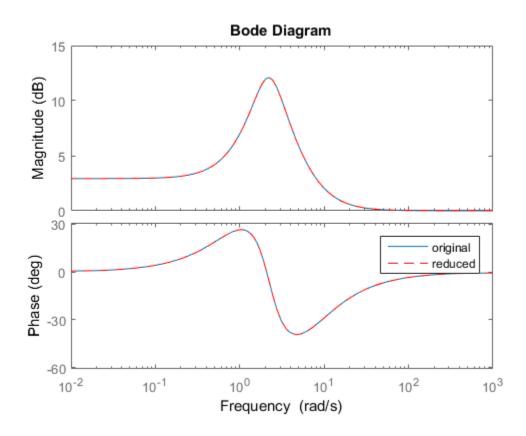
```
H1 = ss(tf([1 1],[1 2 5]));
H2 = ss(tf([1 7],[1]));
H = H1*H2;
size(H)
State-space model with 1 outputs, 1 inputs, and 4 states.
```

H is proper and reducible. isproper returns the reduced model.

```
[isprop,Hr] = isproper(H);
size(Hr)
State-space model with 1 outputs, 1 inputs, and 2 states.
```

H and Hr are equivalent, as a Bode plot demonstrates.

```
bodeplot(H,Hr,'r--')
legend('original','reduced')
```



See Also

Introduced before R2006a

isreal

Determine if model has real-valued coefficients

Syntax

```
B = isreal(sys)
B = isreal(sys,'elem')
```

Description

B = isreal(sys) returns 1 (true) if the model sys has real-valued coefficients, and 0 (false) otherwise. If sys is a model array, then **B** is true if all models in sys have real-valued coefficients.

B = isreal(sys, 'elem') checks each model in the model array sys and returns a logical array of the same size as sys. The logical array indicates which models in sys have real coefficients.

Examples

Check Model for Real-Valued Coefficients

Create model and check whether its coefficients are all real-valued.

```
sys = rss(3);
B = isreal(sys)
B =
1
```

Check Each Model in Array

Create a 1-by-5 array of models and check each model for real-valued coefficients.

sys = rss(2,2,2,1,5); B = isreal(sys, 'elem') B = 1 1 1 1 1

When you use the 'elem' input, isreal checks each model individually and returns a logical array indicating which models have all real-valued coefficients.

Input Arguments

sys – Model or array to check input-output model | model array

Model or array to check, specified as an input-output model or model array. Input-output models include dynamic system models such as numeric LTI models and generalized models. Input-output models also include static models such as tunable parameters or generalized matrices.

Output Arguments

B — Flag indicating whether model has real-valued coefficients

logical | logical array

Flag indicating whether model has real-valued coefficients, returned as a logical value or logical array.

See Also isfinite

Introduced in R2013a

isstable

Determine whether system is stable

Syntax

```
B = isstable(sys)
B = isstable(sys,'elem')
```

Description

B = isstable(sys) returns 1 (true) if the dynamic system model sys has stable dynamics, and 0 (false) otherwise. If sys is a model array, then B is true only if all models in sys are stable.

B = isstable(sys, 'elem') returns a logical array of the same dimensions as the model array sys. The logical array indicates which models in sys are stable.

isstable is only supported for analytical models with a finite number of poles.

Examples

Determine Stability of Models in Model Array

Create an array of SISO transfer function models with poles varying from 2 to -2.

```
a = [-2:2];
sys = tf(zeros(1,1,1,length(a)));
for j = 1:length(a)
        sys(1,1,1,j) = tf(1,[1 a(j)]);
end
```

Examine the stability of the model array.

```
B_all = isstable(sys)
```

B_all =

0

By default, isstable returns a single Boolean value that is 1 (true) only if all models in the array are stable. sys contains some models with nonpositive poles, which are not stable. Therefore, isstable returns 0 (false).

Examine stability of each model in the array, element by element.

The 'elem' flag causes isstable to return an array of Boolean values, which indicate the stability of the corresponding entry in the model array. For example, $B_elem(4) = 1$, which indicates that sys(1,1,1,4) is stable.

See Also

pole

Introduced in R2012a

issiso

Determine if dynamic system model is single-input/single-output (SISO)

Syntax

issiso(sys)

Description

 $\tt issiso(sys) \,$ returns 1 (true) if the dynamic system model $\tt sys$ is SISO and 0 (false) otherwise.

See Also

size | isempty

Introduced before R2006a

isstatic

Determine if model is static or dynamic

Syntax

```
B = isstatic(sys)
B = isstatic(sys,'elem')
```

Description

B = isstatic(sys) returns 1 (true) if the model sys is a static model, and and 0 (false) if sys has dynamics such as states or delays. If sys is a model array, then B is true if all models in sys are static.

 ${\tt B}={\tt isstatic(sys, 'elem')}$ checks each model in the model array sys and returns a logical array of the same size as sys. The logical array indicates which models in sys are static.

Input Arguments

sys — Model or array to check

input-output model | model array

Model or array to check, specified as an input-output model or model array. Input-output models include dynamic system models such as numeric LTI models and generalized models. Input-output models also include static models such as tunable parameters or generalized matrices.

Output Arguments

B - Flag indicating whether input model is static

logical | logical array

Flag indicating whether input model is static, returned as a logical value or logical array.

More About

• "Types of Model Objects"

See Also hasdelay | pole | zero

Introduced in R2013a

kalman

Kalman filter design, Kalman estimator

Syntax

```
[kest,L,P] = kalman(sys,Qn,Rn,Nn)
[kest,L,P] = kalman(sys,Qn,Rn,Nn,sensors,known)
[kest,L,P,M,Z] = kalman(sys,Qn,Rn,...,type)
```

Description

kalman designs a Kalman filter or Kalman state estimator given a state-space model of the plant and the process and measurement noise covariance data. The Kalman estimator provides the optimal solution to the following continuous or discrete estimation problems.

Continuous-Time Estimation

Given the continuous plant

 $\dot{x} = Ax + Bu + Gw$ (state equation) y = Cx + Du + Hw + v (measurement equation)

with known inputs u, white process noise w, and white measurement noise v satisfying

$$E(w) = E(v) = 0, \quad E(ww^T) = Q, \quad E(vv^T) = R, \quad E(wv^T) = N$$

construct a state estimate $\hat{x}(t)$ that minimizes the steady-state error covariance

$$P = \lim_{t \to \infty} E\left(\left\{x - \hat{x}\right\}\left\{x - \hat{x}\right\}^T\right)$$

The optimal solution is the Kalman filter with equations

$$\dot{\hat{x}} = A\hat{x} + Bu + L(y - C\hat{x} - Du)$$
$$\begin{bmatrix} \hat{y} \\ \hat{x} \end{bmatrix} = \begin{bmatrix} C \\ I \end{bmatrix} \hat{x} + \begin{bmatrix} D \\ 0 \end{bmatrix} u$$

The filter gain L is determined by solving an algebraic Riccati equation to be

$$L = (PC^T + \bar{N})\bar{R}^{-1}$$

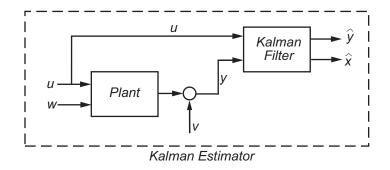
where

$$\bar{R} = R + HN + N^T H^T + HQH^T$$
$$\bar{N} = G(QH^T + N)$$

and P solves the corresponding algebraic Riccati equation.

The estimator uses the known inputs u and the measurements y to generate the output and state estimates \hat{y} and \hat{x} . Note that \hat{y} estimates the true plant output

$$y = Cx + Du + Hw + v$$



Discrete-Time Estimation

Given the discrete plant

$$x[n+1] = Ax[n] + Bu[n] + Gw[n]$$

$$y[n] = Cx[n] + Du[n] + Hw[n] + v[n]$$

and the noise covariance data

$$E(w[n]u[n]^T) = Q, \quad E(v[n]v[n]^T) = R, \quad E(w[n]v[n]^T) = N$$

The estimator has the following state equation:

$$\hat{x}[n+1|n] = A\hat{x}[n|n-1] + Bu[n] + L(y[n] - C\hat{x}[n|n-1] - Du[n])$$

The gain matrix L is derived by solving a discrete Riccati equation to be

$$L = (APC^T + \overline{N})(CPC^T + \overline{R})^{-1}$$

where

$$\bar{R} = R + HN + N^T H^T + HQH^T$$
$$\bar{N} = G(QH^T + N)$$

There are two variants of discrete-time Kalman estimators:

• The current estimator generates output estimates $\hat{y}[n \mid n]$ and state estimates $\hat{x}[n \mid n]$ using all available measurements up to y[n]. This estimator has the output equation

$$\begin{bmatrix} \hat{y}[n \mid n] \\ \hat{x}[n \mid n] \end{bmatrix} = \begin{bmatrix} C(I - MC) \\ I - MC \end{bmatrix} \hat{x}[n \mid n-1] + \begin{bmatrix} (I - CM)D & CM \\ -MD & M \end{bmatrix} \begin{bmatrix} u[n] \\ y[n] \end{bmatrix}$$

where the innovation gain M is defined as

$$M = PC^T (CPC^T + \overline{R})^{-1}$$

M updates the prediction $\hat{x}[n \mid n-1]$ using the new measurement y[n].

$$\hat{x}[n \mid n] = \hat{x}[n \mid n-1] + M(\underbrace{y[n] - C\hat{x}[n \mid n-1] - Du[n]}_{innovation})$$

The delayed estimator generates output estimates $\hat{y}[n | n-1]$ and state estimates $\hat{x}[n | n-1]$ using measurements only up to $y_v[n-1]$. This estimator is easier to implement inside control loops and has the output equation

$$\begin{bmatrix} \hat{y}[n \mid n-1] \\ \hat{x}[n \mid n-1] \end{bmatrix} = \begin{bmatrix} C \\ I \end{bmatrix} \hat{x}[n \mid n-1] + \begin{bmatrix} D & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} u[n] \\ y[n] \end{bmatrix}$$

[kest,L,P] = kalman(sys,Qn,Rn,Nn) creates a state-space model kest of the Kalman estimator given the plant model sys and the noise covariance data Qn, Rn, Nn (matrices Q, R, N described in "Description" on page 1-379). Sys must be a state-space model with matrices A, [BG], C, [DH].

The resulting estimator kest has inputs [u; y] and outputs $[\hat{y}; \hat{x}]$ (or their discrete-time counterparts). You can omit the last input argument Nn when N = 0.

The function kalman handles both continuous and discrete problems and produces a continuous estimator when sys is continuous and a discrete estimator otherwise. In continuous time, kalman also returns the Kalman gain L and the steady-state error covariance matrix P. P solves the associated Riccati equation.

 $[\tt kest, L, P]$ = <code>kalman(sys, Qn, Rn, Nn, sensors, known)</code> handles the more general situation when

- Not all outputs of **sys** are measured.
- The disturbance inputs *w* are not the last inputs of **sys**.

The index vectors sensors and known specify which outputs y of sys are measured and which inputs u are known (deterministic). All other inputs of sys are assumed stochastic.

[kest,L,P,M,Z] = kalman(sys,Qn,Rn,...,type) specifies the estimator type for discrete-time plants sys. The string type is either 'current' (default) or 'delayed'. For discrete-time plants, kalman returns the estimator and innovation gains L and M and the steady-state error covariances

$$P = \lim_{n \to \infty} E(e[n \mid n-1]e[n \mid n-1]^T), \quad e[n \mid n-1] = x[n] - x[n \mid n-1]$$
$$Z = \lim_{n \to \infty} E(e[n \mid n]e[n \mid n]^T), \qquad e[n \mid n] = x[n] - x[n \mid n]$$

Examples

See LQG Design for the x-Axis and Kalman Filtering for examples that use the ${\tt kalman}$ function.

Limitations

The plant and noise data must satisfy:

- (C,A) detectable
- $\bar{R} > 0$ and $\bar{Q} \bar{N}\bar{R}^{-1}\bar{N}^T \ge 0$
- $(A \overline{N}\overline{R}^{-1}C, \overline{Q} \overline{N}\overline{R}^{-1}\overline{N}^T)$ has no uncontrollable mode on the imaginary axis (or unit circle in discrete time) with the notation

$$\begin{split} & \bar{Q} = GQG^T \\ & \bar{R} = R + HN + N^T H^T + HQH^T \\ & \bar{N} = G(QH^T + N) \end{split}$$

References

[1] Franklin, G.F., J.D. Powell, and M.L. Workman, *Digital Control of Dynamic Systems*, Second Edition, Addison-Wesley, 1990.

[2] Lewis, F., Optimal Estimation, John Wiley & Sons, Inc, 1986.

See Also

care | dare | estim | Kalman Filter | kalmd | lqg | lqgreg | ss

Introduced before R2006a

kalmd

Design discrete Kalman estimator for continuous plant

Syntax

```
[kest,L,P,M,Z] = kalmd(sys,Qn,Rn,Ts)
```

Description

kalmd designs a discrete-time Kalman estimator that has response characteristics similar to a continuous-time estimator designed with kalman. This command is useful to derive a discrete estimator for digital implementation after a satisfactory continuous estimator has been designed.

[kest,L,P,M,Z] = kalmd(sys,Qn,Rn,Ts) produces a discrete Kalman estimator kest with sample time Ts for the continuous-time plant

 $\dot{x} = Ax + Bu + Gw$ (state equation) $y_v = Cx + Du + v$ (measurement equation)

with process noise w and measurement noise v satisfying

$$E(w) = E(v) = 0, \quad E(ww^T) = Q_n, \quad E(vv^T) = R_n, \quad E(wv^T) = 0$$

The estimator kest is derived as follows. The continuous plant sys is first discretized using zero-order hold with sample time Ts (see C2d entry), and the continuous noise covariance matrices Q_n and R_n are replaced by their discrete equivalents

$$\begin{aligned} Q_d &= \int_0^{T_s} e^{A\tau} G Q_n G^T e^{A^T \tau} d\tau \\ R_d &= R_n \ / \ T_s \end{aligned}$$

The integral is computed using the matrix exponential formulas in [2]. A discrete-time estimator is then designed for the discretized plant and noise. See kalman for details on discrete-time Kalman estimation.

kalmd also returns the estimator gains L and M, and the discrete error covariance matrices P and Z (see kalman for details).

Limitations

The discretized problem data should satisfy the requirements for kalman.

References

- [1] Franklin, G.F., J.D. Powell, and M.L. Workman, *Digital Control of Dynamic Systems*, Second Edition, Addison-Wesley, 1990.
- [2] Van Loan, C.F., "Computing Integrals Involving the Matrix Exponential," *IEEE Trans. Automatic Control*, AC-15, October 1970.

See Also

kalman | lqrd | lqgreg

Introduced before R2006a

lft

Generalized feedback interconnection of two models (Redheffer star product)

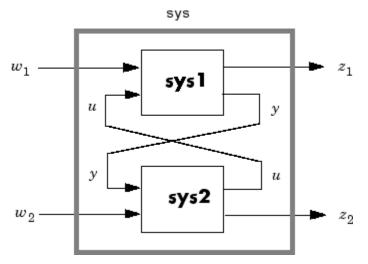
Syntax

```
lft
sys = lft(sys1,sys2,nu,ny)
```

Description

lft forms the star product or linear fractional transformation (LFT) of two model objects or model arrays. Such interconnections are widely used in robust control techniques.

sys = lft(sys1,sys2,nu,ny) forms the star product sys of the two models (or arrays) sys1 and sys2. The star product amounts to the following feedback connection for single models (or for each model in an array).



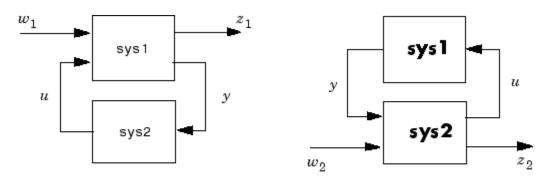
This feedback loop connects the first nu outputs of sys2 to the last nu inputs of sys1 (signals *u*), and the last ny outputs of sys1 to the first ny inputs of sys2 (signals *y*). The resulting system sys maps the input vector $[w_1; w_2]$ to the output vector $[z_1; z_2]$.

The abbreviated syntax

sys = lft(sys1,sys2)

produces:

- The lower LFT of sys1 and sys2 if sys2 has fewer inputs and outputs than sys1. This amounts to deleting w_2 and z_2 in the above diagram.
- The upper LFT of sys1 and sys2 if sys1 has fewer inputs and outputs than sys2. This amounts to deleting w_1 and z_1 in the above diagram.



Lower LFT connection

Upper LFT connection

Limitations

There should be no algebraic loop in the feedback connection.

More About

Algorithms

The closed-loop model is derived by elementary state-space manipulations.

See Also connect | feedback Introduced before R2006a

linearSystemAnalyzer

Linear System Analyzer for LTI system response analysis

Syntax

```
linearSystemAnalyzer
linearSystemAnalyzer(sys1,sys2,...,sysn)
linearSystemAnalyzer(plottype,sys1,sys2,...,sysn)
linearSystemAnalyzer(plottype,sys1,sys2,...,sysn,extras)
H = linearSystemAnalyzer(____)
linearSystemAnalyzer('clear',viewer)
linearSystemAnalyzer('current',sys1,sys2,...,sysn,viewers)
```

Description

linearSystemAnalyzer opens the Linear System Analyzer app. Linear System Analyzer is an interactive user interface for analyzing the time and frequency responses of linear systems and comparing such systems.

linearSystemAnalyzer(sys1,sys2,...,sysn) opens Linear System Analyzer and displays the step response of the LTI models sys1,sys2,...,sysn. You can specify a distinctive color, line style, and marker for each system, as in

```
sys1 = rss(3,2,2);
sys2 = rss(4,2,2);
linearSystemAnalyzer(sys1,'r-*',sys2,'m--');
```

linearSystemAnalyzer(plottype,sys1,sys2,...,sysn) further specifies which responses to display in Linear System Analyzer containing the LTI response type indicated by plottype for the LTI model sys. The string plottype can be any one of the following:

- 'step' Step response.
- 'impulse' Impulse response.
- 'lsim' Linear simulation plot. When you use this plot type, the Linear Simulation Tool dialog opens and prompts you to specify an input signal for the simulation.

- 'initial' Initial condition plot. This plot type is available for state-space models only. When you use this plot type without the extras argument, the Linear Simulation Tool dialog opens and prompts you to specify an initial state for the simulation.
- 'bode' Bode diagram.
- 'bodemag' Bode magnitude diagram.
- 'nyquist' Nyquist plot.
- 'nichols' Nichols plot.
- 'sigma' Singular value plot.
- 'pzmap' Pole/zero map.
- 'iopzmap' I/O pole/zero map.

Alternatively, plottype can be a cell vector containing up to six of these plot types. For example, the following command displays a step response plot and a Nyquist plot for a given system Sys.

```
linearSystemAnalyzer({'step';'nyquist'},sys)
```

linearSystemAnalyzer(plottype,sys1,sys2,...,sysn,extras) allows the additional input arguments supported by the various LTI model response functions to be passed to the linearSystemAnalyzer command.

extras is one or more input arguments as specified by the function named in plottype. These arguments may be required or optional, depending on the type of LTI response. For example, if plottype is 'step', then extras may be the desired final time, Tfinal, as follows:

```
linearSystemAnalyzer('step',sys,Tfinal)
```

However, if plottype is 'initial', then extras must contain the initial conditions x0, and may contain other arguments, such as Tfinal.

```
linearSystemAnalyzer('initial',sys,x0,Tfinal)
```

See the individual references pages of each possible plottype for a list of appropriate arguments for extras. For example, for possible extras values for the bode plot type, see the bode reference page.

H = linearSystemAnalyzer(____) returns the handle to the Linear System Analyzer figure. You can use this syntax with any of the previous combinations of input arguments. Use the handle to modify previously opened Linear System Analyzer figures as described in the next two syntaxes.

linearSystemAnalyzer('clear', viewer) clears the plots and data from the Linear System Analyzer corresponding to handle viewer. To clear multiple Linear System Analyzers at once, set viewer to a vector of handles.

linearSystemAnalyzer('current', sys1, sys2,..., sysn, viewers) adds the responses of the systems sys1, sys2,..., sysn to the Linear System Analyzer corresponding to handle viewer. To update multiple Linear System Analyzers at once, set viewer to a vector of handles. If the new systems do not have the same I/O dimensions as those currently in a specified Linear System Analyzer, the Linear System Analyzer is first cleared and only the new responses are shown.

Alternatives

You can open Linear Analysis Tool from the MATLAB desktop. In the **Apps** tab, in the **Control System Design and Analysis** section of the Apps gallery, click **Linear System Analyzer**.

More About

"Linear System Analyzer Overview"

See Also

bode | impulse | lsim | initial | nichols | nyquist | pzmap | sigma | step

Related Examples

- "Linear Analysis Using the Linear System Analyzer"
- "Joint Time- and Frequency-Domain Analysis"

Introduced in R2015a

lqg

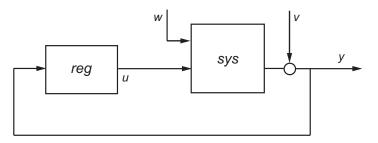
Linear-Quadratic-Gaussian (LQG) design

Syntax

```
reg = lqg(sys,QXU,QWV)
reg = lqg(sys,QXU,QWV,QI)
reg = lqg(sys,QXU,QWV,QI,'1dof')
reg = lqg(sys,QXU,QWV,QI,'2dof')
```

Description

reg = lqg(sys, QXU, QWV) computes an optimal linear-quadratic-Gaussian (LQG) regulator reg given a state-space model sys of the plant and weighting matrices QXU and QWV. The dynamic regulator sys uses the measurements y to generate a control signal u that regulates y around the zero value. Use positive feedback to connect this regulator to the plant output y.



The LQG regulator minimizes the cost function

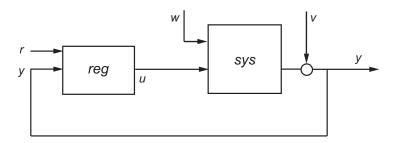
$$J = E\left\{\lim_{\tau \to \infty} \frac{1}{\tau} \int_0^\tau \left[x^T, u^T\right] Q_{xu} \begin{bmatrix} x \\ u \end{bmatrix} dt\right\}$$

subject to the plant equations

dx/dt = Ax + Bu + wy = Cx + Du + v where the process noise w and measurement noise v are Gaussian white noises with covariance:

E([w;v] * [w',v']) = QWV

reg = lqg(sys, QXU, QWV, QI) uses the setpoint command r and measurements y to generate the control signal u. reg has integral action to ensure that y tracks the command r.



The LQG servo-controller minimizes the cost function

$$J = E\left\{\lim_{\tau \to \infty} \frac{1}{\tau} \int_0^{\tau} \left(\left[x^T, u^T \right] Q_{xu} \begin{bmatrix} x \\ u \end{bmatrix} + x_i^T Q_i x_i \right) dt \right\}$$

where x_i is the integral of the tracking error r - y. For MIMO systems, r, y, and x_i must have the same length.

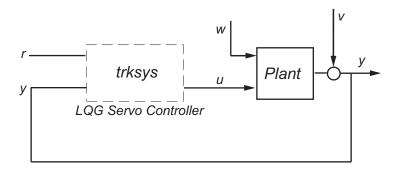
reg = lqg(sys,QXU,QWV,QI, 'ldof') computes a one-degree-of-freedom servo controller that takes e = r - y rather than [r; y] as input.

reg = lqg(sys,QXU,QWV,QI,'2dof') is equivalent to LQG(sys,QXU,QWV,QI) and produces the two-degree-of-freedom servo-controller shown previously.

Examples

Linear-Quadratic-Gaussian (LQG) Regulator and Servo Controller Design

This example shows how to design an linear-quadratic-Gaussian (LQG) regulator, a one-degree-of-freedom LQG servo controller, and a two-degree-of-freedom LQG servo controller for the following system.



The plant has three states (x), two control inputs (u), three random inputs (w), one output (y), measurement noise for the output (v), and the following state and measurement equations.

$$\frac{dx}{dt} = Ax + Bu + w$$
$$y = Cx + Du + v$$

where

$$A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{bmatrix} \qquad B = \begin{bmatrix} 0.3 & 1 \\ 0 & 1 \\ -0.3 & 0.9 \end{bmatrix}$$
$$C = \begin{bmatrix} 1.9 & 1.3 & 1 \end{bmatrix} \qquad D = \begin{bmatrix} 0.53 & -0.61 \end{bmatrix}$$

The system has the following noise covariance data:

$$\begin{aligned} Q_n &= E\left(\omega\omega^T\right) = \begin{bmatrix} 4 & 2 & 0 \\ 2 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \\ R_n &= E\left(\upsilon\upsilon^T\right) = 0.7 \end{aligned}$$

For the regulator, use the following cost function to define the tradeoff between regulation performance and control effort:

lqg

$$J(u) = \int_0^\infty \left(0.1 x^T x + u^T \begin{bmatrix} 1 & 0 \\ 0 & 2 \end{bmatrix} u \right) dt$$

For the servo controllers, use the following cost function to define the tradeoff between tracker performance and control effort:

$$J(u) = \int_0^\infty \left(0.1x^T x + x_i^2 + u^T \begin{bmatrix} 1 & 0 \\ 0 & 2 \end{bmatrix} u \right) dt$$

To design the LQG controllers for this system:

1 Create the state-space system by typing the following in the MATLAB Command Window:

A = [0 1 0;0 0 1;1 0 0]; B = [0.3 1;0 1;-0.3 0.9]; C = [1.9 1.3 1]; D = [0.53 -0.61]; sys = ss(A,B,C,D);

2 Define the noise covariance data and the weighting matrices by typing the following commands:

```
nx = 3; %Number of states
ny = 1; %Number of outputs
Qn = [4 2 0; 2 1 0; 0 0 1];
Rn = 0.7;
R = [1 0;0 2]
QXU = blkdiag(0.1*eye(nx),R);
QWV = blkdiag(Qn,Rn);
QI = eye(ny);
```

3 Form the LQG regulator by typing the following command:

KLQG = lqg(sys,QXU,QWV) This command returns the following LQG regulator:

```
b =
              y1
   x1 e
          2.365
   x2 e
          1.432
   x3_e 0.7684
с =
            x1 e
                         x2 e
                                    х3 е
   u1
        -0.02904
                   0.0008272
                                  0.0303
          -0.7147
   u2
                     -0.7115
                                 -0.7132
d =
       у1
   u1
        0
   u2
        0
Input groups:
       Name
                    Channels
    Measurement
                       1
Output groups:
      Name
                 Channels
    Controls
                   1,2
Continuous-time model.
```

4 Form the one-degree-of-freedom LQG servo controller by typing the following command:

KLQG1 = lqg(sys,QXU,QWV,QI, '1dof')
This command returns the following LQG servo controller:

a = x3_e x1 e x2 e xi1 x1 e -7.626 -5.068 -4.891 0.9018 -4.146 -2.362 x2 e -5.108 0.6762 -2.604 х3 е -2.121 -2.141 0.4088 xi1 0 0 0 0 b = e1 x1_e -2.365 x2 e -1.432 x3_e -0.7684 xi1 1

с = x1 e x2 e х3 е xi1 u1 -0.5388 -0.4173 -0.2481 0.5578 u2 -1.492 -1.388 -1.131 0.5869 d = e1 0 u1 u2 0 Input groups: Name Channels Error 1 Output groups: Channels Name Controls 1,2

- Continuous-time model.
- **5** Form the two-degree-of-freedom LQG servo controller by typing the following command:

KLQG2 = lqg(sys,QXU,QWV,QI,'2dof')
This command returns the following LQG servo controller:

a =					
		x1_e	x2_e	x3_e	xi1
	x1_e	-7.626	-5.068	-4.891	0.9018
	x2_e	-5.108	-4.146	-2.362	0.6762
	x3_e	-2.121	-2.604	-2.141	0.4088
	xi1	0	0	0	0
b =					
		r1	y1		
	x1_e	0	2.365		
	x2_e	0	1.432		
	x3_e	0	0.7684		
	xi1	1	- 1		
C =					
		x1_e	x2_e	x3_e	xi1
	u1 -	0.5388	-0.4173	-0.2481	0.5578
	u2	-1.492	-1.388	-1.131	0.5869

d = r1 y1 0 0 u1 u2 0 0 Input groups: Channels Name Setpoint 1 2 Measurement Output groups: Name Channels Controls 1,2 Continuous-time model.

More About

Tips

lqg can be used for both continuous- and discrete-time plants. In discrete-time, lqg uses x[n | n-1] as state estimate (see kalman for details).

To compute the LQG regulator, lqg uses the commands lqr and kalman. To compute the servo-controller, lqg uses the commands lqi and kalman.

When you want more flexibility for designing regulators you can use the lqr, kalman, and lqgreg commands. When you want more flexibility for designing servo controllers, you can use the lqi, kalman, and lqgtrack commands. For more information on using these commands and how to decide when to use them, see "Linear-Quadratic-Gaussian (LQG) Design for Regulation" and "Linear-Quadratic-Gaussian (LQG) Design of Servo Controller with Integral Action".

See Also

lqr | lqi | kalman | lqry | ss | care | dare

Introduced before R2006a

lqgreg

Form linear-quadratic-Gaussian (LQG) regulator

Syntax

```
rlqg = lqgreg(kest,k)
rlqg = lqgreg(kest,k,controls)
```

Description

lqgreg forms the linear-quadratic-Gaussian (LQG) regulator by connecting the Kalman estimator designed with kalman and the optimal state-feedback gain designed with lqr, dlqr, or lqry. The LQG regulator minimizes some quadratic cost function that trades off regulation performance and control effort. This regulator is dynamic and relies on noisy output measurements to generate the regulating commands.

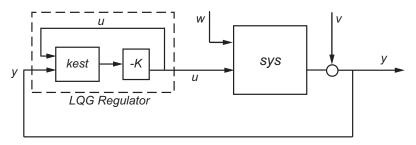
In continuous time, the LQG regulator generates the commands

 $u = -K\hat{x}$

where \hat{x} is the Kalman state estimate. The regulator state-space equations are

$$\dot{\hat{x}} = [A - LC - (B - LD)K]\hat{x} + Ly$$
$$u = -K\hat{x}$$

where y is the vector of plant output measurements (see kalman for background and notation). The following diagram shows this dynamic regulator in relation to the plant.



In discrete time, you can form the LQG regulator using either the delayed state estimate $\hat{x}[n \mid n-1]$ of x[n], based on measurements up to y[n-1], or the current state estimate $\hat{x}[n \mid n]$, based on all available measurements including y[n]. While the regulator

$$u[n] = -K\hat{x}[n \mid n-1]$$

is always well-defined, the current regulator

$$u[n] = -K\hat{x}[n \mid n]$$

is causal only when *I-KMD* is invertible (see kalman for the notation). In addition, practical implementations of the current regulator should allow for the processing time required to compute u[n] after the measurements y[n] become available (this amounts to a time delay in the feedback loop).

Examples

See the example LQG Regulation.

More About

Tips

rlqg = lqgreg(kest,k) returns the LQG regulator rlqg (a state-space model) given the Kalman estimator kest and the state-feedback gain matrix k. The same function handles both continuous- and discrete-time cases. Use consistent tools to design kest and k:

- Continuous regulator for continuous plant: use lqr or lqry and kalman
- Discrete regulator for discrete plant: use dlqr or lqry and kalman
- Discrete regulator for continuous plant: use lqrd and kalmd

In discrete time, lqgreg produces the regulator

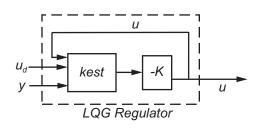
• $u[n] = -K\hat{x}[n \mid n]$ when kest is the "current" Kalman estimator

• $u[n] = -K\hat{x}[n \mid n-1]$ when kest is the "delayed" Kalman estimator

For more information on Kalman estimators, see the kalman reference page.

rlqg = lqgreg(kest, k, controls) handles estimators that have access to additional deterministic known plant inputs u_d . The index vector controls then specifies which estimator inputs are the controls u, and the resulting LQG regulator rlqg has u_d and y as inputs (see the next figure).

Note Always use *positive* feedback to connect the LQG regulator to the plant.



See Also

kalman | kalmd | lqr | dlqr | lqrd | lqry | reg

Introduced before R2006a

lqgtrack

Form Linear-Quadratic-Gaussian (LQG) servo controller

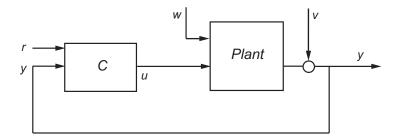
Syntax

```
C = lqgtrack(kest,k)
```

- C = lqgtrack(kest,k,'2dof')
- C = lqgtrack(kest,k,'1dof')
- C = lqgtrack(kest,k,...CONTROLS)

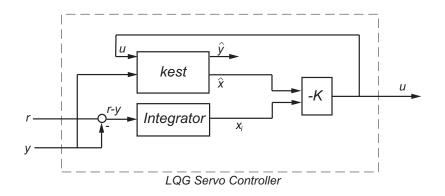
Description

lqgtrack forms a Linear-Quadratic-Gaussian (LQG) servo controller with integral action for the loop shown in the following figure. This compensator ensures that the output y tracks the reference command r and rejects process disturbances w and measurement noise v. lqgtrack assumes that r and y have the same length.



Note: Always use positive feedback to connect the LQG servo controller *C* to the plant output *y*.

C = lqgtrack(kest,k) forms a two-degree-of-freedom LQG servo controller C by connecting the Kalman estimator kest and the state-feedback gain k, as shown in the following figure. C has inputs [r;y] and generates the command $u = -K[\hat{x};x_i]$, where \hat{x} is the Kalman estimate of the plant state, and x_i is the integrator output.



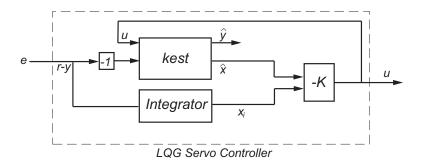
The size of the gain matrix k determines the length of x_i . x_i , y, and r all have the same length.

The two-degree-of-freedom LQG servo controller state-space equations are

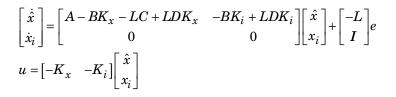
$$\begin{bmatrix} \dot{x} \\ \dot{x}_i \end{bmatrix} = \begin{bmatrix} A - BK_x - LC + LDK_x & -BK_i + LDK_i \\ 0 & 0 \end{bmatrix} \begin{bmatrix} \hat{x} \\ x_i \end{bmatrix} + \begin{bmatrix} 0 & L \\ I & -I \end{bmatrix} \begin{bmatrix} r \\ y \end{bmatrix}$$
$$u = \begin{bmatrix} -K_x & -K_i \end{bmatrix} \begin{bmatrix} \hat{x} \\ x_i \end{bmatrix}$$

Note: The syntax C = lqgtrack(kest,k,'2dof') is equivalent to C = lqgtrack(kest,k).

C = lqgtrack(kest,k,'ldof') forms a one-degree-of-freedom LQG servo controller C that takes the tracking error e = r - y as input instead of [r; y], as shown in the following figure.



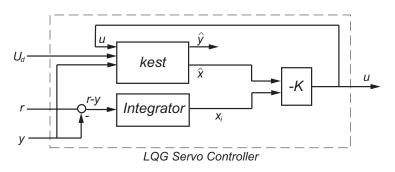
The one-degree-of-freedom LQG servo controller state-space equations are



C = lqgtrack(kest,k,...CONTROLS) forms an LQG servo controller C when the Kalman estimator kest has access to additional known (deterministic) commands U_d of the plant. In the index vector CONTROLS, specify which inputs of kest are the control channels u. The resulting compensator C has inputs

- $[U_d; r; y]$ in the two-degree-of-freedom case
- $[U_d; e]$ in the one-degree-of-freedom case

The corresponding compensator structure for the two-degree-of-freedom cases appears in the following figure.



Examples

See the example "Design an LQG Servo Controller".

More About

Tips

You can use lqgtrack for both continuous- and discrete-time systems.

In discrete-time systems, integrators are based on forward Euler (see lqi for details). The state estimate \hat{x} is either $x[n \mid n]$ or $x[n \mid n-1]$, depending on the type of estimator (see kalman for details).

See Also

lqg | lqi | kalman | lqr | lqgreg

Introduced in R2008b

lqi

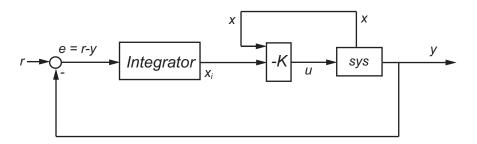
Linear-Quadratic-Integral control

Syntax

[K,S,e] = lqi(SYS,Q,R,N)

Description

lqi computes an optimal state-feedback control law for the tracking loop shown in the following figure.



For a plant sys with the state-space equations (or their discrete counterpart):

$$\frac{dx}{dt} = Ax + Bu$$
$$y = Cx + Du$$

the state-feedback control is of the form

$$u = -K[x; x_i]$$

where x_i is the integrator output. This control law ensures that the output y tracks the reference command r. For MIMO systems, the number of integrators equals the dimension of the output y.

[K,S,e] = lqi(SYS,Q,R,N) calculates the optimal gain matrix K, given a statespace model SYS for the plant and weighting matrices Q, R, N. The control law $u = -Kz = -K[x;x_i]$ minimizes the following cost functions (for r = 0)

$$J(u) = \int_0^\infty \{z^T Q z + u^T R u + 2z^T N u\} dt \text{ for continuous time}$$
$$J(u) = \sum_{n=0}^\infty \{z^T Q z + u^T R u + 2z^T N u\} \text{ for discrete time}$$

In discrete time, 1qi computes the integrator output x_i using the forward Euler formula

$$x_i[n+1] = x_i[n] + Ts(r[n] - y[n])$$

where *Ts* is the sample time of SYS.

When you omit the matrix N, N is set to 0. 1qi also returns the solution S of the associated algebraic Riccati equation and the closed-loop eigenvalues e.

Limitations

For the following state-space system with a plant with augmented integrator:

$$\frac{\delta z}{\delta t} = A_a z + B_a u$$
$$y = C_a z + D_a u$$

The problem data must satisfy:

• The pair (A_a, B_a) is stabilizable.

$$R > 0$$
 and $Q - NR^{-1}N^T \ge 0$.

• $(Q - NR^{-1}N^T, A_a - B_aR^{-1}N^T)$ has no unobservable mode on the imaginary axis (or unit circle in discrete time).

More About

Tips

lqi supports descriptor models with nonsingular E. The output S of lqi is the solution of the Riccati equation for the equivalent explicit state-space model

$$\frac{dx}{dt} = E^{-1}Ax + E^{-1}Bu$$

References

 P. C. Young and J. C. Willems, "An approach to the linear multivariable servomechanism problem", *International Journal of Control*, Volume 15, Issue 5, May 1972, pages 961–979.

See Also

lqr | lqgreg | lqg | care | dare | lqgtrack

Introduced in R2008b

lqr

Linear-Quadratic Regulator (LQR) design

Syntax

[K,S,e] = lqr(SYS,Q,R,N)[K,S,e] = LQR(A,B,Q,R,N)

Description

[K,S,e] = lqr(SYS,Q,R,N) calculates the optimal gain matrix K.

For a continuous time system, the state-feedback law u = -Kx minimizes the quadratic cost function

$$J(u) = \int_0^\infty (x^T Q x + u^T R u + 2x^T N u) dt$$

subject to the system dynamics

$$\dot{x} = Ax + Bu.$$

In addition to the state-feedback gain K, 1qr returns the solution S of the associated Riccati equation

$$A^{T}S + SA - (SB + N)R^{-1}(B^{T}S + N^{T}) + Q = 0$$

and the closed-loop eigenvalues e = eig(A-B*K). K is derived from S using

$$K = R^{-1}(B^T S + N^T)$$

For a discrete-time state-space model, u[n] = -Kx[n] minimizes

$$J = \sum_{n=0}^{\infty} \{ x^T Q x + u^T R u + 2x^T N u \}$$

subject to x[n + 1] = Ax[n] + Bu[n].

[K,S,e] = LQR(A,B,Q,R,N) is an equivalent syntax for continuous-time models with dynamics $\dot{x} = Ax + Bu$.

In all cases, when you omit the matrix N, N is set to 0.

Limitations

The problem data must satisfy:

- The pair (*A*,*B*) is stabilizable.
- $R > 0 \text{ and } Q NR^{-1}N^T \ge 0.$
- $(Q NR^{-1}N^T, A BR^{-1}N^T)$ has no unobservable mode on the imaginary axis (or unit circle in discrete time).

More About

Tips

lqr supports descriptor models with nonsingular *E*. The output S of lqr is the solution of the Riccati equation for the equivalent explicit state-space model:

$$\frac{dx}{dt} = E^{-1}Ax + E^{-1}Bu$$

See Also

care | dlqr | lqgreg | lqrd | lqry | lqi

Introduced before R2006a

lqrd

Design discrete linear-quadratic (LQ) regulator for continuous plant

Syntax

lqrd
[Kd,S,e] = lqrd(A,B,Q,R,Ts)
[Kd,S,e] = lqrd(A,B,Q,R,N,Ts)

Description

lqrd designs a discrete full-state-feedback regulator that has response characteristics similar to a continuous state-feedback regulator designed using lqr. This command is useful to design a gain matrix for digital implementation after a satisfactory continuous state-feedback gain has been designed.

[Kd,S,e] = lqrd(A,B,Q,R,Ts) calculates the discrete state-feedback law

 $u[n] = -K_d x[n]$

that minimizes a discrete cost function equivalent to the continuous cost function

$$J = \int_0^\infty (x^T Q x + u^T R u) dt$$

The matrices A and B specify the continuous plant dynamics

 $\dot{x} = Ax + Bu$

and Ts specifies the sample time of the discrete regulator. Also returned are the solution S of the discrete Riccati equation for the discretized problem and the discrete closed-loop eigenvalues e = eig(Ad-Bd*Kd).

[Kd,S,e] = lqrd(A,B,Q,R,N,Ts) solves the more general problem with a crosscoupling term in the cost function.

$$J = \int_0^\infty \left(x^T Q x + u^T R u + 2x^T N u \right) dt$$

Limitations

The discretized problem data should meet the requirements for dlqr.

More About

Algorithms

The equivalent discrete gain matrix Kd is determined by discretizing the continuous plant and weighting matrices using the sample time Ts and the zero-order hold approximation.

With the notation

$$\begin{split} \Phi(\tau) &= e^{A\tau} \,, \qquad A_d = \Phi(T_s) \\ \Gamma(\tau) &= \int_0^\tau e^{A\eta} B d\eta, \quad B_d = \Gamma(T_s) \end{split}$$

the discretized plant has equations

$$x[n+1] = A_d x[n] + B_d u[n]$$

and the weighting matrices for the equivalent discrete cost function are

$$\begin{bmatrix} Q_d & N_d \\ N_d^T & R_d \end{bmatrix} = \int_0^{T_s} \begin{bmatrix} \Phi^T(\tau) & 0 \\ \Gamma^T(\tau) & I \end{bmatrix} \begin{bmatrix} Q & N \\ N^T & R \end{bmatrix} \begin{bmatrix} \Phi(\tau) & \Gamma(\tau) \\ 0 & I \end{bmatrix} d\tau$$

The integrals are computed using matrix exponential formulas due to Van Loan (see [2]). The plant is discretized using c2d and the gain matrix is computed from the discretized data using dlqr.

References

- [1] Franklin, G.F., J.D. Powell, and M.L. Workman, *Digital Control of Dynamic Systems*, Second Edition, Addison-Wesley, 1980, pp. 439-440.
- [2] Van Loan, C.F., "Computing Integrals Involving the Matrix Exponential," *IEEE Trans. Automatic Control*, AC-23, June 1978.

See Also

c2d | dlqr | kalmd | lqr

Introduced before R2006a

lqry

Form linear-quadratic (LQ) state-feedback regulator with output weighting

Syntax

[K,S,e] = lqry(sys,Q,R,N)

Description

Given the plant

$$\dot{x} = Ax + Bu$$
$$y = Cx + Du$$

or its discrete-time counterpart, lqry designs a state-feedback control

$$u = -Kx$$

that minimizes the quadratic cost function with output weighting

$$J(u) = \int_0^\infty (y^T Q y + u^T R u + 2y^T N u) dt$$

(or its discrete-time counterpart). The function lqry is equivalent to lqr or dlqr with weighting matrices:

$$\begin{bmatrix} \bar{Q} & \bar{N} \\ \bar{N}^T & \bar{R} \end{bmatrix} = \begin{bmatrix} C^T & 0 \\ D^T & I \end{bmatrix} \begin{bmatrix} Q & N \\ N^T & R \end{bmatrix} \begin{bmatrix} C & D \\ 0 & I \end{bmatrix}$$

[K,S,e] = lqry(sys,Q,R,N) returns the optimal gain matrix K, the Riccati solution S, and the closed-loop eigenvalues e = eig(A-B*K). The state-space model sys specifies the continuous- or discrete-time plant data (A, B, C, D). The default value N=0 is assumed when N is omitted.

Examples

See LQG Design for the x-Axis for an example.

Limitations

The data $A, B, \overline{Q}, \overline{R}, \overline{N}$ must satisfy the requirements for lqr or dlqr.

See Also lqr | dlqr | kalman | lqgreg

Introduced before R2006a

lsim

Simulate time response of dynamic system to arbitrary inputs

Syntax

```
lsim(sys,u,t)
lsim(sys,u,t,x0)
lsim(sys,u,t,x0,method)
lsim(sys1,...,sysn,u,t)
lsim(sys1,PlotStyle1,...,sysN,PlotStyleN,u,t)
y = lsim(___)
[y,t,x] = lsim(___)
lsim(sys)
```

Description

lsim simulates the (time) response of continuous or discrete linear systems to arbitrary inputs. When invoked without left-hand arguments, lsim plots the response on the screen.

lsim(sys,u,t) produces a plot of the time response of the dynamic system model sys
to the input history, t,u. The vector t specifies the time samples for the simulation (in
system time units, specified in the TimeUnit property of sys), and consists of regularly
spaced time samples:

t = 0:dt:Tfinal

The input u is an array having as many rows as time samples (length(t)) and as many columns as system inputs. For instance, if sys is a SISO system, then u is a t-by-1 vector. If sys has three inputs, then u is a t-by-3 array. Each row u(i,:) specifies the input value(s) at the time sample t(i). The signal u also appears on the plot.

The model sys can be continuous or discrete, SISO or MIMO. In discrete time, u must be sampled at the same rate as the system. In this case, the input t is redundant and can be omitted or set to an empty matrix. In continuous time, the time sampling dt = t(2)-

t(1) is used to discretize the continuous model. If dt is too large (undersampling), lsim issues a warning suggesting that you use a more appropriate sample time, but will use the specified sample time. See "Algorithms" on page 1-420 for a discussion of sample times.

lsim(sys,u,t,x0) further specifies an initial condition x0 for the system states. This syntax applies only when sys is a state-space model. x0 is a vector whose entries are the initial values of the corresponding states of sys.

lsim(sys,u,t,x0,method) explicitly specifies how the input values should be interpolated between samples, when sys is a continuous-time system. The string method can take one of the following values:

- 'zoh' Use zero-order hold
- 'foh' Use linear interpolation (first-order hold)

If you do not specify a method, lsim selects the interpolation method automatically based on the smoothness of the signal u.

lsim(sys1,...,sysn,u,t) simulates the responses of several dynamic system models to the same input history t,u and plots these responses on a single figure. You can also use the xO and method input arguments when computing the responses of multiple models.

lsim(sys1,PlotStyle1,...,sysN,PlotStyleN,u,t) specifies the line style, marker, and color of each of the system responses in the plot. (You can also use the x0 and method input arguments with this syntax.) Each PlotStyle entry is a one-part, two-part, or three-part string enclosed in single quotes (' '). The elements of the string can appear in any order. The string can specify only the line style, the marker, or the color. For example, the following code plots the response of sys1 as a yellow dotted line and the response of sys2 as a green dashed line:

lsim(sys1,'y:',sys2,'g--',u,t,x0)

For more information about configuring the PlotStyle string, see "Specify Line Style, Color, and Markers" in the MATLAB documentation.

 $y = lsim(___)$ returns the system response y, sampled at the same times as the input (t). The output y is an array having as many rows as time samples (length(t)) and as many columns as system outputs. No plot is drawn on the screen. You can use

this syntax with any of the input arguments described in previous syntaxes except the PlotStyle strings.

 $[y,t,x] = lsim(___)$ also returns the time vector t used for simulation and the state trajectories x (for state-space models only). The output x has as many rows as time samples (length(t)) and as many columns as system states. You can use this syntax with any of the input arguments described in previous syntaxes except the PlotStyle strings.

lsim(sys) opens the Linear Simulation Tool GUI. For more information about working with this GUI, see Working with the Linear Simulation Tool.

Examples

Simulate Response to Square Wave

Simulate and plot the response of the following system to a square wave with period of four seconds:

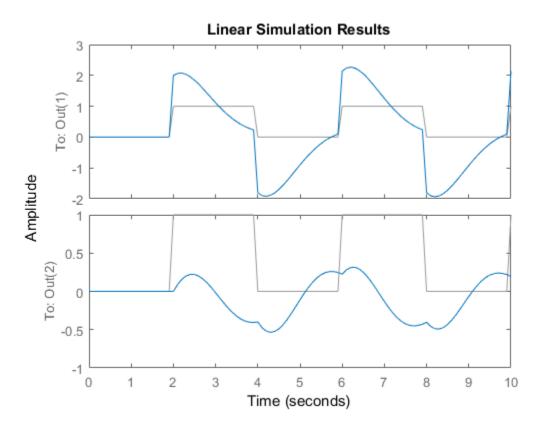
$$H(s) = \begin{bmatrix} \frac{2s^2 + 5s + 1}{s^2 + 2s + 3} \\ \frac{s - 1}{s^2 + s + 5} \end{bmatrix}.$$

Create the transfer function, and generate the square wave with gensig. Sample every 0.1 second during 10 seconds.

H = [tf([2 5 1],[1 2 3]);tf([1 -1],[1 1 5])]; [u,t] = gensig('square',4,10,0.1);

Then simulate with lsim.

lsim(H,u,t)



The plot displays both the applied signal and the response.

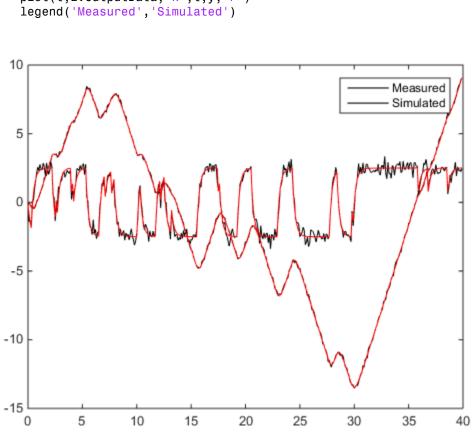
Simulate Response of Identified Model

Simulate the response of an identified linear model using the same input signal as the one used for estimation and the initial states returned by the estimation command.

```
load(fullfile(matlabroot,'toolbox','ident','iddemos','data','dcmotordata'));
z = iddata(y,u,0.1,'Name','DC-motor');
```

```
[sys,x0] = n4sid(z,4);
[y,t,x] = lsim(sys, z.InputData, [], x0);
```

Compare the simulated response y to measured response z.OutputData.



plot(t,z.OutputData,'k',t,y,'r')

More About

Algorithms

Discrete-time systems are simulated with ltitr (state space) or filter (transfer function and zero-pole-gain).

Continuous-time systems are discretized with c2d using either the 'zoh' or 'foh' method ('foh' is used for smooth input signals and 'zoh' for discontinuous signals such as pulses or square waves). The sample time is set to the spacing dt between the user-supplied time samples t.

The choice of sample time can drastically affect simulation results. To illustrate why, consider the second-order model

$$H(s) = \frac{\omega^2}{s^2 + 2s + \omega^2}, \quad \omega = 62.83$$

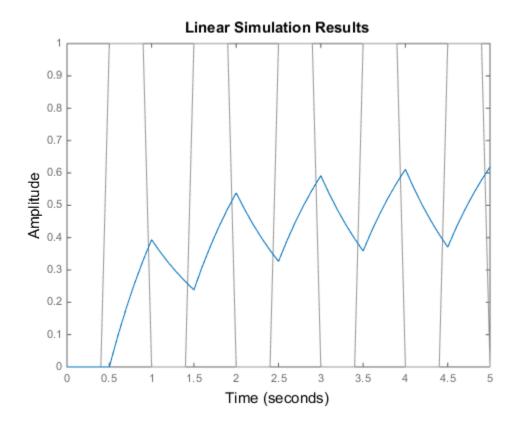
To simulate its response to a square wave with period 1 second, you can proceed as follows:

w2 = 62.83^2; h = tf(w2,[1 2 w2]); t = 0:0.1:5; u = (rem(t,1) >= 0.5); lsim(h,u,t)

% vector of time samples % square wave values

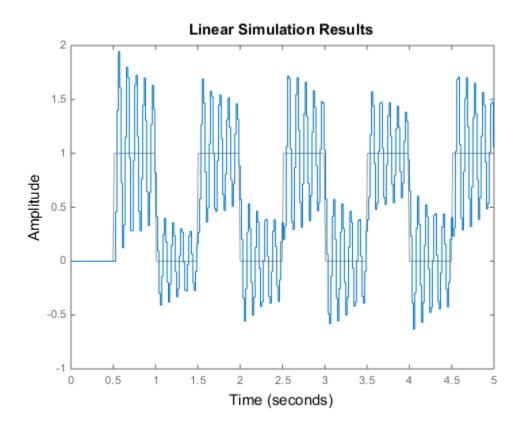
lsim evaluates the specified sample time, and issues a warning:

Warning: Input signal is undersampled. Sample every 0.016 sec or faster.



To improve on this response, discretize H(s) using the recommended sample time:

```
dt = 0.016;
ts = 0:dt:5;
us = (rem(ts,1) >= 0.5);
hd = c2d(h,dt);
lsim(hd,us,ts)
```



This response exhibits strong oscillatory behavior that is hidden in the undersampled version.

See Also

gensig | initial | step | lsiminfo | impulse | linearSystemAnalyzer | sim

Introduced before R2006a

lsiminfo

Compute linear response characteristics

Syntax

```
S = lsiminfo(y,t,yfinal)
S = lsiminfo(y,t)
S = lsiminfo(...,'SettlingTimeThreshold',ST)
```

Description

S = lsiminfo(y,t,yfinal) takes the response data (t,y) and a steady-state value yfinal and returns a structure S containing the following performance indicators:

- SettlingTime Settling time
- Min Minimum value of Y
- MinTime Time at which the min value is reached
- Max Maximum value of Y
- MaxTime Time at which the max value is reached

For SISO responses, t and y are vectors with the same length NS. For responses with NY outputs, you can specify y as an NS-by-NY array and yfinal as a NY-by-1 array. lsiminfo then returns an NY-by-1 structure array S of performance metrics for each output channel.

S = lsiminfo(y,t) uses the last sample value of y as steady-state value yfinal.s = lsiminfo(y) assumes t = 1:NS.

S = lsiminfo(..., 'SettlingTimeThreshold', ST) lets you specify the threshold ST used in the settling time calculation. The response has settled when the error |y(t) - yfinal| becomes smaller than a fraction ST of its peak value. The default value is ST=0.02 (2%).

Examples

Create a fourth order transfer function and ascertain the response characteristics.

```
sys = tf([1 -1],[1 2 3 4]);
[y,t] = impulse(sys);
s = lsiminfo(y,t,0) % final value is 0
s =
SettlingTime: 22.8626
Min: -0.4270
MinTime: 2.0309
Max: 0.2845
MaxTime: 4.0619
```

See Also

impulse | stepinfo | lsim | initial

Introduced in R2006a

lsimplot

Simulate response of dynamic system to arbitrary inputs and return plot handle

Syntax

```
h = lsimplot(sys)
lsimplot(sys1,sys2,...)
lsimplot(sys,u,t)
lsimplot(sys,u,t,x0)
lsimplot(sys1,sys2,...,u,t,x0)
lsimplot(AX,...)
lsimplot(..., plotoptions)
lsimplot(sys,u,t,x0,'zoh')
lsimplot(sys,u,t,x0,'foh')
```

Description

h = lsimplot(sys) opens the Linear Simulation Tool for the dynamic system model sys, which enables interactive specification of driving input(s), the time vector, and initial state. It also returns the plot handle h. You can use this handle to customize the plot with the getoptions and setoptions commands. Type

help timeoptions

for a list of available plot options.

lsimplot(sys1,sys2,...) opens the Linear Simulation Tool for multiple models sys1,sys2,.... Driving inputs are common to all specified systems but initial conditions can be specified separately for each.

lsimplot(sys,u,t) plots the time response of the model sys to the input signal described by u and t. The time vector t consists of regularly spaced time samples (in system time units, specified in the TimeUnit property of sys). For MIMO systems, u is a matrix with as many columns as inputs and whose ith row specifies the input value at time t(i). For SISO systems u can be specified either as a row or column vector. For example, t = 0:0.01:5; u = sin(t); lsimplot(sys,u,t)

simulates the response of a single-input model sys to the input u(t)=sin(t) during 5 seconds.

For discrete-time models, u should be sampled at the same rate as sys (t is then redundant and can be omitted or set to the empty matrix).

For continuous-time models, choose the sampling period t(2) - t(1) small enough to accurately describe the input U. lsim issues a warning when U is undersampled, and hidden oscillations can occur.

lsimplot(sys,u,t,x0) specifies the initial state vector x0 at time t(1) (for state-space models only). x0 is set to zero when omitted.

lsimplot(sys1,sys2,...,u,t,x0) simulates the responses of multiple LTI models sys1,sys2,... on a single plot. The initial condition x0 is optional. You can also specify a color, line style, and marker for each system, as in

```
lsimplot(sys1,'r',sys2,'y--',sys3,'gx',u,t)
```

lsimplot(AX,...) plots into the axes with handle AX.

lsimplot(..., plotoptions) plots the initial condition response with the options
specified in plotoptions. Type

help timeoptions

for more detail.

For continuous-time models, lsimplot(sys,u,t,x0, 'zoh') or lsimplot(sys,u,t,x0, 'foh') explicitly specifies how the input values should be interpolated between samples (zero-order hold or linear interpolation). By default, lsimplot selects the interpolation method automatically based on the smoothness of the signal u.

See Also

lsim | setoptions | getoptions

Introduced before R2006a

ltiblock.gain

Tunable static gain block

Syntax

```
blk = ltiblock.gain(name,Ny,Nu)
blk = ltiblock.gain(name,G)
```

Description

Model object for creating tunable static gains. ltiblock.gain lets you parametrize tunable static gains for parameter studies or for automatic tuning with Robust Control Toolbox tuning commands such as systume or looptune.

ltiblock.gain is part of the Control Design Block family of parametric models. Other Control Design Blocks include ltiblock.pid, ltiblock.ss, and ltiblock.tf.

Construction

blk = ltiblock.gain(name,Ny,Nu) creates a parametric static gain block named name. This block has Ny outputs and Nu inputs. The tunable parameters are the gains across each of the Ny-by-Nu I/O channels.

blk = ltiblock.gain(name,G) uses the double array G to dimension the block and initialize the tunable parameters.

Input Arguments

name

String specifying the block Name. (See "Properties" on page 1-429.)

Ny

Non-negative integer specifying the number of outputs of the parametric static gain block blk.

Nu

Non-negative integer specifying the number of inputs of the parametric static gain block blk.

G

Double array of static gain values. The number of rows and columns of G determine the number of inputs and outputs of blk. The entries G are the initial values of the parametric gain block parameters.

Properties

Gain

Parametrization of the tunable gain.

blk.Gain is a param.Continuous object. For general information about the properties of the param.Continuous object blk.Gain, see the param.Continuous object reference page.

The following fields of blk.Gain are used when you tune blk using hinfstruct:

Field	Description
Value	Current value of the gain matrix. For a block that has Ny outputs and Nu inputs, blk.Gain.Value is a Ny-by-Nu matrix. If you use the G input argument to create blk, blk.Gain.Value initializes to the values of G. Otherwise, all entries of blk.Gain.Value initialize to zero. hinfstruct tunes all entries in blk.Gain.Value except those whose values are fixed by blk.Gain.Free. Default: Array of zero values.
Free	Array of logical values determining whether the gain entries in

Field	Description
	 blk.Gain.Value are fixed or free parameters. If blk.Gain.Free(i,j) = 1, then blk.Gain.Value(i,j) is a tunable parameter. If blk.Gain.Free(i,j) = 0, then blk.Gain.Value(i,j) is fixed.
Minimum	Default: Array of 1 (true) values. Minimum value of the parameter. This property places a lower bound on the tuned value of the parameter. For example, setting blk.Gain.Minimum = 1 ensures that all entries in the gain matrix have gain greater than 1. Default: -Inf.
Maximum	Maximum value of the parameter. This property places an upper bound on the tuned value of the parameter. For example, setting blk.Gain.Maximum = 100 ensures that all entries in the gain matrix have gain less than 100. Default: Inf.

Ts

Sample time. For continuous-time models, Ts = 0. For discrete-time models, Ts is a positive scalar representing the sampling period. This value is expressed in the unit specified by the TimeUnit property of the model. To denote a discrete-time model with unspecified sample time, set Ts = -1.

Changing this property does not discretize or resample the model. Use c2d and d2c to convert between continuous- and discrete-time representations. Use d2d to change the sample time of a discrete-time system.

Default: 0 (continuous time)

TimeUnit

String representing the unit of the time variable. This property specifies the units for the time variable, the sample time Ts, and any time delays in the model. Use any of the following values:

- 'nanoseconds'
- 'microseconds'
- 'milliseconds'
- 'seconds'
- 'minutes'
- 'hours'
- 'days'
- 'weeks'
- 'months'
- 'years'

Changing this property has no effect on other properties, and therefore changes the overall system behavior. Use chgTimeUnit to convert between time units without modifying system behavior.

Default: 'seconds'

InputName

Input channel names. Set InputName to a string for single-input model. For a multiinput model, set InputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign input names for multi-input models. For example, if **sys** is a two-input model, enter:

sys.InputName = 'controls';

The input names automatically expand to { 'controls(1) '; 'controls(2) '}.

You can use the shorthand notation u to refer to the InputName property. For example, sys.u is equivalent to sys.InputName.

Input channel names have several uses, including:

- · Identifying channels on model display and plots
- · Extracting subsystems of MIMO systems
- · Specifying connection points when interconnecting models

Default: Empty string ' ' for all input channels

InputUnit

Input channel units. Use InputUnit to keep track of input signal units. For a singleinput model, set InputUnit to a string. For a multi-input model, set InputUnit to a cell array of strings. InputUnit has no effect on system behavior.

Default: Empty string ' ' for all input channels

InputGroup

Input channel groups. The InputGroup property lets you assign the input channels of MIMO systems into groups and refer to each group by name. Specify input groups as a structure. In this structure, field names are the group names, and field values are the input channels belonging to each group. For example:

```
sys.InputGroup.controls = [1 2];
sys.InputGroup.noise = [3 5];
```

creates input groups named controls and noise that include input channels 1, 2 and 3, 5, respectively. You can then extract the subsystem from the controls inputs to all outputs using:

```
sys(:,'controls')
```

Default: Struct with no fields

OutputName

Output channel names. Set OutputName to a string for single-output model. For a multioutput model, set OutputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign output names for multi-output models. For example, if **sys** is a two-output model, enter:

```
sys.OutputName = 'measurements';
```

```
The output names automatically expand to { 'measurements(1) '; 'measurements(2) '}.
```

You can use the shorthand notation y to refer to the OutputName property. For example, sys.y is equivalent to sys.OutputName.

Output channel names have several uses, including:

- · Identifying channels on model display and plots
- Extracting subsystems of MIMO systems
- Specifying connection points when interconnecting models

Default: Empty string ' ' for all output channels

OutputUnit

Output channel units. Use OutputUnit to keep track of output signal units. For a single-output model, set OutputUnit to a string. For a multi-output model, set OutputUnit to a cell array of strings. OutputUnit has no effect on system behavior.

Default: Empty string ' ' for all output channels

OutputGroup

Output channel groups. The OutputGroup property lets you assign the output channels of MIMO systems into groups and refer to each group by name. Specify output groups as a structure. In this structure, field names are the group names, and field values are the output channels belonging to each group. For example:

```
sys.OutputGroup.temperature = [1];
sys.InputGroup.measurement = [3 5];
```

creates output groups named temperature and measurement that include output channels 1, and 3, 5, respectively. You can then extract the subsystem from all inputs to the measurement outputs using:

```
sys('measurement',:)
```

Default: Struct with no fields

Name

System name. Set Name to a string to label the system.

Default: ' '

Notes

Any text that you want to associate with the system. Set **Notes** to a string or a cell array of strings.

Default: { }

UserData

Any type of data you want to associate with system. Set UserData to any MATLAB data type.

Default: []

Examples

Create a 2-by-2 parametric gain block of the form

$$\begin{bmatrix} g_1 & 0 \\ 0 & g_2 \end{bmatrix}$$

where g_1 and g_2 are tunable parameters, and the off-diagonal elements are fixed to zero.

```
blk = ltiblock.gain('gainblock',2,2); % 2 outputs, 2 inputs
blk.Gain.Free = [1 0; 0 1]; % fix off-diagonal entries to zero
```

All entries in **blk.Gain.Value** initialize to zero. Initialize the diagonal values to 1 as follows.

```
blk.Gain.Value = eye(2); % set diagonals to 1
```

Create a two-input, three-output parametric gain block and initialize all the parameter values to 1.

To do so, create a matrix to dimension the parametric gain block and initialize the parameter values.

```
G = ones(3,2);
blk = ltiblock.gain('gainblock',G);
```

Create a 2-by-2 parametric gain block and assign names to the inputs.

```
blk = ltiblock.gain('gainblock',2,2) % 2 outputs, 2 inputs
blk.InputName = {'Xerror', 'Yerror'} % assign input names
```

More About

Tips

- Use the blk.Gain.Free field of blk to specify additional structure or fix the values of specific entries in the block. To fix the gain value from input i to output j, set blk.Gain.Free(i,j) = 0. To allow hinfstruct to tune this gain value, set blk.Gain.Free(i,j) = 1.
- To convert an ltiblock.gain parametric model to a numeric (non-tunable) model object, use model commands such as tf, zpk, or ss.
- "Control Design Blocks"
- "Models with Tunable Coefficients"

See Also

ltiblock.pid | ltiblock.pid2 | ltiblock.ss | ltiblock.tf | genss | systume
| looptune | hinfstruct

Introduced in R2011a

ltiblock.pid

Tunable PID controller

Syntax

```
blk = ltiblock.pid(name,type)
blk = ltiblock.pid(name,type,Ts)
blk = ltiblock.pid(name,sys)
```

Description

Model object for creating tunable one-degree-of-freedom PID controllers. ltiblock.pid lets you parametrize a tunable SISO PID controller for parameter studies or for automatic tuning with Robust Control Toolbox tuning commands such as systume, looptune, or hinfstruct.

ltiblock.pid is part of the family of parametric Control Design Blocks. Other
parametric Control Design Blocks include ltiblock.gain, ltiblock.ss, and
ltiblock.tf.

Construction

blk = ltiblock.pid(name,type) creates the one-degree-of-freedom continuous-time
PID controller:

$$blk = K_p + \frac{K_i}{s} + \frac{K_d s}{1 + T_f s},$$

with tunable parameters Kp, Ki, Kd, and Tf. The string type sets the controller type by fixing some of these values to zero (see "Input Arguments" on page 1-437).

blk = ltiblock.pid(name,type,Ts) creates a discrete-time PID controller with
sample time Ts:

$$blk = K_p + K_i IF(z) + \frac{K_d}{T_f + DF(z)},$$

where IF(z) and DF(z) are the discrete integrator formulas for the integral and derivative terms, respectively. The values of the IFormula and DFormula properties set the discrete integrator formulas (see "Properties" on page 1-438).

blk = ltiblock.pid(name,sys) uses the dynamic system model, sys, to set the sample time, Ts, and the initial values of the parameters Kp, Ki, Kd, and Tf.

Input Arguments

name

PID controller Name, specified as a string. (See "Properties" on page 1-438.)

type

String specifying controller type. Specifying a controller type fixes up to three of the PID controller parameters. **type** can take the following values:

String	Controller Type	Effect on PID Parameters
'P'	Proportional only	Ki and Kd are fixed to zero; Tf is fixed to 1; Kp is free
'PI'	Proportional-integral	Kd is fixed to zero; Tf is fixed to 1; Kp and Ki are free
' PD '	Proportional-derivative with first-order filter on derivative action	Ki is fixed to zero; Kp, Kd, and Tf are free
'PID'	Proportional-integral- derivative with first-order filter on derivative action	Kp, Ki, Kd, and Tf are free

Ts

Sample time, specified as a scalar.

sys

Dynamic system model representing a PID controller.

Properties

Kp, Ki, Kd, Tf

Parametrization of the PID gains Kp, Ki, Kd, and filter time constant Tf of the tunable PID controller blk.

The following fields of blk.Kp, blk.Ki, blk.Kd, and blk.Tf are used when you tune blk using a tuning command such as systume:

Field	Description
Value	Current value of the parameter.
Free	Logical value determining whether the parameter is fixed or tunable. For example,
	 If blk.Kp.Free = 1, then blk.Kp.Value is tunable.
	 If blk.Kp.Free = 0, then blk.Kp.Value is fixed.
Minimum	Minimum value of the parameter. This property places a lower bound on the tuned value of the parameter. For example, setting blk.Kp.Minimum = 0 ensures that Kp remains positive. blk.Tf.Minimum must always be positive.
Maximum	Maximum value of the parameter. This property places an upper bound on the tuned value of the parameter. For example, setting blk.Tf.Maximum = 100 ensures that the filter time constant does not exceed 100.

blk.Kp, blk.Ki, blk.Kd, and blk.Tf are param.Continuous objects. For general information about the properties of these param.Continuous objects, see the param.Continuous object reference page.

IFormula, DFormula

Strings setting the discrete integrator formulas IF(z) and DF(z) for the integral and derivative terms, respectively. IFormula and DFormula can have the following values:

String	IF(z) or DF(z) Formula
'ForwardEuler'	$\frac{T_s}{z-1}$
'BackwardEuler'	$\frac{T_s z}{z-1}$
'Trapezoidal'	$\frac{T_s}{2}\frac{z+1}{z-1}$

Default: 'ForwardEuler'

Ts

Sample time. For continuous-time models, Ts = 0. For discrete-time models, Ts is a positive scalar representing the sampling period. This value is expressed in the unit specified by the TimeUnit property of the model. To denote a discrete-time model with unspecified sample time, set Ts = -1.

Changing this property does not discretize or resample the model. Use c2d and d2c to convert between continuous- and discrete-time representations. Use d2d to change the sample time of a discrete-time system.

Default: 0 (continuous time)

TimeUnit

String representing the unit of the time variable. This property specifies the units for the time variable, the sample time Ts, and any time delays in the model. Use any of the following values:

- 'nanoseconds'
- 'microseconds'
- 'milliseconds'
- 'seconds'

- 'minutes'
- 'hours'
- 'days'
- 'weeks'
- 'months'
- 'years'

Changing this property has no effect on other properties, and therefore changes the overall system behavior. Use chgTimeUnit to convert between time units without modifying system behavior.

Default: 'seconds'

InputName

Input channel names. Set InputName to a string for single-input model. For a multiinput model, set InputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign input names for multi-input models. For example, if **sys** is a two-input model, enter:

```
sys.InputName = 'controls';
```

The input names automatically expand to { 'controls(1) '; 'controls(2) '}.

You can use the shorthand notation u to refer to the InputName property. For example, sys.u is equivalent to sys.InputName.

Input channel names have several uses, including:

- · Identifying channels on model display and plots
- · Extracting subsystems of MIMO systems
- · Specifying connection points when interconnecting models

Default: Empty string ' ' for all input channels

InputUnit

Input channel units. Use InputUnit to keep track of input signal units. For a singleinput model, set InputUnit to a string. For a multi-input model, set InputUnit to a cell array of strings. InputUnit has no effect on system behavior. **Default:** Empty string ' ' for all input channels

InputGroup

Input channel groups. The InputGroup property lets you assign the input channels of MIMO systems into groups and refer to each group by name. Specify input groups as a structure. In this structure, field names are the group names, and field values are the input channels belonging to each group. For example:

```
sys.InputGroup.controls = [1 2];
sys.InputGroup.noise = [3 5];
```

creates input groups named controls and noise that include input channels 1, 2 and 3, 5, respectively. You can then extract the subsystem from the controls inputs to all outputs using:

sys(:,'controls')

Default: Struct with no fields

OutputName

Output channel names. Set OutputName to a string for single-output model. For a multioutput model, set OutputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign output names for multi-output models. For example, if **sys** is a two-output model, enter:

```
sys.OutputName = 'measurements';
```

The output names automatically expand to { 'measurements(1) '; 'measurements(2) '}.

You can use the shorthand notation y to refer to the OutputName property. For example, sys.y is equivalent to sys.OutputName.

Output channel names have several uses, including:

- · Identifying channels on model display and plots
- · Extracting subsystems of MIMO systems
- · Specifying connection points when interconnecting models

Default: Empty string ' ' for all output channels

OutputUnit

Output channel units. Use OutputUnit to keep track of output signal units. For a single-output model, set OutputUnit to a string. For a multi-output model, set OutputUnit to a cell array of strings. OutputUnit has no effect on system behavior.

Default: Empty string ' ' for all output channels

OutputGroup

Output channel groups. The OutputGroup property lets you assign the output channels of MIMO systems into groups and refer to each group by name. Specify output groups as a structure. In this structure, field names are the group names, and field values are the output channels belonging to each group. For example:

sys.OutputGroup.temperature = [1]; sys.InputGroup.measurement = [3 5];

creates output groups named temperature and measurement that include output channels 1, and 3, 5, respectively. You can then extract the subsystem from all inputs to the measurement outputs using:

sys('measurement',:)

Default: Struct with no fields

Name

System name. Set Name to a string to label the system.

Default: ' '

Notes

Any text that you want to associate with the system. Set **Notes** to a string or a cell array of strings.

Default: {}

UserData

Any type of data you want to associate with system. Set UserData to any MATLAB data type.

Default: []

Examples

Tunable Controller with a Fixed Parameter

Create a tunable PD controller. Then, initialize the parameter values, and fix the filter time constant.

Controller Initialized by Dynamic System Model

Create a tunable discrete-time PI controller. Use a **pid** object to initialize the parameters and other properties.

Type "pid(blk)" to see the current value and "get(blk)" to see all properties.

```
and tunable parameters Kp, Ki.
```

Type "pid(blk)" to see the current value and "get(blk)" to see all properties.

blk takes the value of properties, such as Ts and IFormula, from C.

Controller with Named Input and Output

Create a tunable PID controller, and assign names to the input and output.

```
blk = ltiblock.pid('pidblock','pid')
blk.InputName = {'error'} % assign input name
blk.OutputName = {'control'} % assign output name
```

More About

Tips

- You can modify the PID structure by fixing or freeing any of the parameters Kp, Ki, Kd, and Tf. For example, blk.Tf.Free = false fixes Tf to its current value.
- To convert an ltiblock.pid parametric model to a numeric (nontunable) model object, use model commands such as pid, pidstd, tf, or ss. You can also use getValue to obtain the current value of a tunable model.
- "Control Design Blocks"
- "Models with Tunable Coefficients"

See Also

```
ltiblock.pid2 | ltiblock.ss | ltiblock.tf | systume | looptume |
hinfstruct | getValue
```

Introduced in R2011a

ltiblock.pid2

Tunable two-degree-of-freedom PID controller

Syntax

```
blk = ltiblock.pid2(name,type)
blk = ltiblock.pid2(name,type,Ts)
blk = ltiblock.pid2(name,sys)
```

Description

Model object for creating tunable two-degree-of-freedom PID controllers. ltiblock.pid2 lets you parametrize a tunable SISO two-degree-of-freedom PID controller. You can use this parametrized controller for parameter studies or for automatic tuning with Robust Control Toolbox tuning commands such as systume, looptune, or hinfstruct.

ltiblock.pid2 is part of the family of parametric Control Design Blocks. Other
parametric Control Design Blocks include ltiblock.gain, ltiblock.ss, and
ltiblock.tf.

Construction

blk = ltiblock.pid2(name,type) creates the two-degree-of-freedom continuoustime PID controller described by the equation:

$$u = K_p \left(br - y \right) + \frac{K_i}{s} \left(r - y \right) + \frac{K_d s}{1 + T_f s} \left(cr - y \right).$$

r is the setpoint command, y is the measured response to that setpoint, and u is the control signal, as shown in the following illustration.

$$r \rightarrow blk \rightarrow u$$

The tunable parameters of the block are:

- Scalar gains Kp, Ki, and Kd
- Filter time constant Tf
- Scalar weights **b** and **c**

The string type sets the controller type by fixing some of these values to zero (see "Input Arguments" on page 1-446).

blk = ltiblock.pid2(name,type,Ts) creates a discrete-time PID controller with
sample time Ts. The equation describing this controller is:

$$u = K_p \left(br - y \right) + K_i IF(z)(r - y) + \frac{K_d}{T_f + DF(z)} (cr - y).$$

IF(z) and DF(z) are the discrete integrator formulas for the integral and derivative terms, respectively. The values of the IFormula and DFormula properties set the discrete integrator formulas (see "Properties" on page 1-447).

blk = ltiblock.pid2(name,sys) uses the dynamic system model, sys, to set the sample time, Ts, and the initial values of all the tunable parameters. The model sys must be compatible with the equation of a two-degree-of-freedom PID controller.

Input Arguments

name

PID controller Name, specified as a string. (See "Properties" on page 1-447.)

type

Controller type, specified as a string. Specifying a controller type fixes up to three of the PID controller parameters. **type** can take the following values:

String	Controller Type	Effect on PID Parameters
'P'	1 0	Ki and Kd are fixed to zero; Tf is fixed to 1; Kp is free
'PI'		Kd is fixed to zero; Tf is fixed to 1; Kp and Ki are free

String	Controller Type	Effect on PID Parameters
' PD '	Proportional-derivative with first-order filter on derivative action	Ki is fixed to zero; Kp, Kd, and Tf are free
'PID'	Proportional-integral- derivative with first-order filter on derivative action	Kp, Ki, Kd, and Tf are free

Ts

Sample time, specified as a scalar.

sys

Dynamic system model representing a two-degree-of-freedom PID controller.

Properties

Kp,Ki,Kd,Tf,b,c

Parametrization of the PID gains $Kp,\,Ki,\,Kd,$ the filter time constant, Tf, and the scalar gains, b and c.

The following fields of blk.Kp, blk.Ki, blk.Kd, blk.Tf, blk.b, and blk.c are used when you tune blk using a tuning command such as systume:

Field	Description
Value	Current value of the parameter. blk.b.Value, and blk.c.Value are always nonnegative.
Free	 Logical value determining whether the parameter is fixed or tunable. For example, If blk.Kp.Free = 1, then blk.Kp.Value is tunable.
	 If blk.Kp.Free = 0, then blk.Kp.Value is fixed.

Field	Description
Minimum	Minimum value of the parameter. This property places a lower bound on the tuned value of the parameter. For example, setting blk.Kp.Minimum = 0 ensures that Kp remains positive. blk.Tf.Minimum must always be positive.
Maximum	Maximum value of the parameter. This property places an upper bound on the tuned value of the parameter. For example, setting blk.c.Maximum = 1 ensures that C does not exceed unity.

blk.Kp, blk.Ki, blk.Kd, blk.Tf, blk.b, and blk.c are param.Continuous objects. For more information about the properties of these param.Continuous objects, see the param.Continuous object reference page.

IFormula, DFormula

Strings setting the discrete integrator formulas IF(z) and DF(z) for the integral and derivative terms, respectively. IFormula and DFormula can have the following values:

String	IF(z) or DF(z) Formula
'ForwardEuler'	$\frac{T_s}{z-1}$
'BackwardEuler'	$\frac{T_s z}{z-1}$
'Trapezoidal'	$\frac{T_s}{2}\frac{z+1}{z-1}$

Default: 'ForwardEuler'

Ts

Sample time. For continuous-time models, Ts = 0. For discrete-time models, Ts is a positive scalar representing the sampling period. This value is expressed in the unit

specified by the TimeUnit property of the model. To denote a discrete-time model with unspecified sample time, set Ts = -1.

Changing this property does not discretize or resample the model. Use c2d and d2c to convert between continuous- and discrete-time representations. Use d2d to change the sample time of a discrete-time system.

Default: 0 (continuous time)

TimeUnit

String representing the unit of the time variable. This property specifies the units for the time variable, the sample time Ts, and any time delays in the model. Use any of the following values:

- 'nanoseconds'
- 'microseconds'
- 'milliseconds'
- 'seconds'
- 'minutes'
- 'hours'
- 'days'
- 'weeks'
- 'months'
- 'years'

Changing this property has no effect on other properties, and therefore changes the overall system behavior. Use chgTimeUnit to convert between time units without modifying system behavior.

Default: 'seconds'

InputName

Input channel names. Set InputName to a string for single-input model. For a multiinput model, set InputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign input names for multi-input models. For example, if **sys** is a two-input model, enter:

```
sys.InputName = 'controls';
```

The input names automatically expand to { 'controls(1) '; 'controls(2) '}.

You can use the shorthand notation u to refer to the InputName property. For example, sys.u is equivalent to sys.InputName.

Input channel names have several uses, including:

- · Identifying channels on model display and plots
- Extracting subsystems of MIMO systems
- · Specifying connection points when interconnecting models

Default: Empty string ' ' for all input channels

InputUnit

Input channel units. Use InputUnit to keep track of input signal units. For a singleinput model, set InputUnit to a string. For a multi-input model, set InputUnit to a cell array of strings. InputUnit has no effect on system behavior.

Default: Empty string ' ' for all input channels

InputGroup

Input channel groups. The InputGroup property lets you assign the input channels of MIMO systems into groups and refer to each group by name. Specify input groups as a structure. In this structure, field names are the group names, and field values are the input channels belonging to each group. For example:

```
sys.InputGroup.controls = [1 2];
sys.InputGroup.noise = [3 5];
```

creates input groups named controls and noise that include input channels 1, 2 and 3, 5, respectively. You can then extract the subsystem from the controls inputs to all outputs using:

```
sys(:,'controls')
```

Default: Struct with no fields

OutputName

Output channel names. Set OutputName to a string for single-output model. For a multioutput model, set OutputName to a cell array of strings. Alternatively, use automatic vector expansion to assign output names for multi-output models. For example, if **sys** is a two-output model, enter:

```
sys.OutputName = 'measurements';
```

```
The output names automatically expand to { 'measurements(1) '; 'measurements(2) ' }.
```

You can use the shorthand notation y to refer to the OutputName property. For example, sys.y is equivalent to sys.OutputName.

Output channel names have several uses, including:

- · Identifying channels on model display and plots
- · Extracting subsystems of MIMO systems
- · Specifying connection points when interconnecting models

Default: Empty string ' ' for all output channels

OutputUnit

Output channel units. Use OutputUnit to keep track of output signal units. For a single-output model, set OutputUnit to a string. For a multi-output model, set OutputUnit to a cell array of strings. OutputUnit has no effect on system behavior.

Default: Empty string ' ' for all output channels

OutputGroup

Output channel groups. The OutputGroup property lets you assign the output channels of MIMO systems into groups and refer to each group by name. Specify output groups as a structure. In this structure, field names are the group names, and field values are the output channels belonging to each group. For example:

```
sys.OutputGroup.temperature = [1];
sys.InputGroup.measurement = [3 5];
```

creates output groups named temperature and measurement that include output channels 1, and 3, 5, respectively. You can then extract the subsystem from all inputs to the measurement outputs using:

```
sys('measurement',:)
```

Default: Struct with no fields

Name

System name. Set Name to a string to label the system.

Default: ' '

Notes

Any text that you want to associate with the system. Set **Notes** to a string or a cell array of strings.

Default: {}

UserData

Any type of data you want to associate with system. Set UserData to any MATLAB data type.

Default: []

Examples

Tunable Two-Degree-of-Freedom Controller with a Fixed Parameter

Create a tunable two-degree-of-freedom PD controller. Then, initialize the parameter values, and fix the filter time constant.

Tf*s+1

where r,y are the controller inputs and Kp, Kd, b, c are tunable gains.

Type "showBlockValue(blk)" to see the current value and "get(blk)" to see all properties.

Controller Initialized by Dynamic System Model

Create a tunable two-degree-of-freedom PI controller. Use a two-input, one-output tf model to initialize the parameters and other properties.

```
s = tf('s');
Kp = 10;
Ki = 0.1;
b = 0.7;
sys = [(b*Kp + Ki/s), (-Kp - Ki/s)];
blk = ltiblock.pid2('PI2dof',sys)
blk =
Parametric continuous-time 2-DOF PID controller "PI2dof" with equation:
u = Kp (b*r-y) + Ki 1 --- (r-y)
s
where r,y are the controller inputs and Kp, Ki, b are tunable gains.
Type "showBlockValue(blk)" to see the current value and "get(blk)" to see all
```

blk takes initial parameter values from sys.

properties.

If sys is a discrete-time system, blk takes the value of properties, such as Ts and IFormula, from sys.

Controller with Named Inputs and Output

Create a tunable PID controller, and assign names to the inputs and output.

```
blk = ltiblock.pid2('pidblock','pid');
blk.InputName = {'reference','measurement'};
blk.OutputName = {'control'};
```

blk.InputName is a cell array containing two strings, because a two-degree-of-freedom PID controller has two inputs.

More About

Tips

- You can modify the PID structure by fixing or freeing any of the parameters. For example, blk.Tf.Free = false fixes Tf to its current value.
- To convert a ltiblock.pid2 parametric model to a numeric (nontunable) model object, use model commands such as tf or ss. You can also use getValue to obtain the current value of a tunable model.
- "Control Design Blocks"
- "Models with Tunable Coefficients"

See Also

```
ltiblock.pid | ltiblock.ss | ltiblock.tf | systume | looptume | hinfstruct
| getValue
```

Introduced in R2012b

ltiblock.ss

Tunable fixed-order state-space model

Syntax

```
blk = ltiblock.ss(name,Nx,Ny,Nu)
blk = ltiblock.ss(name,Nx,Ny,Nu,Ts)
blk = ltiblock.ss(name,sys)
blk = ltiblock.ss(...,Astruct)
```

Description

Model object for creating tunable fixed-order state-space models. ltiblock.ss lets you parametrize a state-space model of a given order for parameter studies or for automatic tuning with Robust Control Toolbox tuning commands such as systume or looptune.

ltiblock.ss is part of the Control Design Block family of parametric models. Other Control Design Blocks includeltiblock.pid, ltiblock.gain, and ltiblock.tf.

Construction

blk = ltiblock.ss(name, Nx, Ny, Nu) creates the continuous-time parametric statespace model named name. The state-space model blk has Nx states, Ny outputs, and Nu inputs. The tunable parameters are the entries in the *A*, *B*, *C*, and *D* matrices of the state-space model.

blk = ltiblock.ss(name,Nx,Ny,Nu,Ts) creates a discrete-time parametric statespace model with sample time Ts.

blk = ltiblock.ss(name,sys) uses the dynamic system sys to dimension the
parametric state-space model, set its sample time, and initialize the tunable parameters.

blk = ltiblock.ss(...,Astruct) creates a parametric state-space model whose A
matrix is restricted to the structure specified in Astruct.

Input Arguments

name

String specifying the Name of the parametric state-space model blk. (See "Properties" on page 1-457.)

Nx

Nonnegative integer specifying the number of states (order) of the parametric state-space model blk.

Ny

Nonnegative integer specifying the number of outputs of the parametric state-space model blk.

Nu

Nonnegative integer specifying the number of inputs of the parametric state-space model blk.

Ts

Scalar sample time.

Astruct

String specifying constraints on the form of the A matrix of the parametric state-space model blk. Astruct can take the following values:

String	Structure of A matrix
'tridiag'	A is tridiagonal. In tridiagonal form, A has free elements only in the main diagonal, the first diagonal below the main diagonal, and the first diagonal above the main diagonal. The remaining elements of A are fixed to zero.
'full'	A is full (every entry in A is a free parameter).
'companion'	A is in companion form. In companion form, the characteristic polynomial of the

String	Structure of A matrix
	system appears explicitly in the rightmost column of the A matrix. See canon for more information.

If you do not specify Astruct, blk defaults to 'tridiag' form.

sys

Dynamic system model providing number of states, number of inputs and outputs, sample time, and initial values of the parameters of blk. To obtain the dimensions and initial parameter values, ltiblock.ss converts sys to a state-space model with the structure specified in Astruct. If you omit Astruct, ltiblock.ss converts sys into tridiagonal state-space form.

Properties

a, b, c, d

Parametrization of the state-space matrices A, B, C, and D of the tunable state-space model blk.

blk.a, blk.b, blk.c, and blk.d are param.Continuous objects. For general information about the properties of these param.Continuous objects, see the param.Continuous object reference page.

The following fields of blk.a, blk.b, blk.c, and blk.d are used when you tune blk using hinfstruct:

Field	Description
Value	Current values of the entries in the parametrized state-space matrix. For example, blk.a.Value contains the values of the A matrix of blk. hinfstruct tunes all entries in blk.a.Value, blk.b.Value, blk.c.Value, and blk.d.Value except those whose values are fixed by blk.Gain.Free.

Field	Description
Free	2-D array of logical values determining whether the corresponding state-space matrix parameters are fixed or free parameters. For example:
	 If blk.a.Free(i,j) = 1, then blk.a.Value(i,j) is a tunable parameter. If blk.a.Free(i,j) = 0, then
	blk.a.Value(i,j) is fixed.
	Defaults: By default, all entries in b, c, and c are tunable. The default free entries in a depend upon the value of Astruct:
	 'tridiag' — entries on the three diagonals of blk.a.Free are 1; the rest are 0.
	 'full' — all entries in blk.a.Free are 0.
	 'companion' — blk.a.Free(1,:) = 1 and blk.a.Free(j,j-1) = 1; all other entries are 0.
Minimum	Minimum value of the parameter. This property places a lower bound on the tuned value of the parameter. For example, setting blk.a.Minimum(1,1) = 0 ensures that the first entry in the A matrix remains positive. Default: -Inf.
Maximum	Maximum value of the parameter. This property places an upper bound on the tuned value of the parameter. For example, setting blk.a.Maximum(1,1) = 0 ensures that the first entry in the A matrix remains negative. Default: Inf.

StateName

State names. For first-order models, set <code>StateName</code> to a string. For models with two or more states, set <code>StateName</code> to a cell array of strings . Use an empty string ' ' for unnamed states.

Default: Empty string ' ' for all states

StateUnit

State units. Use StateUnit to keep track of the units each state is expressed in. For first-order models, set StateUnit to a string. For models with two or more states, set StateUnit to a cell array of strings. StateUnit has no effect on system behavior.

Default: Empty string ' ' for all states

Ts

Sample time. For continuous-time models, Ts = 0. For discrete-time models, Ts is a positive scalar representing the sampling period. This value is expressed in the unit specified by the TimeUnit property of the model. To denote a discrete-time model with unspecified sample time, set Ts = -1.

Changing this property does not discretize or resample the model. Use c2d and d2c to convert between continuous- and discrete-time representations. Use d2d to change the sample time of a discrete-time system.

Default: 0 (continuous time)

TimeUnit

String representing the unit of the time variable. This property specifies the units for the time variable, the sample time Ts, and any time delays in the model. Use any of the following values:

- 'nanoseconds'
- 'microseconds'
- 'milliseconds'
- 'seconds'
- 'minutes'

- 'hours'
- 'days'
- 'weeks'
- 'months'
- 'years'

Changing this property has no effect on other properties, and therefore changes the overall system behavior. Use chgTimeUnit to convert between time units without modifying system behavior.

Default: 'seconds'

InputName

Input channel names. Set InputName to a string for single-input model. For a multiinput model, set InputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign input names for multi-input models. For example, if **sys** is a two-input model, enter:

```
sys.InputName = 'controls';
```

```
The input names automatically expand to { 'controls(1) '; 'controls(2) '}.
```

You can use the shorthand notation u to refer to the InputName property. For example, sys.u is equivalent to sys.InputName.

Input channel names have several uses, including:

- · Identifying channels on model display and plots
- · Extracting subsystems of MIMO systems
- · Specifying connection points when interconnecting models

Default: Empty string ' ' for all input channels

InputUnit

Input channel units. Use InputUnit to keep track of input signal units. For a singleinput model, set InputUnit to a string. For a multi-input model, set InputUnit to a cell array of strings. InputUnit has no effect on system behavior. Default: Empty string ' ' for all input channels

InputGroup

Input channel groups. The InputGroup property lets you assign the input channels of MIMO systems into groups and refer to each group by name. Specify input groups as a structure. In this structure, field names are the group names, and field values are the input channels belonging to each group. For example:

```
sys.InputGroup.controls = [1 2];
sys.InputGroup.noise = [3 5];
```

creates input groups named controls and noise that include input channels 1, 2 and 3, 5, respectively. You can then extract the subsystem from the controls inputs to all outputs using:

sys(:,'controls')

Default: Struct with no fields

OutputName

Output channel names. Set OutputName to a string for single-output model. For a multioutput model, set OutputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign output names for multi-output models. For example, if **sys** is a two-output model, enter:

```
sys.OutputName = 'measurements';
```

The output names automatically expand to { 'measurements(1) '; 'measurements(2) ' }.

You can use the shorthand notation y to refer to the OutputName property. For example, sys.y is equivalent to sys.OutputName.

Output channel names have several uses, including:

- · Identifying channels on model display and plots
- · Extracting subsystems of MIMO systems
- · Specifying connection points when interconnecting models

Default: Empty string ' ' for all output channels

OutputUnit

Output channel units. Use OutputUnit to keep track of output signal units. For a single-output model, set OutputUnit to a string. For a multi-output model, set OutputUnit to a cell array of strings. OutputUnit has no effect on system behavior.

Default: Empty string ' ' for all output channels

OutputGroup

Output channel groups. The OutputGroup property lets you assign the output channels of MIMO systems into groups and refer to each group by name. Specify output groups as a structure. In this structure, field names are the group names, and field values are the output channels belonging to each group. For example:

sys.OutputGroup.temperature = [1]; sys.InputGroup.measurement = [3 5];

creates output groups named temperature and measurement that include output channels 1, and 3, 5, respectively. You can then extract the subsystem from all inputs to the measurement outputs using:

```
sys('measurement',:)
```

Default: Struct with no fields

Name

System name. Set Name to a string to label the system.

Default: ' '

Notes

Any text that you want to associate with the system. Set **Notes** to a string or a cell array of strings.

Default: {}

UserData

Any type of data you want to associate with system. Set UserData to any MATLAB data type.

Default: []

Examples

Create a parametrized 5th-order SISO model with zero ${\tt D}$ matrix.

blk = ltiblock.ss('ssblock',5,1,1); blk.d.Value = 0; % set D = 0 blk.d.Free = false; % fix D to zero

By default, the A matrix is in tridiagonal form. To parametrize the model in companion form, use the 'companion' input argument:

```
blk = ltiblock.ss('ssblock',5,1,1,'companion');
blk.d.Value = 0; % set D = 0
blk.d.Free = false; % fix D to zero
```

Create a parametric state-space model, and assign names to the inputs.

```
blk = ltiblock.ss('ssblock',5,2,2) % 5 states, 2 outputs, 2 inputs
blk.InputName = {'Xerror','Yerror'} % assign input names
```

More About

Tips

• Use the Astruct input argument to constrain the structure of the A matrix of the parametric state-space model. To impose additional structure constrains on the state-space matrices, use the fields blk.a.Free, blk.b.Free, blk.c.Free, and blk.d.Free to fix the values of specific entries in the parameter matrices.

For example, to fix the value of blk.b(i,j), set blk.b.Free(i,j) = 0. To allow hinfstruct to tune blk.b(i,j), set blk.b.Free(i,j) = 1.

- To convert an ltiblock.ss parametric model to a numeric (non-tunable) model object, use model commands such as ss, tf, or zpk.
- "Control Design Blocks"
- "Models with Tunable Coefficients"

See Also

```
ltiblock.pid | ltiblock.pid2 | ltiblock.ss | ltiblock.tf | genss | systume | looptune | hinfstruct
```

Introduced in R2011a

ltiblock.tf

Tunable transfer function with fixed number of poles and zeros

Syntax

```
blk = ltiblock.tf(name,Nz,Np)
blk = ltiblock.tf(name,Nz,Np,Ts)
blk = ltiblock.tf(name,sys)
```

Description

Model object for creating tunable SISO transfer function models of fixed order. ltiblock.tf lets you parametrize a transfer function of a given orderfor parameter studies or for automatic tuning with Robust Control Toolbox tuning commands such as systume or looptune.

ltiblock.tf is part of the Control Design Block family of parametric models. Other Control Design Blocks includeltiblock.pid, ltiblock.ss, and ltiblock.gain.

Construction

blk = ltiblock.tf(name,Nz,Np) creates the parametric SISO transfer function:

$$blk = \frac{a_m s^m + a_{m-1} s^{m-1} + \ldots + a_1 s + a_0}{s^n + b_{n-1} s^{n-1} + \ldots + b_1 s + b_0}$$

n = Np is the maximum number of poles of blk, and m = Nz is the maximum number of zeros. The tunable parameters are the numerator and denominator coefficients $a_0, ..., a_m$ and $b_0, ..., b_{n-1}$. The leading coefficient of the denominator is fixed to 1.

blk = ltiblock.tf(name,Nz,Np,Ts) creates a discrete-time parametric transfer function with sample time Ts. blk = ltiblock.tf(name,sys) uses the tf model sys to set the number of poles, number of zeros, sample time, and initial parameter values.

Input Arguments

name

String specifying the Name of the parametric transfer function blk. (See "Properties" on page 1-466.)

Nz

Nonnegative integer specifying the number of zeros of the parametric transfer function blk.

Np

Nonnegative integer specifying the number of poles of the parametric transfer function blk.

Ts

Scalar sample time.

sys

tf model providing number of poles, number of zeros, sample time, and initial values of the parameters of blk.

Properties

num, den

Parametrization of the numerator coefficients a_m , ..., a_0 and the denominator coefficients $1, b_{n-1}, ..., b_0$ of the tunable transfer function blk.

blk.num and blk.den are param.Continuous objects. For general information about the properties of these param.Continuous objects, see the param.Continuous object reference page.

Field	Description
Value	Array of current values of the numerator a_m ,, a_0 or the denominator coefficients $1, b_{n-1},, b_0$. blk.num.Value has length Nz + 1. blk.den.Value has length Np + 1. The leading coefficient of the denominator (blk.den.Value(1)) is always fixed to 1. By default, the coefficients initialize to values that yield a stable, strictly proper transfer function. Use the input sys to initialize the coefficients to different values. hinfstruct tunes all values except those whose Free field is zero.
Free	 Array of logical values determining whether the coefficients are fixed or tunable. For example, If blk.num.Free(j) = 1, then blk.num.Value(j) is tunable. If blk.num.Free(j) = 0, then blk.num.Value(j) is fixed. Default: blk.den.Free(1) = 0; all other entries are 1.
Minimum	Minimum value of the parameter. This property places a lower bound on the tuned value of the parameter. For example, setting blk.num.Minimum(1) = 0 ensures that the leading coefficient of the numerator remains positive. Default: - Inf.
Maximum	Maximum value of the parameter. This property places an upper bound on the

The following fields of blk.num and blk.den are used when you tune blk using hinfstruct:

Field	Description
	<pre>tuned value of the parameter. For example, setting blk.num.Maximum(1) = 1 ensures that the leading coefficient of the numerator does not exceed 1. Default: Inf.</pre>

Ts

Sample time. For continuous-time models, Ts = 0. For discrete-time models, Ts is a positive scalar representing the sampling period. This value is expressed in the unit specified by the TimeUnit property of the model. To denote a discrete-time model with unspecified sample time, set Ts = -1.

Changing this property does not discretize or resample the model. Use c2d and d2c to convert between continuous- and discrete-time representations. Use d2d to change the sample time of a discrete-time system.

Default: 0 (continuous time)

TimeUnit

String representing the unit of the time variable. This property specifies the units for the time variable, the sample time Ts, and any time delays in the model. Use any of the following values:

- 'nanoseconds'
- 'microseconds'
- 'milliseconds'
- 'seconds'
- 'minutes'
- 'hours'
- 'days'
- 'weeks'
- 'months'
- 'years'

Changing this property has no effect on other properties, and therefore changes the overall system behavior. Use chgTimeUnit to convert between time units without modifying system behavior.

Default: 'seconds'

InputName

Input channel names. Set InputName to a string for single-input model. For a multiinput model, set InputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign input names for multi-input models. For example, if **sys** is a two-input model, enter:

```
sys.InputName = 'controls';
```

The input names automatically expand to { 'controls(1) '; 'controls(2) '}.

You can use the shorthand notation u to refer to the InputName property. For example, sys.u is equivalent to sys.InputName.

Input channel names have several uses, including:

- · Identifying channels on model display and plots
- · Extracting subsystems of MIMO systems
- · Specifying connection points when interconnecting models

Default: Empty string ' ' for all input channels

InputUnit

Input channel units. Use InputUnit to keep track of input signal units. For a singleinput model, set InputUnit to a string. For a multi-input model, set InputUnit to a cell array of strings. InputUnit has no effect on system behavior.

Default: Empty string ' ' for all input channels

InputGroup

Input channel groups. The InputGroup property lets you assign the input channels of MIMO systems into groups and refer to each group by name. Specify input groups as a structure. In this structure, field names are the group names, and field values are the input channels belonging to each group. For example:

```
sys.InputGroup.controls = [1 2];
sys.InputGroup.noise = [3 5];
```

creates input groups named controls and noise that include input channels 1, 2 and 3, 5, respectively. You can then extract the subsystem from the controls inputs to all outputs using:

sys(:,'controls')

Default: Struct with no fields

OutputName

Output channel names. Set OutputName to a string for single-output model. For a multioutput model, set OutputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign output names for multi-output models. For example, if **sys** is a two-output model, enter:

```
sys.OutputName = 'measurements';
```

```
The output names automatically expand to { 'measurements(1) '; 'measurements(2) '}.
```

You can use the shorthand notation y to refer to the OutputName property. For example, sys.y is equivalent to sys.OutputName.

Output channel names have several uses, including:

- · Identifying channels on model display and plots
- · Extracting subsystems of MIMO systems
- · Specifying connection points when interconnecting models

Default: Empty string '' for all output channels

OutputUnit

Output channel units. Use OutputUnit to keep track of output signal units. For a single-output model, set OutputUnit to a string. For a multi-output model, set OutputUnit to a cell array of strings. OutputUnit has no effect on system behavior.

Default: Empty string ' ' for all output channels

OutputGroup

Output channel groups. The OutputGroup property lets you assign the output channels of MIMO systems into groups and refer to each group by name. Specify output groups as a structure. In this structure, field names are the group names, and field values are the output channels belonging to each group. For example:

```
sys.OutputGroup.temperature = [1];
sys.InputGroup.measurement = [3 5];
```

creates output groups named temperature and measurement that include output channels 1, and 3, 5, respectively. You can then extract the subsystem from all inputs to the measurement outputs using:

```
sys('measurement',:)
```

Default: Struct with no fields

Name

System name. Set Name to a string to label the system.

Default: ' '

Notes

Any text that you want to associate with the system. Set **Notes** to a string or a cell array of strings.

Default: {}

UserData

Any type of data you want to associate with system. Set UserData to any MATLAB data type.

Default: []

Examples

Create a parametric SISO transfer function with two zeros, four poles, and at least one integrator.

A transfer function with an integrator includes a factor of 1/s. Therefore, to ensure that a parametrized transfer function has at least one integrator regardless of the parameter values, fix the lowest-order coefficient of the denominator to zero.

```
blk = ltiblock.tf('tfblock',2,4); % two zeros, four poles
blk.den.Value(end) = 0; % set last denominator entry to zero
blk.den.Free(end) = 0; % fix it to zero
```

Create a parametric transfer function, and assign names to the input and output.

```
blk = ltiblock.tf('tfblock',2,3);
blk.InputName = {'error'}; % assign input name
blk.OutputName = {'control'}; % assign output name
```

More About

Tips

- To convert an ltiblock.tf parametric model to a numeric (non-tunable) model object, use model commands such as tf, zpk, or ss.
- "Control Design Blocks"
- "Models with Tunable Coefficients"

See Also

ltiblock.pid | ltiblock.pid2 | ltiblock.ss | ltiblock.tf | genss | systume
| looptume | hinfstruct

Introduced in R2011a

lyap

Continuous Lyapunov equation solution

Syntax

lyap
X = lyap(A,Q)
X = lyap(A,B,C)
X = lyap(A,Q,[],E)

Description

lyap solves the special and general forms of the Lyapunov equation. Lyapunov equations arise in several areas of control, including stability theory and the study of the RMS behavior of systems.

X = lyap(A,Q) solves the Lyapunov equation

$$AX + XA^T + Q = 0$$

where A and Q represent square matrices of identical sizes. If Q is a symmetric matrix, the solution X is also a symmetric matrix.

X = lyap(A,B,C) solves the Sylvester equation

AX + XB + C = 0

The matrices A, B, and C must have compatible dimensions but need not be square.

X = lyap(A,Q,[],E) solves the generalized Lyapunov equation

$$AXE^T + EXA^T + Q = 0$$

where Q is a symmetric matrix. You must use empty square brackets [] for this function. If you place any values inside the brackets, the function errors out.

Limitations

The continuous Lyapunov equation has a unique solution if the eigenvalues $\alpha_1, \alpha_2, ..., \alpha_n$ of A and $\beta_1, \beta_2, ..., \beta_n$ of B satisfy

 $\alpha_i + \beta_j \neq 0$ for all pairs(i, j)

If this condition is violated, lyap produces the error message:

Solution does not exist or is not unique.

Examples

Example 1

Solve Lyapunov Equation

Solve the Lyapunov equation

$$AX + XA^T + Q = 0$$

where

$$A = \begin{bmatrix} 1 & 2 \\ -3 & -4 \end{bmatrix} \qquad Q = \begin{bmatrix} 3 & 1 \\ 1 & 1 \end{bmatrix}$$

The A matrix is stable, and the Q matrix is positive definite.

A = [1 2; -3 -4]; Q = [3 1; 1 1]; X = lyap(A,Q) These commands return the following X matrix:

Х =

6.1667	-3.8333
-3.8333	3.0000

You can compute the eigenvalues to see that X is positive definite.

eig(X)

The command returns the following result:

ans =

0.4359 8.7308

Example 2

Solve Sylvester Equation

Solve the Sylvester equation

$$AX + XB + C = 0$$

where

$$A = 5 \qquad B = \begin{bmatrix} 4 & 3 \\ 4 & 3 \end{bmatrix} \qquad C = \begin{bmatrix} 2 & 1 \end{bmatrix}$$

A = 5; B = [4 3; 4 3]; C = [2 1]; X = lyap(A,B,C)

These commands return the following X matrix:

X =

-0.2000 -0.0500

More About

Algorithms

 $1yap\ uses\ SLICOT\ routines\ SB03MD\ and\ SG03AD\ for\ Lyapunov\ equations\ and\ SB04MD\ (SLICOT)\ and\ ZTRSYL\ (LAPACK)\ for\ Sylvester\ equations.$

References

- [1] Bartels, R.H. and G.W. Stewart, "Solution of the Matrix Equation AX + XB = C," Comm. of the ACM, Vol. 15, No. 9, 1972.
- [2] Barraud, A.Y., "A numerical algorithm to solve A XA X = Q," *IEEE Trans. Auto. Contr.*, AC-22, pp. 883–885, 1977.
- [3] Hammarling, S.J., "Numerical solution of the stable, non-negative definite Lyapunov equation," *IMA J. Num. Anal.*, Vol. 2, pp. 303–325, 1982.
- [4] Penzl, T., "Numerical solution of generalized Lyapunov equations," Advances in Comp. Math., Vol. 8, pp. 33–48, 1998.
- [5] Golub, G.H., Nash, S. and Van Loan, C.F., "A Hessenberg-Schur method for the problem AX + XB = C," *IEEE Trans. Auto. Contr.*, AC-24, pp. 909–913, 1979.

See Also

covar | dlyap

Introduced before R2006a

lyapchol

Square-root solver for continuous-time Lyapunov equation

Syntax

R = lyapchol(A,B) X = lyapchol(A,B,E)

Description

R = lyapchol(A,B) computes a Cholesky factorization X = R'*R of the solution X to the Lyapunov matrix equation:

A*X + X*A' + B*B' = 0

All eigenvalues of matrix A must lie in the open left half-plane for R to exist.

X = lyapchol(A,B,E) computes a Cholesky factorization X = R'*R of X solving the generalized Lyapunov equation:

A*X*E' + E*X*A' + B*B' = 0

All generalized eigenvalues of (A,E) must lie in the open left half-plane for R to exist.

More About

Algorithms

lyapchol uses SLICOT routines SB03OD and SG03BD.

References

[1] Bartels, R.H. and G.W. Stewart, "Solution of the Matrix Equation AX + XB = C," Comm. of the ACM, Vol. 15, No. 9, 1972.

- [2] Hammarling, S.J., "Numerical solution of the stable, non-negative definite Lyapunov equation," *IMA J. Num. Anal.*, Vol. 2, pp. 303-325, 1982.
- [3] Penzl, T., "Numerical solution of generalized Lyapunov equations," Advances in Comp. Math., Vol. 8, pp. 33-48, 1998.

See Also

lyap | dlyapchol

Introduced before R2006a

mag2db

Convert magnitude to decibels (dB)

Syntax

ydb = mag2db(y)

Description

ydb = mag2db(y) returns the corresponding decibel (dB) value ydb for a given magnitude y. The relationship between magnitude and decibels is $ydb = 20 \log_{10}(y)$.

See Also

db2mag

Introduced in R2008a

make1DOF

Convert 2-DOF PID controller to 1-DOF controller

Syntax

C1 = make1DOF(C2)

Description

C1 = make1DOF(C2) converts the two-degree-of-freedom PID controller C2 to one degree of freedom by removing the terms that depend on coefficients *b* and *c*.

Examples

Convert 2-DOF PID controller to 1-DOF

Design a 2-DOF PID controller for a plant.

```
 \begin{array}{l} G = tf(1, [1 \ 0.5 \ 0.1]);\\ C2 = pidtune(G, 'pidf2', 1.5) \\ \\ C2 = \\ u = Kp \ (b^*r - y) \ + \ Ki \ - - - \ (r - y) \ + \ Kd \ - - - - - - \ (c^*r - y) \\ s \ Tf^*s + 1 \\ \\ with \ Kp = 1.12, \ Ki \ = \ 0.23, \ Kd \ = \ 1.3, \ Tf \ = \ 0.122, \ b \ = \ 0.664, \ c \ = \ 0.0136 \\ \\ Continuous-time \ 2-DOF \ PIDF \ controller \ in \ parallel \ form. \end{array}
```

Convert the controller to one degree of freedom.

C1 = make1DOF(C2)

```
C1 =

Kp + Ki * \frac{1}{\cdots} + Kd * \frac{s}{\cdots}

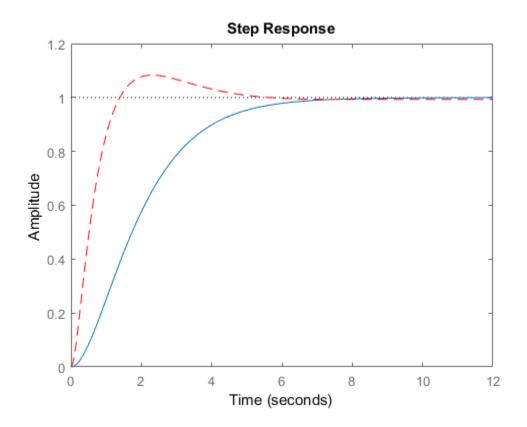
Tf*s+1

with Kp = 1.12, Ki = 0.23, Kd = 1.3, Tf = 0.122

Continuous-time PIDF controller in parallel form.
```

The new controller has the same PID gains and filter constant. However, make1DOF removes the terms involving the setpoint weights b and c. Therefore, in a closed loop with the plant G, the 2-DOF controller C2 yields a different closed-loop response from C1.

```
CM = tf(C2);
T2 = CM(1)*feedback(G,-CM(2));
T1 = feedback(G*C1,1);
stepplot(T2,T1,'r--')
```



Input Arguments

C2 — 2-DOF PID controller pid2 object | pidstd2 object

2-DOF PID controller, specified as a pid2 object or a pidstd2 object.

Output Arguments

C1 — 1-DOF PID controller pid object | pidstd object 1-DOF PID controller, returned as a pid or pidstd object. C1 is in parallel form if C2 is in parallel form, and standard form if C2 is in standard form.

For example, suppose C2 is a continuous-time, parallel-form 2-DOF pid2 controller. The relationship between the inputs, r and y, and the output u of C2 is given by:

$$u = K_p \left(br - y \right) + \frac{K_i}{s} \left(r - y \right) + \frac{K_d s}{T_f s + 1} \left(cr - y \right).$$

Then C1 is a parallel-form 1-DOF pid controller of the form:

$$C_1 = K_p + \frac{K_i}{s} + \frac{K_d s}{T_f s + 1}.$$

The PID gains K_p , K_i , and K_d , and the filter time constant T_f are unchanged. make1DOF removes the terms that depend on the setpoint weights b and c. For more information about 2-DOF PID controllers, see "Two-Degree-of-Freedom PID Controllers".

The conversion also preserves the values of the properties TS, TimeUnit, Sampling Grid, IFormula, and DFormula.

More About

"Two-Degree-of-Freedom PID Controllers"

See Also

getComponents | make2DOF | pid | pid2 | pidstd | pidstd2

Introduced in R2015b

make2DOF

Convert 1-DOF PID controller to 2-DOF controller

Syntax

```
C2 = make2DOF(C1)
C2 = make2DOF(C1,b)
C2 = make2DOF(C1,b,c)
```

Description

C2 = make2DOF(C1) converts the one-degree-of-freedom PID controller C1 to two degrees of freedom. The setpoint weights *b* and *c* of the 2-DOF controller are 1, and the remaining PID coefficients do not change.

C2 = make2DOF(C1,b) specifies the setpoint weight for the proportional term.

C2 = make2DOF(C1,b,c) specifies the setpoint weights for both the proportional and derivative terms.

Examples

Convert 1-DOF PID controller to 2-DOF

Design a 1-DOF PID controller for a plant.

with Kp = 1.12, Ki = 0.23, Kd = 1.3, Tf = 0.122

Continuous-time PIDF controller in parallel form.

Convert the controller to two degrees of freedom.

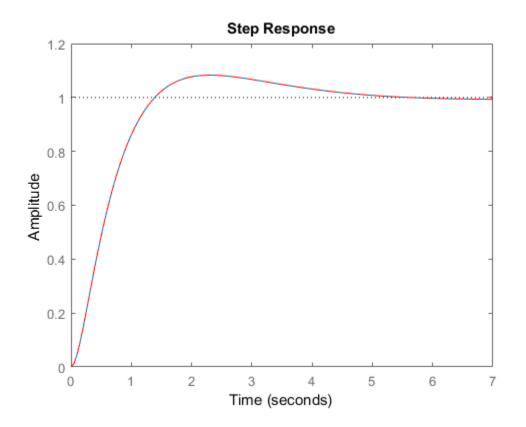
```
C2 = make2DOF(C1)

C2 =

u = Kp (b*r-y) + Ki - (r-y) + Kd - (c*r-y) + Kd - (c*r-y) + Kd - (c*r-y) + Kd + (c*r-y) + (c*r-y) + Kd + (c*r-y) + (c*r-y) + Kd + (c*r-y) + (c*r
```

The new controller has the same PID gains and filter constant. It also contains new terms involving the setpoint weights b and c. By default, b = c = 1. Therefore, in a closed loop with the plant G, the 2-DOF controller C2 yields the same response as C1.

T1 = feedback(G*C1,1); CM = tf(C2); T2 = CM(1)*feedback(G,-CM(2)); stepplot(T1,T2,'r--')

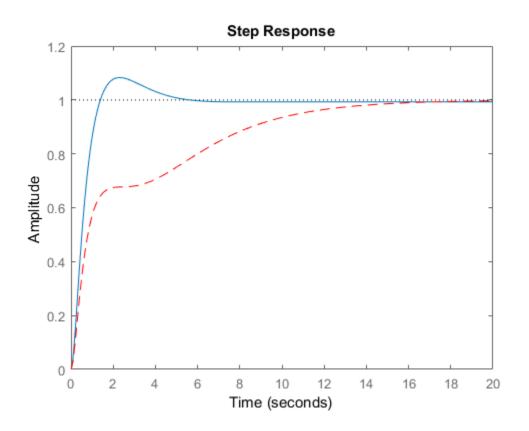


Convert C1 to a 2-DOF controller with different b and c values.

 $C2_2 = make2DOF(C1, 0.5, 0.75)$

The PID gains and filter constant are still unchanged, but the setpoint weights now change the closed-loop response.

CM_2 = tf(C2_2); T2_2 = CM_2(1)*feedback(G,-CM_2(2)); stepplot(T1,T2_2,'r--')



Input Arguments

C1 — 1-DOF PID controller pid object | pidstd object 1-DOF PID controller, specified as a pid object or a pidstd object.

b - Setpoint weight on proportional term

1 (default) | real nonnegative scalar

Setpoint weight on proportional term, specified as a real, nonnegative, finite value. If you do not specify b, then C2 has b = 1.

c - Setpoint weight on derivative term

1 (default) | real nonnegative scalar

Setpoint weight on derivative term, specified as a real, nonnegative, finite value. If you do not specify c, then C2 has c = 1.

Output Arguments

C2 - 2-DOF PID controller

pid2 object | pidstd2 object

2-DOF PID controller, returned as a pid2 object or pidstd2 object. C2 is in parallel form if C1 is in parallel form, and standard form if C1 is in standard form.

For example, suppose C1 is a continuous-time, parallel-form pid controller of the form:

$$C_1 = K_p + \frac{K_i}{s} + \frac{K_d s}{T_f s + 1}.$$

Then C2 is a parallel-form 2-DOF pid2 controller, which has two inputs and one output. The relationship between the inputs, r and y, and the output u of C2 is given by:

$$u = K_p \left(br - y \right) + \frac{K_i}{s} \left(r - y \right) + \frac{K_d s}{T_f s + 1} \left(cr - y \right).$$

The PID gains K_p , K_i , and K_d , and the filter time constant T_f are unchanged. The setpoint weights b and c are specified by the input arguments **b** and **c**, or 1 by default. For more information about 2-DOF PID controllers, see "Two-Degree-of-Freedom PID Controllers".

The conversion also preserves the values of the properties TS, TimeUnit, Sampling Grid, IFormula, and DFormula.

More About

"Two-Degree-of-Freedom PID Controllers"

See Also

getComponents | make1DOF | pid | pid2 | pidstd | pidstd2

Introduced in R2015b

margin

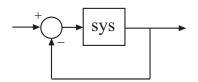
Gain margin, phase margin, and crossover frequencies

Syntax

```
[Gm,Pm,Wgm,Wpm] = margin(sys)
[Gm,Pm,Wgm,Wpm] = margin(mag,phase,w)
margin(sys)
```

Description

margin calculates the minimum gain margin, Gm, phase margin, Pm, and associated frequencies Wgm and Wpm of SISO open-loop models. The gain and phase margin of a system Sys indicates the relative stability of the closed-loop system formed by applying unit negative feedback to sys, as in the following illustration.



The gain margin is the amount of gain increase or decrease required to make the loop gain unity at the frequency Wgm where the phase angle is -180° (modulo 360°). In other words, the gain margin is 1/g if g is the gain at the -180° phase frequency. Similarly, the phase margin is the difference between the phase of the response and -180° when the loop gain is 1.0. The frequency Wpm at which the magnitude is 1.0 is called the *unity-gain frequency* or *gain crossover frequency*. It is generally found that gain margins of three or more combined with phase margins between 30 and 60 degrees result in reasonable trade-offs between bandwidth and stability.

[Gm,Pm,Wgm,Wpm] = margin(sys) computes the gain margin Gm, the phase margin Pm, and the corresponding frequencies Wgm and Wpm, given the SISO open-loop dynamic system model sys. Wgm is the frequency where the gain margin is measured, which is

a -180 degree phase crossing frequency. Wpm is the frequency where the phase margin is measured, which is a 0dB gain crossing frequency. These frequencies are expressed in radians/TimeUnit, where TimeUnit is the unit specified in the TimeUnit property of sys. When sys has several crossovers, margin returns the smallest gain and phase margins and corresponding frequencies.

The phase margin Pm is in degrees. The gain margin Gm is an absolute magnitude. You can compute the gain margin in dB by

 $Gm_dB = 20 \times \log 10(Gm)$

[Gm, Pm, Wgm, Wpm] = margin(mag, phase, w) derives the gain and phase margins from Bode frequency response data (magnitude, phase, and frequency vector). margin interpolates between the frequency points to estimate the margin values. Provide the gain data mag in absolute units, and phase data phase in degrees. You can provide the frequency vector w in any units; margin returns Wgm and Wpm in the same units.

Note: When you use margin(mag,phase,w), margin relies on interpolation to approximate the margins, which generally produces less accurate results. For example, if there is no 0 dB crossing within the w range, margin returns a phase margin of Inf. Therefore, if you have an analytical model sys, using [Gm,Pm,Wgm,Wpm] = margin(sys) is the most robust way to obtain the margins.

margin(sys), without output arguments, plots the Bode response of sys on the screen and indicates the gain and phase margins on the plot. By default, gain margins are expressed in dB on the plot.

Examples

Gain and Phase Margins of Open-Loop Transfer Function

Create an open-loop discrete-time transfer function.

```
hd = tf([0.04798 0.0464],[1 -1.81 0.9048],0.1)
```

hd =

0.04798 z + 0.0464

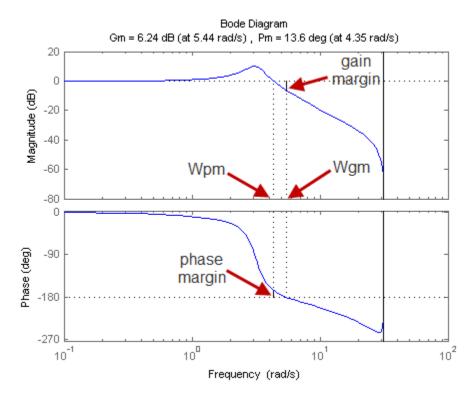
z^2 - 1.81 z + 0.9048

```
Sample time: 0.1 seconds
Discrete-time transfer function.
```

Compute the gain and phase margins.

Display the gain and phase margins graphically.

margin(hd)



Solid vertical lines mark the gain margin and phase margin. The dashed vertical lines indicate the locations of Wpm, the frequency where the phase margin is measured, and Wgm, the frequency where the gain margin is measured.

More About

Algorithms

The phase margin is computed using H_{∞} theory, and the gain margin by solving $H(j\omega) = \overline{H(j\omega)}$ for the frequency ω .

See Also

bode | linearSystemAnalyzer

Introduced before R2006a

minreal

Minimal realization or pole-zero cancelation

Syntax

```
sysr = minreal(sys)
sysr = minreal(sys,tol)
[sysr,u] = minreal(sys,tol)
... = minreal(sys,tol,false)
... = minreal(sys,[],false)
```

Description

sysr = minreal(sys) eliminates uncontrollable or unobservable state in state-space models, or cancels pole-zero pairs in transfer functions or zero-pole-gain models. The output sysr has minimal order and the same response characteristics as the original model sys.

sysr = minreal(sys,tol) specifies the tolerance used for state elimination or polezero cancellation. The default value is tol = sqrt(eps) and increasing this tolerance forces additional cancellations.

```
[sysr,u] = minreal(sys,tol) returns, for state-space model sys, an orthogonal matrix U such that (U^*A^*U', U^*B, C^*U') is a Kalman decomposition of (A, B, C)
```

... = minreal(sys,tol,false) and ... = minreal(sys,[],false) disable the verbose output of the function. By default, minreal displays a message indicating the number of states removed from a state-space model sys.

Examples

The commands

g = zpk([],1,1); h = tf([2 1],[1 0]);

```
cloop = inv(1+g*h) * g
```

produce the nonminimal zero-pole-gain model cloop.

cloop =

s (s-1) (s-1) (s² + s + 1)

Continuous-time zero/pole/gain model.

To cancel the pole-zero pair at s = 1, type

cloopmin = minreal(cloop)

This command produces the following result.

cloopmin =

s (s^2 + s + 1)

Continuous-time zero/pole/gain model.

More About

Algorithms

Pole-zero cancellation is a straightforward search through the poles and zeros looking for matches that are within tolerance. Transfer functions are first converted to zero-pole-gain form.

See Also

balreal | modred | sminreal

Introduced before R2006a

modred

Model order reduction

Syntax

```
rsys = modred(sys,elim)
rsys = modred(sys,elim,'method')
```

Description

rsys = modred(sys, elim) reduces the order of a continuous or discrete state-space model sys by eliminating the states found in the vector elim. The full state vector X is partitioned as X = [X1;X2] where X1 is the reduced state vector and X2 is discarded.

elim can be a vector of indices or a logical vector commensurate with X where true values mark states to be discarded. This function is usually used in conjunction with balreal. Use balreal to first isolate states with negligible contribution to the I/O response. If sys has been balanced with balreal and the vector g of Hankel singular values has M small entries, you can use modred to eliminate the corresponding M states. For example:

```
[sys,g] = balreal(sys) % Compute balanced realization
elim = (g<1e-8) % Small entries of g are negligible states
rsys = modred(sys,elim) % Remove negligible states
```

rsys = modred(sys,elim, 'method') also specifies the state elimination method. Choices for 'method' include

- 'MatchDC' (default): Enforce matching DC gains. The state-space matrices are recomputed as described in "Algorithms" on page 1-501.
- 'Truncate': Simply delete X2.

The 'Truncate' option tends to produces a better approximation in the frequency domain, but the DC gains are not guaranteed to match.

If the state-space model sys has been balanced with balreal and the grammians have m small diagonal entries, you can reduce the model order by eliminating the last m states with modred.

Examples

Order Reduction by Matched-DC-Gain and Direct-Deletion Methods

Consider the following continuous fourth-order model.

$$h(s) = \frac{s^3 + 11s^2 + 36s + 26}{s^4 + 14.6s^3 + 74.96s^2 + 153.7s + 99.65}$$

To reduce its order, first compute a balanced state-space realization with balreal.

h = tf([1 11 36 26],[1 14.6 74.96 153.7 99.65]);
[hb,g] = balreal(h);

Examine the gramians.

g'

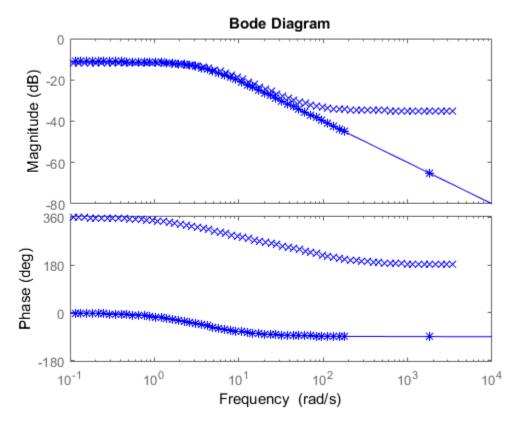
ans = 0.1394 0.0095 0.0006 0.0000

The last three diagonal entries of the balanced gramians are relatively small. Eliminate these three least-contributing states with modred, using both matched-DC-gain and direct-deletion methods.

```
hmdc = modred(hb,2:4,'MatchDC');
hdel = modred(hb,2:4,'Truncate');
```

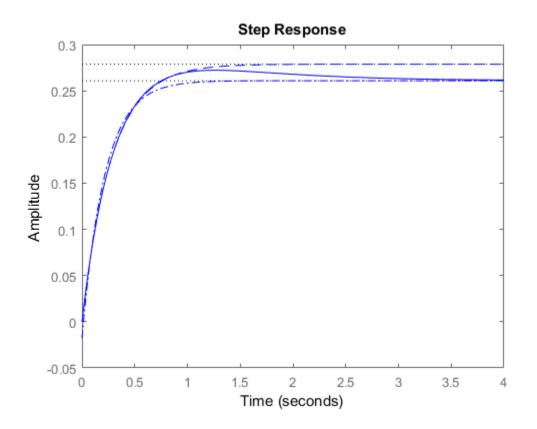
Both hmdc and hdel are first-order models. Compare their Bode responses against that of the original model.

```
bodeplot(h,'-',hmdc,'x',hdel,'*')
```



The reduced-order model hdel is clearly a better frequency-domain approximation of h. Now compare the step responses.

stepplot(h,'-',hmdc,'-.',hdel,'--')



While ${\tt hdel}$ accurately reflects the transient behavior, only ${\tt hmdc}$ gives the true steady-state response.

Limitations

With the matched DC gain method, A_{22} must be invertible in continuous time, and $I - A_{22}$ must be invertible in discrete time.

More About

Algorithms

The algorithm for the matched DC gain method is as follows. For continuous-time models

$$\dot{x} = Ax + By$$
$$y = Cx + Du$$

the state vector is partitioned into x_1 , to be kept, and x_2 , to be eliminated.

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} A_{11} & A_{12} \\ A_{21} & A_{22} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} B_1 \\ B_2 \end{bmatrix} u$$
$$y = \begin{bmatrix} C_1 & C_2 \end{bmatrix} x + Du$$

Next, the derivative of x_2 is set to zero and the resulting equation is solved for x_1 . The reduced-order model is given by

$$\dot{x}_{1} = \left[A_{11} - A_{12}A_{22}^{-1}A_{21}\right]x_{1} + \left[B_{1} - A_{12}A_{22}^{-1}B_{2}\right]u$$
$$y = \left[C_{1} - C_{2}A_{22}^{-1}A_{21}\right]x + \left[D - C_{2}A_{22}^{-1}B_{2}\right]u$$

The discrete-time case is treated similarly by setting

$$x_2[n+1] = x_2[n]$$

See Also balreal | minreal

modsep

Region-based modal decomposition

Syntax

```
[H,H0] = modsep(G,N,REGIONFCN)
MODSEP(G,N,REGIONFCN,PARAM1,...)
```

Description

[H,H0] = modsep(G,N,REGIONFCN) decomposes the LTI model G into a sum of n simpler models Hj with their poles in disjoint regions Rj of the complex plane:

 $G(s) = H0 + \sum_{j=1}^{N} Hj(s)$

G can be any LTI model created with ss, tf, or zpk, and N is the number of regions used in the decomposition. modsep packs the submodels Hj into an LTI array H and returns the static gain HO separately. Use H(:,:,j) to retrieve the submodel Hj(s).

To specify the regions of interest, use a function of the form

IR = REGIONFCN(p)

that assigns a region index IR between 1 and N to a given pole p. You can specify this function as a string or a function handle, and use the syntax MODSEP(G,N,REGIONFCN,PARAM1,...) to pass extra input arguments:

IR = REGIONFCN(p,PARAM1,...)

Examples

To decompose G into G(z) = H0 + H1(z) + H2(z) where H1 and H2 have their poles inside and outside the unit disk respectively, use

[H,HO] = modsep(G,2,@udsep)

where the function udsep is defined by

function r = udsep(p)if abs(p)<1, r = 1; % assign r=1 to poles inside unit disk else r = 2; % assign r=2 to poles outside unit disk end

To extract H1(z) and H2(z) from the LTI array H, use

H1 = H(:,:,1); H2 = H(:,:,2);

See Also

stabsep

nblocks

Number of blocks in Generalized matrix or Generalized LTI model

Syntax

N = nblocks(M)

Description

N = nblocks(M) returns the number of "Control Design Blocks" in the Generalized LTI model or Generalized matrix M.

Input Arguments

М

AGeneralized LTI model (genss or genfrd model), a Generalized matrix (genmat), or an array of such models.

Output Arguments

Ν

The number of "Control Design Blocks" in M. If a block appears multiple times in $M,\,N$ reflects the total number of occurrences.

If M is a model array, N is an array with the same dimensions as M. Each entry of N is the number of Control Design Blocks in the corresponding entry of M.

Examples

Number of Control Design Blocks in a Second-Order Filter Model

This example shows how to use nblocks to examine two different ways of parametrizing a model of a second-order filter.

1 Create a tunable (parametric) model of the second-order filter:

$$F(s) = \frac{\omega_n^2}{s^2 + 2\zeta\omega_n + \omega_n^2},$$

where the damping ζ and the natural frequency ω_n are tunable parameters.

wn = realp('wn',3); zeta = realp('zeta',0.8); F = tf(wn^2,[1 2*zeta*wn wn^2]);

F is a genss model with two tunable Control Design Blocks, the realp blocks wn and zeta. The blocks wn and zeta have initial values of 3 and 0.8, respectively.

2 Examine the number of tunable blocks in the model using nblocks.

```
nblocks(F)
```

This command returns the result:

ans =

6

 ${\sf F}$ has two tunable parameters, but the parameter wn appears five times—twice in the numerator and three times in the denominator.

3 Rewrite F for fewer occurrences of wn.

The second-order filter transfer function can be expressed as follows:

$$F(s) = \frac{1}{\left(\frac{s}{\omega_n}\right)^2 + 2\zeta\left(\frac{s}{\omega_n}\right) + 1}.$$

Use this expression to create the tunable filter:

F = tf(1,[(1/wn)^2 2*zeta*(1/wn) 1])

4 Examine the number of tunable blocks in the new filter model.

nblocks(F)

This command returns the result:

ans =

4

In the new formulation, there are only three occurrences of the tunable parameter wn. Reducing the number of occurrences of a block in a model can improve performance time of calculations involving the model. However, the number of occurrences does not affect the results of tuning the model or sampling the model for parameter studies.

More About

- "Control Design Blocks"
- "Generalized Matrices"
- "Generalized and Uncertain LTI Models"

See Also

genss | genfrd | genmat | getValue

Introduced in R2011a

ndims

Query number of dimensions of dynamic system model or model array

Syntax

```
n = ndims(sys)
```

Description

n = ndims(sys) is the number of dimensions of a dynamic system model or a model array sys. A single model has two dimensions (one for outputs, and one for inputs). A model array has 2 + p dimensions, where $p \ge 2$ is the number of array dimensions. For example, a 2-by-3-by-4 array of models has 2 + 3 = 5 dimensions.

```
ndims(sys) = length(size(sys))
```

Examples

ndims returns 4 for this 3-by-1 array of SISO models.

See Also

size

ngrid

Superimpose Nichols chart on Nichols plot

Syntax

ngrid

Description

ngrid superimposes Nichols chart grid lines over the Nichols frequency response of a SISO LTI system. The range of the Nichols grid lines is set to encompass the entire Nichols frequency response.

The chart relates the complex number H/(1 + H) to H, where H is any complex number. For SISO systems, when H is a point on the open-loop frequency response, then

$$\frac{H}{1+H}$$

is the corresponding value of the closed-loop frequency response assuming unit negative feedback.

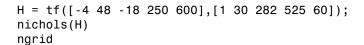
If the current axis is empty, ngrid generates a new Nichols chart grid in the region – 40 dB to 40 dB in magnitude and –360 degrees to 0 degrees in phase. If the current axis does not contain a SISO Nichols frequency response, ngrid returns a warning.

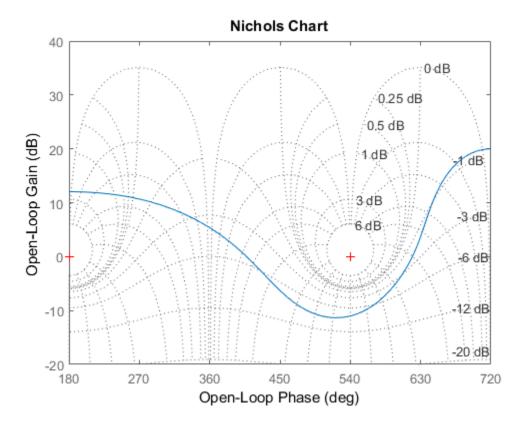
Examples

Nichols Response with Nichols Grid Lines

Plot the Nichols response with Nichols grid lines for the following system:

$$H(s) = \frac{-4s^4 + 48s^3 - 18s^2 + 250s + 600}{s^4 + 30s^3 + 282s^2 + 525s + 60}.$$





The right-click menu for Nichols charts includes the **Tight** option under **Zoom**. You can use this to clip unbounded branches of the Nichols chart.

See Also

nichols

nichols

Nichols chart of frequency response

Syntax

```
nichols(sys)
nichols(sys,w)
nichols(sys1,sys2,...,sysN)
nichols(sys1,sys2,...,sysN,w)
nichols(sys1,'PlotStyle1',...,sysN,'PlotStyleN')
[mag,phase,w] = nichols(sys)
[mag,phase] = nichols(sys,w)
```

Description

nichols creates a Nichols chart of the frequency response. A Nichols chart displays the magnitude (in dB) plotted against the phase (in degrees) of the system response. Nichols charts are useful to analyze open- and closed-loop properties of SISO systems, but offer little insight into MIMO control loops. Use ngrid to superimpose a Nichols chart on an existing SISO Nichols chart.

nichols(sys) creates a Nichols chart of the dynamic system sys. This model can be continuous or discrete, SISO or MIMO. In the MIMO case, nichols produces an array of Nichols charts, each plot showing the response of one particular I/O channel. The frequency range and gridding are determined automatically based on the system poles and zeros.

nichols(sys,w) specifies the frequency range or frequency points to be used for the chart. To focus on a particular frequency interval [wmin,wmax], set w = {wmin,wmax}. To use particular frequency points, set w to the vector of desired frequencies. Use logspace to generate logarithmically spaced frequency vectors. Frequencies must be in rad/TimeUnit, where TimeUnit is the time units of the input dynamic system, specified in the TimeUnit property of sys.

```
nichols(sys1,sys2,...,sysN) or nichols(sys1,sys2,...,sysN,w)
superimposes the Nichols charts of several models on a single figure. All
```

systems must have the same number of inputs and outputs, but may otherwise be a mix of continuous- and discrete-time systems. You can also specify a distinctive color, linestyle, and/or marker for each system plot with the syntax nichols(sys1,'PlotStyle1',...,sysN,'PlotStyleN').

See bode for an example.

[mag,phase,w] = nichols(sys) or [mag,phase] = nichols(sys,w) returns the magnitude and phase (in degrees) of the frequency response at the frequencies w (in rad/ TimeUnit). The outputs mag and phase are 3-D arrays similar to those produced by bode (see the bode reference page). They have dimensions (number of outputs) × (number of inputs) × (length of w)

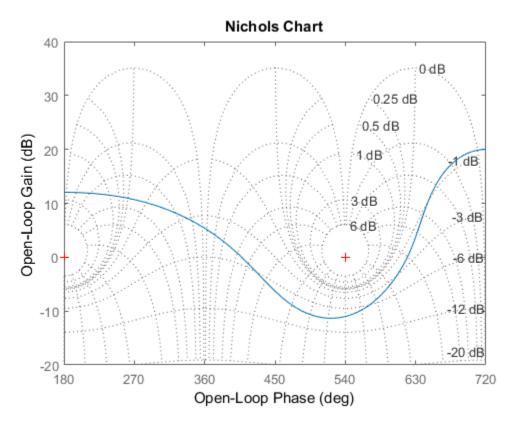
Examples

Nichols Response with Nichols Grid Lines

Plot the Nichols response with Nichols grid lines for the following system:

$$H(s) = \frac{-4s^4 + 48s^3 - 18s^2 + 250s + 600}{s^4 + 30s^3 + 282s^2 + 525s + 60}.$$

H = tf([-4 48 -18 250 600],[1 30 282 525 60]);
nichols(H)
ngrid



The right-click menu for Nichols charts includes the **Tight** option under **Zoom**. You can use this to clip unbounded branches of the Nichols chart.

More About

Tips

You can change the properties of your plot, for example the units. For information on the ways to change properties of your plots, see "Ways to Customize Plots".

Algorithms

 $See \; \text{bode}.$

See Also

bode | evalfr | freqresp | linearSystemAnalyzer | ngrid | nyquist | sigma

nicholsoptions

Create list of Nichols plot options

Syntax

```
P = nicholsoptions
P = nicholsoptions('cstprefs')
```

Description

P = nicholsoptions returns a list of available options for Nichols plots with default values set. You can use these options to customize the Nichols plot appearance from the command line.

P = nicholsoptions('cstprefs') initializes the plot options with the options you selected in the Control System Toolbox Preferences Editor. For more information about the editor, see "Toolbox Preferences Editor" in the User's Guide documentation.

This table summarizes the Nichols plot options.

Option	Description
Title, XLabel, YLabel	Label text and style
TickLabel	Tick label style
Grid	Show or hide the grid Specified as one of the following strings: 'off' 'on' Default : 'off'
GridColor	Color of the grid lines Specified as one of the following: Vector of RGB values in the range [0,1] color string 'none'. Default: [0.15,0.15,0.15]
XlimMode, YlimMode	Limit modes
Xlim, Ylim	Axes limits

Option	Description
IOGrouping	Grouping of input-output pairs Specified as one of the following strings: 'none' 'inputs' 'outputs' 'all' Default: 'none'
InputLabels, OutputLabels	Input and output label styles.
InputVisible, OutputVisible	Visibility of input and output channels

Option	Description
FreqUnits	Frequency units, specified as one of the following strings:
	• 'Hz'
	• 'rad/second'
	• 'rpm'
	• 'kHz'
	• 'MHz'
	• 'GHz'
	 'rad/nanosecond'
	 'rad/microsecond'
	 'rad/millisecond'
	• 'rad/minute'
	• 'rad/hour'
	• 'rad/day'
	<pre>• 'rad/week'</pre>
	<pre>• 'rad/month'</pre>
	• 'rad/year'
	 'cycles/nanosecond'
	 'cycles/microsecond'
	 'cycles/millisecond'
	• 'cycles/hour'
	• 'cycles/day'
	 'cycles/week'
	 'cycles/month'
	• 'cycles/year'
	Default: 'rad/s'
	You can also specify 'auto' which uses frequency units rad/TimeUnit relative

Option	Description
	to system time units specified in the TimeUnit property. For multiple systems with different time units, the units of the first system are used.
MagLowerLimMode	Enables a lower magnitude limit Specified as one of the following strings: 'auto' 'manual' Default: 'auto'
MagLowerLim	Specifies the lower magnitude limit
PhaseUnits	Phase units Specified as one of the following strings: 'deg' 'rad' Default: 'deg'
PhaseWrapping	Enables phase wrapping Specified as one of the following strings: 'on' 'off' Default: 'off'
PhaseMatching	Enables phase matching Specified as one of the following strings: 'on' 'off' Default : 'off'
PhaseMatchingFreq	Frequency for matching phase
PhaseMatchingValue	The value to make the phase responses close to

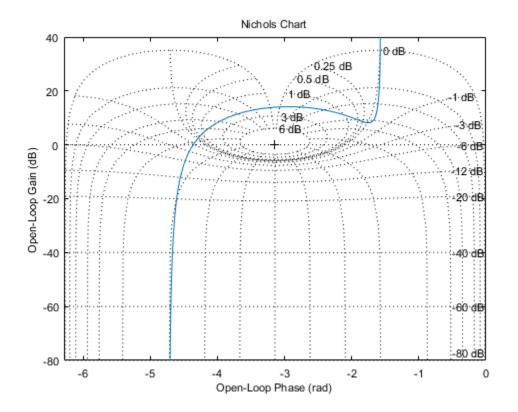
Examples

Set Options for Nichols Plot

Create an options set, and set the phase units and grid option.

```
P = nicholsoptions;
P.PhaseUnits = 'rad';
P.Grid = 'on';
```

Use the options set to generate a Nichols plot. Not the phase units and grid in the plot.



h = nicholsplot(tf(1,[1,.2,1,0]),P);

See Also getoptions | nicholsplot | setoptions

Introduced in R2008a

nicholsplot

Plot Nichols frequency responses and return plot handle

Syntax

```
h = nicholsplot(sys)
nicholsplot(sys,{wmin,wmax})
nicholsplot(sys,w)
nicholsplot(sys1,sys2,...,w)
nicholsplot(AX,...)
nicholsplot(..., plotoptions)
```

Description

h = nicholsplot(sys) draws the Nichols plot of the dynamic system sys. It also returns the plot handle h. You can use this handle to customize the plot with the getoptions and setoptions commands. Type

help nicholsoptions

for a list of available plot options.

The frequency range and number of points are chosen automatically. See **bode** for details on the notion of frequency in discrete time.

nicholsplot(sys, {wmin,wmax}) draws the Nichols plot for frequencies between
wmin and wmax (in rad/TimeUnit, where TimeUnit is the time units of the input
dynamic system, specified in the TimeUnit property of sys).

nicholsplot(sys,w) uses the user-supplied vector w of frequencies, in rad/ TimeUnit, at which the Nichols response is to be evaluated. See logspace to generate logarithmically spaced frequency vectors.

nicholsplot(sys1,sys2,...,w) draws the Nichols plots of multiple models
sys1,sys2,... on a single plot. The frequency vector w is optional. You can also specify a
color, line style, and marker for each system, as in

```
nicholsplot(sys1,'r',sys2,'y--',sys3,'gx').
```

nicholsplot(AX,...) plots into the axes with handle AX.

nicholsplot(..., plotoptions) plots the Nichols plot with the options specified in
plotoptions. Type

help nicholsoptions

for more details.

Examples

Generate Nichols plot and use plot handle to change frequency units to Hz

```
sys = rss(5);
h = nicholsplot(sys);
% Change units to Hz
setoptions(h,'FreqUnits','Hz');
```

More About

Tips

You can change the properties of your plot, for example the units. For information on the ways to change properties of your plots, see "Ways to Customize Plots".

See Also

getoptions | nichols | nicholsoptions | setoptions

nmodels

Number of models in model array

Syntax

```
N = nmodels(sysarray)
```

Description

N = nmodels(sysarray) returns the number of models in an array of dynamic system models or static models.

Examples

Number of Models in Array

Create a 2-by-3-by-5 array of state-space models and confirm the number of models in the array.

```
sysarr = rss(2,2,2,2,3,4);
N = nmodels(sysarr)
N =
24
```

Input Arguments

sysarray — Input model array

model array

Input model array, specified as an array of input-output models such as numeric LTI models, generalized models, or identified LTI models.

Output Arguments

N - Number of models in array

positive integer

Number of models in the input model array, returned as a positive integer.

See Also

ndims | size

Introduced in R2013a

norm

Norm of linear model

Syntax

```
n = norm(sys)
n = norm(sys,2)
n = norm(sys,inf)
[n,fpeak] = norm(sys,inf)
[...] = norm(sys,inf,tol)
```

Description

n = norm(sys) or n = norm(sys, 2) return the H_2 norm of the linear dynamic system model sys.

n = norm(sys, inf) returns the H_{∞} norm of sys.

[n,fpeak] = norm(sys,inf) also returns the frequency fpeak at which the gain reaches its peak value.

[...] = norm(sys, inf, tol) sets the relative accuracy of the H_{∞} norm to tol.

Input Arguments

sys

Continuous- or discrete-time linear dynamic system model. ${\tt sys}$ can also be an array of linear models.

tol

Positive real value setting the relative accuracy of the H_{∞} norm.

Default: 0.01

Output Arguments

n

 H_2 norm or H_∞ norm of the linear model sys.

If sys is an array of linear models, n is an array of the same size as sys. In that case each entry of n is the norm of each entry of sys.

fpeak

Frequency at which the peak gain of sys occurs.

Examples

This example uses norm to compute the H_2 and H_∞ norms of a discrete-time linear system.

Consider the discrete-time transfer function

$$H(z) = \frac{z^3 - 2.841z^2 + 2.875z - 1.004}{z^3 - 2.417z^2 + 2.003z - 0.5488}$$

with sample time 0.1 second.

To compute the H_2 norm of this transfer function, enter:

```
H = tf([1 -2.841 2.875 -1.004], [1 -2.417 2.003 -0.5488], 0.1)norm(H)
```

These commands return the result:

```
ans =
1.2438
```

To compute the H_{∞} infinity norm, enter:

```
[ninf,fpeak] = norm(H,inf)
```

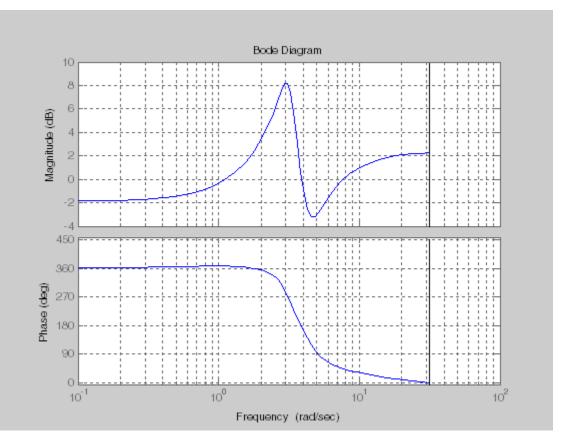
This command returns the result:

ninf =

2.5488 fpeak = 3.0844

You can use a Bode plot of H(z) to confirm these values.

bode(H)
grid on;



The gain indeed peaks at approximately 3 rad/sec. To find the peak gain in dB, enter: 20*log10(ninf)

This command produces the following result:

ans = 8.1268

More About

H2 norm

The H_2 norm of a stable continuous-time system with transfer function H(s), is given by:

$$\left\|H\right\|_{2} = \sqrt{\frac{1}{2\pi}\int_{-\infty}^{\infty} \operatorname{Trace}\left[H(j\omega)^{H}H(j\omega)\right]d\omega}.$$

For a discrete-time system with transfer function H(z), the H_2 norm is given by:

$$\left\|H\right\|_{2} = \sqrt{\frac{1}{2\pi} \int_{-\pi}^{\pi} \operatorname{Trace}\left[H(e^{j\omega})^{H} H(e^{j\omega})\right] d\omega}.$$

The H_2 norm is equal to the root-mean-square of the impulse response of the system. The H_2 norm measures the steady-state covariance (or power) of the output response y = Hw to unit white noise inputs w:

$$\|H\|_2^2 = \lim_{t \to \infty} E\left\{y(t)^T y(t)\right\}, \qquad E\left(w(t)w(\tau)^T\right) = \delta\left(t - \tau\right)I.$$

The H_2 norm is infinite in the following cases:

- sys is unstable.
- **Sys** is continuous and has a nonzero feedthrough (that is, nonzero gain at the frequency $\omega = \infty$).

norm(sys) produces the same result as

```
sqrt(trace(covar(sys,1)))
```

H-infinity norm

The H_{∞} norm (also called the L_{∞} norm) of a SISO linear system is the peak gain of the frequency response. For a MIMO system, the H_{∞} norm is the peak gain across all input/ output channels. Thus, for a continuous-time system H(s), the H_{∞} norm is given by:

$$\begin{split} \left\| H\left(s\right) \right\|_{\infty} &= \max_{\omega} \left| H\left(j\omega\right) \right| \qquad (\text{SISO}) \\ \left\| H\left(s\right) \right\|_{\infty} &= \max_{\omega} \sigma_{\max} \left(H\left(j\omega\right) \right) \qquad (\text{MIMO}) \end{split}$$

where $\sigma_{max}(\cdot)$ denotes the largest singular value of a matrix.

For a discrete-time system H(z):

$$\begin{split} \left\| H\left(z\right) \right\|_{\infty} &= \max_{\theta \in [0,\pi]} \left| H\left(e^{j\theta}\right) \right| \qquad \text{(SISO)} \\ \left\| H\left(z\right) \right\|_{\infty} &= \max_{\theta \in [0,\pi]} \sigma_{\max}\left(H\left(e^{j\theta}\right) \right) \qquad \text{(MIMO)} \end{split}$$

The H_{∞} norm is infinite if **sys** has poles on the imaginary axis (in continuous time), or on the unit circle (in discrete time).

Algorithms

norm first converts sys to a state space model.

norm uses the same algorithm as covar for the H_2 norm. For the H_{∞} norm, norm uses the algorithm of [1]. norm computes the H_{∞} norm (peak gain) using the SLICOT library. For more information about the SLICOT library, see http://slicot.org.

References

 Bruisma, N.A. and M. Steinbuch, "A Fast Algorithm to Compute the H_∞-Norm of a Transfer Function Matrix," System Control Letters, 14 (1990), pp. 287-293.

See Also

freqresp | sigma

nyquist

Nyquist plot of frequency response

Syntax

```
nyquist(sys)
nyquist(sys,w)
nyquist(sys1,sys2,...,sysN)
nyquist(sys1,sys2,...,sysN,w)
nyquist(sys1,'PlotStyle1',...,sysN,'PlotStyleN')
[re,im,w] = nyquist(sys)
[re,im] = nyquist(sys,w)
[re,im,w,sdre,sdim] = nyquist(sys)
```

Description

nyquist creates a Nyquist plot of the frequency response of a dynamic system model. When invoked without left-hand arguments, **nyquist** produces a Nyquist plot on the screen. Nyquist plots are used to analyze system properties including gain margin, phase margin, and stability.

nyquist(sys) creates a Nyquist plot of a dynamic system sys. This model can be continuous or discrete, and SISO or MIMO. In the MIMO case, nyquist produces an array of Nyquist plots, each plot showing the response of one particular I/O channel. The frequency points are chosen automatically based on the system poles and zeros.

nyquist(sys,w) explicitly specifies the frequency range or frequency points to be used for the plot. To focus on a particular frequency interval, set w = {wmin,wmax}. To use particular frequency points, set w to the vector of desired frequencies. Use logspace to generate logarithmically spaced frequency vectors. Frequencies must be in rad/ TimeUnit, where TimeUnit is the time units of the input dynamic system, specified in the TimeUnit property of sys.

nyquist(sys1,sys2,...,sysN) or nyquist(sys1,sys2,...,sysN,w) superimposes the Nyquist plots of several LTI models on a single figure. All systems must have the same number of inputs and outputs, but may otherwise be a mix of continuous- and discrete-time systems. You can also specify a

distinctive color, linestyle, and/or marker for each system plot with the syntax nyquist(sys1, 'PlotStyle1',...,sysN, 'PlotStyleN').

[re,im,w] = nyquist(sys) and [re,im] = nyquist(sys,w) return the real and imaginary parts of the frequency response at the frequencies w (in rad/TimeUnit). re and im are 3-D arrays (see "Arguments" below for details).

[re,im,w,sdre,sdim] = nyquist(sys) also returns the standard deviations of re
and im for the identified system sys.

Arguments

The output arguments re and im are 3-D arrays with dimensions

(number of outputs) \times (number of inputs) \times (length of w)

For SISO systems, the scalars re(1,1,k) and im(1,1,k) are the real and imaginary parts of the response at the frequency $\omega_k = w(k)$.

 $\operatorname{re}(1,1,k) = \operatorname{Re}(h(j\omega_k))$ $\operatorname{im}(1,1,k) = \operatorname{Im}(h(jw_k))$

For MIMO systems with transfer function H(s), re(:,:,k) and im(:,:,k) give the real and imaginary parts of $H(j\omega_k)$ (both arrays with as many rows as outputs and as many columns as inputs). Thus,

$$\begin{split} &\operatorname{re}(\mathbf{i},\mathbf{j},\mathbf{k}) = \operatorname{Re}\left(h_{ij}(j\omega_k)\right) \\ &\operatorname{im}(\mathbf{i},\mathbf{j},\mathbf{k}) = \operatorname{Im}\left(h_{ij}(j\omega_k)\right) \end{split}$$

where h_{ij} is the transfer function from input *j* to output *i*.

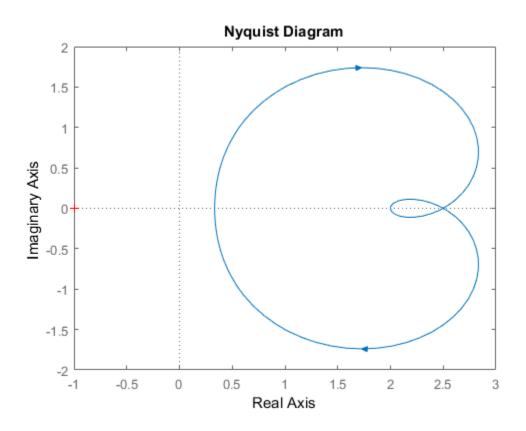
Examples

Nyquist Plot of Dynamic System

Plot the Nyquist response of the system

$$H(s) = \frac{2s^2 + 5s + 1}{s^2 + 2s + 3}$$

H = tf([2 5 1],[1 2 3]);
nyquist(H)



The nyquist function has support for M-circles, which are the contours of the constant closed-loop magnitude. M-circles are defined as the locus of complex numbers where

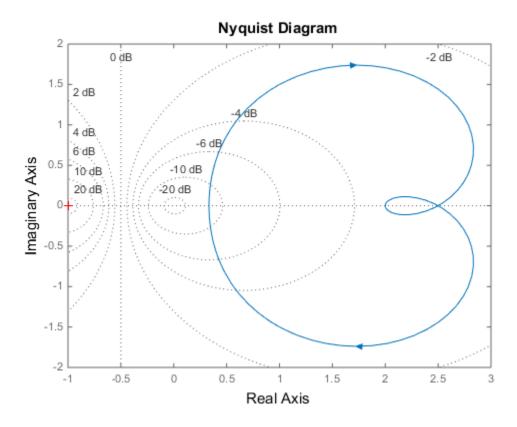
$$T(j\omega) = \left| \frac{G(j\omega)}{1 + G(j\omega)} \right|$$

is a constant value. In this equation, ω is the frequency in radians/TimeUnit, where TimeUnit is the system time units, and *G* is the collection of complex numbers that satisfy the constant magnitude requirement.

To activate the grid, select Grid from the right-click menu or type

grid

at the MATLAB prompt. This figure shows the M circles for transfer function H.

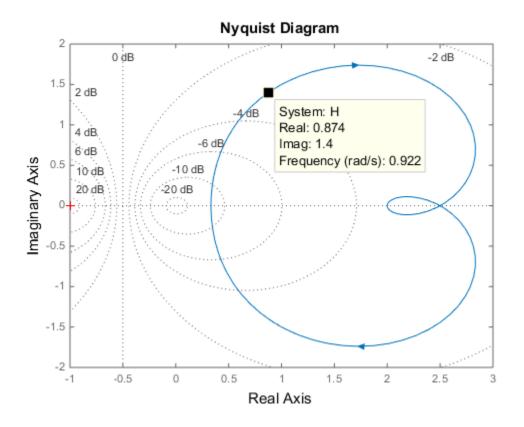


You have two zoom options available from the right-click menu that apply specifically to Nyquist plots:

• **Tight**—Clips unbounded branches of the Nyquist plot, but still includes the critical point (-1, 0)

• On (-1,0) — Zooms around the critical point (-1,0)

Also, click anywhere on the curve to activate data markers that display the real and imaginary values at a given frequency. This figure shows the nyquist plot with a data marker.



Nyquist Plot of Identified Model with Response Uncertainty

Compute the standard deviation of the real and imaginary parts of frequency response of an identified model. Use this data to create a 3σ plot of the response uncertainty. (Identified models require System Identification Toolbox.)

Identify a transfer function model based on data. Obtain the standard deviation data for the real and imaginary parts of the frequency response.

```
load iddata2 z2;
sys_p = tfest(z2,2);
w = linspace(-10*pi,10*pi,512);
[re, im, ~, sdre, sdim] = nyquist(sys_p,w);
```

 sys_p is an identified transfer function model. sdre and sdim contain 1-std standard deviation uncertainty values in re and im respectively.

Create a Nyquist plot showing the response and its 30 uncertainty:

```
re = squeeze(re);
im = squeeze(im);
sdre = squeeze(sdre);
sdim = squeeze(sdim);
plot(re,im,'b', re+3*sdre, im+3*sdim, 'k:', re-3*sdre, im-3*sdim, 'k:')
```

More About

Tips

You can change the properties of your plot, for example the units. For information on the ways to change properties of your plots, see "Ways to Customize Plots".

Algorithms

See bode.

See Also

evalfr | freqresp | bode | linearSystemAnalyzer | nichols | sigma

nyquistoptions

List of Nyquist plot options

Syntax

```
P = nyquistoptions
P = nyquistoptions('cstprefs')
```

Description

P = nyquistoptions returns the default options for Nyquist plots. You can use these options to customize the Nyquist plot appearance using the command line.

P = nyquistoptions('cstprefs') initializes the plot options with the options you selected in the Control System and System Identification Toolbox Preferences Editor. For more information about the editor, see "Toolbox Preferences Editor" in the User's Guide documentation.

The following table summarizes the Nyquist plot options.

Option	Description
Title, XLabel, YLabel	Label text and style
TickLabel	Tick label style
Grid	Show or hide the grid Specified as one of the following strings: 'off' 'on' Default: 'off'
GridColor	Color of the grid lines Specified as one of the following: Vector of RGB values in the range [0,1] color string 'none'. Default: [0.15,0.15,0.15]
XlimMode, YlimMode	Limit modes
Xlim, Ylim	Axes limits
IOGrouping	Grouping of input-output pairs

Option	Description
	Specified as one of the following strings: 'none' 'inputs' 'outputs' 'all' Default: 'none'
InputLabels, OutputLabels	Input and output label styles
InputVisible, OutputVisible	Visibility of input and output channels

Option	Description
FreqUnits	Frequency units, specified as one of the following strings:
	• 'Hz'
	• 'rad/second'
	• 'rpm'
	• 'kHz'
	• 'MHz'
	• 'GHz'
	• 'rad/nanosecond'
	 'rad/microsecond'
	• 'rad/millisecond'
	• 'rad/minute'
	• 'rad/hour'
	• 'rad/day'
	• 'rad/week'
	• 'rad/month'
	• 'rad/year'
	• 'cycles/nanosecond'
	• 'cycles/microsecond'
	• 'cycles/millisecond'
	• 'cycles/hour'
	• 'cycles/day'
	• 'cycles/week'
	• 'cycles/month'
	• 'cycles/year'
	Default: 'rad/s'
	You can also specify 'auto' which uses frequency units rad/TimeUnit relative to system time units specified in the TimeUnit property. For

Option	Description
	multiple systems with different time units, the units of the first system are used.
MagUnits	Magnitude units Specified as one of the following strings: 'dB' 'abs' Default: 'dB'
PhaseUnits	Phase units Specified as one of the following strings: 'deg' 'rad' Default: 'deg'
ShowFullContour	Show response for negative frequencies Specified as one of the following strings: 'on' 'off' Default: 'on'
ConfidenceRegionNumbe	Number of standard deviations to use to plotting the response confidence region (identified models only). Default : 1.
ConfidenceRegionDisplay	The frequency spacing of confidence ellipses. For identified models only. Default: 5, which means the confidence ellipses are shown at every 5th frequency sample.

Examples

This example shows how to create a Nyquist plot displaying the full contour (the response for both positive and negative frequencies).

P = nyquistoptions; P.ShowFullContour = 'on'; h = nyquistplot(tf(1,[1,.2,1]),P);

See Also

nyquist | nyquistplot | getoptions | setoptions

Introduced in R2011a

nyquistplot

Nyquist plot with additional plot customization options

Syntax

```
h = nyquistplot(sys)
nyquistplot(sys,{wmin,wmax})
nyquistplot(sys,w)
nyquistplot(sys1,sys2,...,w)
nyquistplot(AX,...)
nyquistplot(..., plotoptions)
```

Description

h = nyquistplot(sys) draws the Nyquist plot of the dynamic system model sys. It also returns the plot handle h. You can use this handle to customize the plot with the getoptions and setoptions commands. Type

help nyquistoptions

for a list of available plot options.

The frequency range and number of points are chosen automatically. See **bode** for details on the notion of frequency in discrete time.

nyquistplot(sys, {wmin,wmax}) draws the Nyquist plot for frequencies between wmin and wmax (in rad/TimeUnit, where TimeUnit is the time units of the input dynamic system, specified in the TimeUnit property of sys).

nyquistplot(sys,w) uses the user-supplied vector w of frequencies (in rad/ TimeUnit, where TimeUnit is the time units of the input dynamic system, specified in the TimeUnit property of sys) at which the Nyquist response is to be evaluated. See logspace to generate logarithmically spaced frequency vectors.

nyquistplot(sys1,sys2,...,w) draws the Nyquist plots of multiple models sys1,sys2,... on a single plot. The frequency vector w is optional. You can also specify a color, line style, and marker for each system, as in

```
nyquistplot(sys1,'r',sys2,'y--',sys3,'gx')
```

nyquistplot(AX,...) plots into the axes with handle AX.

nyquistplot(..., plotoptions) plots the Nyquist response with the options
specified in plotoptions. Type

help nyquistoptions

for more details.

Examples

Example 1

Customize Nyquist Plot Frequency Units

Plot the Nyquist frequency response and change the units to rad/s.

```
sys = rss(5);
h = nyquistplot(sys);
% Change units to radians per second.
setoptions(h, 'FreqUnits', 'rad/s');
```

Example 2

Compare the frequency responses of identified state-space models of order 2 and 6 along with their 1-std confidence regions rendered at every 50th frequency sample.

```
load iddata1
sys1 = n4sid(z1, 2) % discrete-time IDSS model of order 2
sys2 = n4sid(z1, 6) % discrete-time IDSS model of order 6
```

Both models produce about 76% fit to data. However, **sys2** shows higher uncertainty in its frequency response, especially close to **Nyquist** frequency as shown by the plot:

```
w = linspace(10,10*pi,256);
h = nyquistplot(sys1,sys2,w);
setoptions(h,'ConfidenceRegionDisplaySpacing',50,'ShowFullContour','off');
```

Right-click to turn on the confidence region characteristic by using the **Characteristics-** > **Confidence Region**.

More About

Tips

You can change the properties of your plot, for example the units. For information on the ways to change properties of your plots, see "Ways to Customize Plots".

See Also

nyquist | setoptions | getoptions

Introduced before R2006a

obsv

Observability matrix

Syntax

obsv(A,C) Ob = obsv(sys)

Description

obsv computes the observability matrix for state-space systems. For an *n*-by-*n* matrix A and a *p*-by-*n* matrix C, obsv(A,C) returns the observability matrix

$$Ob = \begin{bmatrix} C \\ CA \\ CA^2 \\ \vdots \\ CA^{n-1} \end{bmatrix}$$

with n columns and np rows.

Ob = obsv(sys) calculates the observability matrix of the state-space model sys. This syntax is equivalent to executing

Ob = obsv(sys.A,sys.C)

The model is observable if Ob has full rank n.

Examples

Determine if the pair

```
4 -2

C =

1 0

0 1

is observable. Type

Ob = obsv(A,C);

% Number of unobservable states

unob = length(A)-rank(Ob)

These commands produce the following result.
```

unob = 0

More About

Tips

obsv is here for educational purposes and is not recommended for serious control design. Computing the rank of the observability matrix is not recommended for observability testing. **Ob** will be numerically singular for most systems with more than a handful of states. This fact is well documented in the control literature. For example, see section III in http://lawww.epfl.ch/webdav/site/la/users/105941/public/NumCompCtrl.pdf

See Also

obsvf

Introduced before R2006a

obsvf

Compute observability staircase form

Syntax

[Abar,Bbar,Cbar,T,k] = obsvf(A,B,C)
obsvf(A,B,C,tol)

Description

If the observability matrix of (A,C) has rank $r \le n$, where n is the size of A, then there exists a similarity transformation such that

 $\overline{A} = TAT^T, \quad \overline{B} = TB, \quad \overline{C} = CT^T$

where T is unitary and the transformed system has a *staircase* form with the unobservable modes, if any, in the upper left corner.

$$\bar{A} = \begin{bmatrix} A_{no} & A_{12} \\ 0 & A_o \end{bmatrix}, \ \bar{B} = \begin{bmatrix} B_{no} \\ B_o \end{bmatrix}, \ \bar{C} = \begin{bmatrix} 0 \ C_o \end{bmatrix}$$

where (C_o, A_o) is observable, and the eigenvalues of A_{no} are the unobservable modes.

[Abar, Bbar, Cbar, T, k] = obsvf(A, B, C) decomposes the state-space system with matrices A, B, and C into the observability staircase form Abar, Bbar, and Cbar, as described above. T is the similarity transformation matrix and k is a vector of length n, where n is the number of states in A. Each entry of k represents the number of observable states factored out during each step of the transformation matrix calculation [1]. The number of nonzero elements in k indicates how many iterations were necessary to calculate T, and sum(k) is the number of states in A_o , the observable portion of Abar.

obsvf(A,B,C,tol) uses the tolerance tol when calculating the observable/ unobservable subspaces. When the tolerance is not specified, it defaults to 10*n*norm(a,1)*eps.

Examples

Form the observability staircase form of

A = 1 1 4 -2 В = 1 - 1 - 1 1 C = 1 0 0 1 by typing [Abar,Bbar,Cbar,T,k] = obsvf(A,B,C) Abar = 1 1 4 -2 Bbar = 1 1 1 - 1 Cbar = 1 0 0 1 T = 1 0 0 1 k = 0 2

More About

Algorithms

obsvf implements the Staircase Algorithm of [1] by calling ctrbf and using duality.

References

[1] Rosenbrock, M.M., State-Space and Multivariable Theory, John Wiley, 1970.

See Also ctrbf | obsv

Introduced before R2006a

ord2

Generate continuous second-order systems

Syntax

[A,B,C,D] = ord2(wn,z)[num,den] = ord2(wn,z)

Description

[A,B,C,D] = ord2(wn,z) generates the state-space description (A,B,C,D) of the second-order system

 $h(s) = \frac{1}{s^2 + 2\zeta\omega_n s + \omega_n^2}$

given the natural frequency $Wn(\omega_n)$ and damping factor $z(\zeta)$. Use **ss** to turn this description into a state-space object.

[num,den] = ord2(wn,z) returns the numerator and denominator of the secondorder transfer function. Use tf to form the corresponding transfer function object.

Examples

To generate an LTI model of the second-order transfer function with damping factor $\zeta = 0.4$ and natural frequency $\omega_n = 2.4$ rad/sec., type

s^2 + 1.92 s + 5.76

See Also

rss | ss | tf

Introduced before R2006a

order

Query model order

Syntax

NS = order(sys)

Description

NS = order(sys) returns the model order NS. The order of a dynamic system model is the number of poles (for proper transfer functions) or the number of states (for statespace models). For improper transfer functions, the order is defined as the minimum number of states needed to build an equivalent state-space model (ignoring pole/zero cancellations).

order(sys) is an overloaded method that accepts SS, TF, and ZPK models. For LTI arrays, NS is an array of the same size listing the orders of each model in sys.

Caveat

order does not attempt to find minimal realizations of MIMO systems. For example, consider this 2-by-2 MIMO system:

```
s=tf('s');
h = [1, 1/(s*(s+1)); 1/(s+2), 1/(s*(s+1)*(s+2))];
order(h)
ans =
```

6

Although h has a 3rd order realization, order returns 6. Use

```
order(ss(h,'min'))
```

to find the minimal realization order.

See Also pole | balred

Introduced in R2012a

pade

Padé approximation of model with time delays

Syntax

```
[num,den] = pade(T,N)
pade(T,N)
sysx = pade(sys,N)
sysx = pade(sys,NU,NY,NINT)
```

Description

pade approximates time delays by rational models. Such approximations are useful to model time delay effects such as transport and computation delays within the context of continuous-time systems. The Laplace transform of a time delay of T seconds is $\exp(-sT)$. This exponential transfer function is approximated by a rational transfer function using Padé approximation formulas [1].

[num,den] = pade(T,N) returns the Padé approximation of order N of the continuous-time I/O delay exp(-sT) in transfer function form. The row vectors num and den contain the numerator and denominator coefficients in descending powers of s. Both are Nth-order polynomials.

When invoked without output arguments, pade(T,N) plots the step and phase responses of the Nth-order Padé approximation and compares them with the exact responses of the model with I/O delay T. Note that the Padé approximation has unit gain at all frequencies.

sysx = pade(sys,N) produces a delay-free approximation sysx of the continuous delay system sys. All delays are replaced by their Nth-order Padé approximation. See "Time Delays in Linear Systems" for more information about models with time delays.

sysx = pade(sys,NU,NY,NINT) specifies independent approximation orders for each input, output, and I/O or internal delay. Here NU, NY, and NINT are integer arrays such that

- $\ensuremath{\mathsf{NU}}$ is the vector of approximation orders for the input channel
- NY is the vector of approximation orders for the output channel
- NINT is the approximation order for I/O delays (TF or ZPK models) or internal delays (state-space models)

You can use scalar values for NU, NY, or NINT to specify a uniform approximation order. You can also set some entries of NU, NY, or NINT to Inf to prevent approximation of the corresponding delays.

Examples

Third-Order Padé Approximation

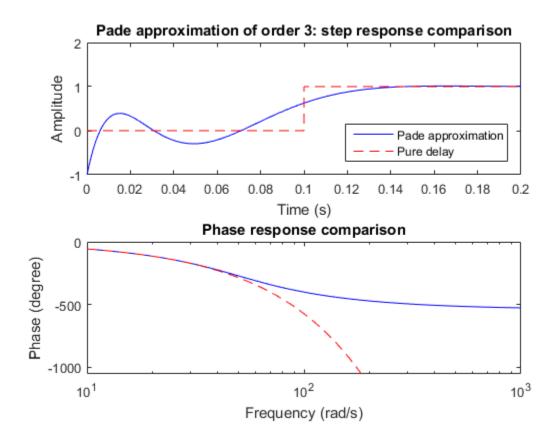
Compute a third-order Padé approximation of a 0.1-second I/O delay.

```
s = tf('s');
sys = exp(-0.1*s);
sysx = pade(sys,3)
sysx =
   -s^3 + 120 s^2 - 6000 s + 1.2e05
   s^3 + 120 s^2 + 6000 s + 1.2e05
Continuous-time transfer function.
```

Here, sys is a dynamic system representation of the exact time delay of 0.1 s. sysx is a transfer function that approximates that delay.

Compare the time and frequency responses of the true delay and its approximation. Calling the pade command without output arguments generates the comparison plots. In this case the first argument to pade is just the magnitude of the exact time delay, rather than a dynamic system representing the time delay.

pade(0.1,3)



Limitations

High-order Padé approximations produce transfer functions with clustered poles. Because such pole configurations tend to be very sensitive to perturbations, Padé approximations with order N>10 should be avoided.

More About

• "Time-Delay Approximation"

References

[1] Golub, G. H. and C. F. Van Loan, *Matrix Computations*, Johns Hopkins University Press, Baltimore, 1989, pp. 557-558.

See Also

c2d | absorbDelay | thiran

Introduced before R2006a

parallel

Parallel connection of two models

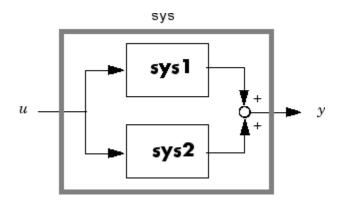
Syntax

```
parallel
sys = parallel(sys1,sys2)
sys = parallel(sys1,sys2,inp1,inp2,out1,out2)
sys = parallel(sys1,sys2,'name')
```

Description

parallel connects two model objects in parallel. This function accepts any type of model. The two systems must be either both continuous or both discrete with identical sample time. Static gains are neutral and can be specified as regular matrices.

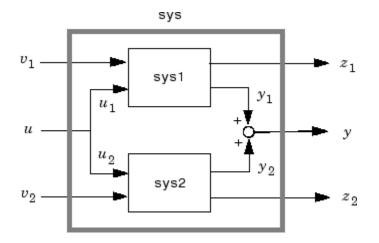
sys = parallel(sys1,sys2) forms the basic parallel connection shown in the
following figure.



This command equals the direct addition

sys = sys1 + sys2

sys = parallel(sys1,sys2,inp1,inp2,out1,out2) forms the more general
parallel connection shown in the following figure.



The vectors inp1 and inp2 contain indexes into the input channels of sys1 and sys2, respectively, and define the input channels u_1 and u_2 in the diagram. Similarly, the vectors out1 and out2 contain indexes into the outputs of these two systems and define the output channels y_1 and y_2 in the diagram. The resulting model sys has $[v_1; u; v_2]$ as inputs and $[z_1; y; z_2]$ as outputs.

sys = parallel(sys1,sys2, 'name') connects sys1 and sys2 by matching I/O
names. You must specify all I/O names of sys1 and sys2. The matching names appear in
sys in the same order as in sys1. For example, the following specification:

```
sys1 = ss(eye(3), 'InputName', {'C', 'B', 'A'}, 'OutputName', {'Z', 'Y', 'X'});
sys2 = ss(eye(3), 'InputName', {'A', 'C', 'B'}, 'OutputName', {'X', 'Y', 'Z'});
parallel(sys1,sys2,'name')
returns this result:
d =
           С
                 В
                       А
      Ζ
                       0
           1
                 1
      Υ
                       0
           1
                 1
      Х
           0
                 0
                     2
Static gain.
```

Note: If sys1 and sys2 are model arrays, parallel returns model array sys of the same size, where sys(:,:,k)=parallel(sys1(:,:,k),sys2(:,:,k),inp1,...).

Examples

See Kalman Filtering for an example.

See Also append | feedback | series

Introduced before R2006a

permute

Permute array dimensions in model arrays

Syntax

```
newarray = permute(sysarray,order)
```

Description

newarray = permute(sysarray,order) rearranges the array dimensions of a model array so that the dimensions are in the specified order. The input and output dimensions of the model array are not counted as array dimensions for this operation.

Examples

Permute Model Array Dimensions

Create a 1-by-2-by-3 array of state-space models and rearrange it so that its dimensions are 3-by-2-by-1.

```
sysarr = rss(2,2,2,1,2,3);
newarr = permute(sysarr,[3 2 1]);
size(newarr)
3x2 array of state-space models.
Each model has 2 outputs, 2 inputs, and 2 states.
```

The input and output dimensions of the model array remain unchanged.

Input Arguments

sysarray - Model array to rearrange model array

Model array to rearrange, specified as an array of input-output models such as numeric LTI models, generalized models, or identified LTI models.

order - Dimensions of rearranged model array

vector

Dimensions of rearranged model array, specified as a vector of positive integers. For example, to rearrange a model array into a 3-by-2 array, order is [3 2].

Data Types: double

Output Arguments

newarray — Rearranged model array

model array

Rearranged model array, returned as an array of input-output models with the new dimensions as specified in **order**.

See Also ndims | reshape | size

Introduced in R2013a

pid

Create PID controller in parallel form, convert to parallel-form PID controller

Syntax

C = pid(Kp,Ki,Kd,Tf) C = pid(Kp,Ki,Kd,Tf,Ts) C = pid(sys) C = pid(Kp) C = pid(Kp,Ki) C = pid(Kp,Ki,Kd) C = pid(...,Name,Value) C = pid

Description

C = pid(Kp,Ki,Kd,Tf) creates a continuous-time PID controller with proportional, integral, and derivative gains Kp, Ki, and Kd and first-order derivative filter time constant Tf:

$$C = K_p + \frac{K_i}{s} + \frac{K_d s}{T_f s + 1}.$$

This representation is in *parallel form*. If all of Kp, Ki, Kd, and Tf are real, then the resulting C is a pid controller object. If one or more of these coefficients is tunable (realp or genmat), then C is a tunable generalized state-space (genss) model object.

C = pid(Kp,Ki,Kd,Tf,Ts) creates a discrete-time PID controller with sample time Ts. The controller is:

$$C = K_p + K_i IF(z) + \frac{K_d}{T_f + DF(z)}.$$

IF(z) and DF(z) are the *discrete integrator formulas* for the integrator and derivative filter. By default,

$$IF\left(z\right)=DF\left(z\right)=\frac{T_{s}}{z-1}.$$

To choose different discrete integrator formulas, use the IFormula and DFormula properties. (See "Properties" on page 1-563 for more information about IFormula and DFormula). If DFormula = 'ForwardEuler' (the default value) and Tf \neq 0, then Ts and Tf must satisfy Tf > Ts/2. This requirement ensures a stable derivative filter pole.

C = pid(sys) converts the dynamic system sys to a parallel form pid controller object.

C = pid(Kp) creates a continuous-time proportional (P) controller with Ki = 0, Kd = 0, and Tf = 0.

C = pid(Kp,Ki) creates a proportional and integral (PI) controller with Kd = 0 and Tf = 0.

C = pid(Kp,Ki,Kd) creates a proportional, integral, and derivative (PID) controller with Tf = 0.

C = pid(...,Name,Value) creates a controller or converts a dynamic system to a pid controller object with additional options specified by one or more Name,Value pair arguments.

C = pid creates a P controller with Kp = 1.

Input Arguments

Кр

Proportional gain.

Kp can be:

- A real and finite value.
- An array of real and finite values.
- A tunable parameter (realp) or generalized matrix (genmat).
- A tunable surface for gain-scheduled tuning, created using tunableSurface (requires Robust Control Toolbox software).

When Kp = 0, the controller has no proportional action.

Default: 1

Ki

Integral gain.

Ki can be:

- A real and finite value.
- An array of real and finite values.
- A tunable parameter (realp) or generalized matrix (genmat).
- A tunable surface for gain-scheduled tuning, created using tunableSurface (requires Robust Control Toolbox software).

When Ki = 0, the controller has no integral action.

Default: 0

Kd

Derivative gain.

Kd can be:

- A real and finite value.
- An array of real and finite values.
- A tunable parameter (realp) or generalized matrix (genmat).
- A tunable surface for gain-scheduled tuning, created using tunableSurface (requires Robust Control Toolbox software).

When Kd = 0, the controller has no derivative action.

Default: 0

Τf

Time constant of the first-order derivative filter.

Tf can be:

• A real, finite, and nonnegative value.

- · An array of real, finite, and nonnegative values.
- A tunable parameter (realp) or generalized matrix (genmat).
- A tunable surface for gain-scheduled tuning, created using tunableSurface (requires Robust Control Toolbox software).

When Tf = 0, the controller has no filter on the derivative action.

Default: 0

Ts

Sample time.

To create a discrete-time pid controller, provide a positive real value (Ts > 0). pid does not support discrete-time controller with undetermined sample time (Ts = -1).

Ts must be a scalar value. In an array of pid controllers, each controller must have the same Ts.

Default: 0 (continuous time)

sys

SISO dynamic system to convert to parallel pid form.

sys must represent a valid PID controller that can be written in parallel form with $Tf \ge 0$.

sys can also be an array of SISO dynamic systems.

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside single quotes (' '). You can specify several name and value pair arguments in any order as Name1, Value1, ..., NameN, ValueN.

Use Name, Value syntax to set the numerical integration formulas IFormula and DFormula of a discrete-time pid controller, or to set other object properties such as InputName and OutputName. For information about available properties of pid controller objects, see "Properties" on page 1-563.

Output Arguments

C

PID controller, represented as a pid controller object, an array of pid controller objects, a genss object, or a genss array.

- If all the gains Kp, Ki, Kd, and Tf have numeric values, then C is a pid controller object. When the gains are numeric arrays, C is an array of pid controller objects. The controller type (P, I, PI, PD, PDF, PID, PIDF) depends upon the values of the gains. For example, when Kd = 0, but Kp and Ki are nonzero, C is a PI controller.
- If one or more gains is a tunable parameter (realp), generalized matrix (genmat), or tunable gain surface (tunableSurface), then C is a generalized state-space model (genss).

Properties

Kp, Ki, Kd

PID controller gains.

The Kp, Ki, and Kd properties store the proportional, integral, and derivative gains, respectively. Kp, Ki, and Kd are real and finite.

Τf

Derivative filter time constant.

The Tf property stores the derivative filter time constant of the pid controller object. Tf is real, finite, and nonnegative.

IFormula

Discrete integrator formula IF(z) for the integrator of the discrete-time pid controller C:

$$C = K_p + K_i IF(z) + \frac{K_d}{T_f + DF(z)}.$$

IFormula can take the following values:

$$\mathsf{'ForwardEuler'} - IF(z) = \frac{T_s}{z-1}.$$

This formula is best for small sample time, where the Nyquist limit is large compared to the bandwidth of the controller. For larger sample time, the ForwardEuler formula can result in instability, even when discretizing a system that is stable in continuous time.

'BackwardEuler' —
$$IF(z) = \frac{T_s z}{z-1}$$
.

An advantage of the BackwardEuler formula is that discretizing a stable continuoustime system using this formula always yields a stable discrete-time result.

$$Trapezoidal' - IF(z) = \frac{T_s}{2} \frac{z+1}{z-1}$$

An advantage of the Trapezoidal formula is that discretizing a stable continuoustime system using this formula always yields a stable discrete-time result. Of all available integration formulas, the Trapezoidal formula yields the closest match between frequency-domain properties of the discretized system and the corresponding continuous-time system.

When C is a continuous-time controller, IFormula is ''.

Default: 'ForwardEuler'

DFormula

Discrete integrator formula DF(z) for the derivative filter of the discrete-time pid controller C:

$$C = K_p + K_i IF(z) + \frac{K_d}{T_f + DF(z)}.$$

DFormula can take the following values:

'ForwardEuler' —
$$DF(z) = \frac{T_s}{z-1}$$

This formula is best for small sample time, where the Nyquist limit is large compared to the bandwidth of the controller. For larger sample time, the ForwardEuler formula can result in instability, even when discretizing a system that is stable in continuous time.

'BackwardEuler' —
$$DF(z) = \frac{T_s z}{z-1}$$
.

An advantage of the **BackwardEuler** formula is that discretizing a stable continuoustime system using this formula always yields a stable discrete-time result.

'Trapezoidal' —
$$DF(z) = \frac{T_s}{2} \frac{z+1}{z-1}$$
.

An advantage of the Trapezoidal formula is that discretizing a stable continuoustime system using this formula always yields a stable discrete-time result. Of all available integration formulas, the Trapezoidal formula yields the closest match between frequency-domain properties of the discretized system and the corresponding continuous-time system.

The Trapezoidal value for DFormula is not available for a pid controller with no derivative filter (Tf = 0).

When C is a continuous-time controller, DFormula is ''.

Default: 'ForwardEuler'

InputDelay

Time delay on the system input. InputDelay is always 0 for a pid controller object.

OutputDelay

Time delay on the system Output. OutputDelay is always 0 for a pid controller object.

Ts

Sample time. For continuous-time models, Ts = 0. For discrete-time models, Ts is a positive scalar representing the sampling period. This value is expressed in the unit specified by the TimeUnit property of the model. To denote a discrete-time model with unspecified sample time, set Ts = -1.

Changing this property does not discretize or resample the model. Use c2d and d2c to convert between continuous- and discrete-time representations. Use d2d to change the sample time of a discrete-time system.

Default: 0 (continuous time)

TimeUnit

String representing the unit of the time variable. This property specifies the units for the time variable, the sample time Ts, and any time delays in the model. Use any of the following values:

- 'nanoseconds'
- 'microseconds'
- 'milliseconds'
- 'seconds'
- 'minutes'
- 'hours'
- 'days'
- 'weeks'
- 'months'
- 'years'

Changing this property has no effect on other properties, and therefore changes the overall system behavior. Use chgTimeUnit to convert between time units without modifying system behavior.

Default: 'seconds'

InputName

Input channel names. Set InputName to a string for single-input model. For a multiinput model, set InputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign input names for multi-input models. For example, if **sys** is a two-input model, enter:

sys.InputName = 'controls';

The input names automatically expand to { 'controls(1) '; 'controls(2) '}.

You can use the shorthand notation u to refer to the InputName property. For example, sys.u is equivalent to sys.InputName.

Input channel names have several uses, including:

- · Identifying channels on model display and plots
- · Extracting subsystems of MIMO systems
- Specifying connection points when interconnecting models

Default: Empty string ' ' for all input channels

InputUnit

Input channel units. Use InputUnit to keep track of input signal units. For a singleinput model, set InputUnit to a string. For a multi-input model, set InputUnit to a cell array of strings. InputUnit has no effect on system behavior.

Default: Empty string ' ' for all input channels

InputGroup

Input channel groups. The InputGroup property lets you assign the input channels of MIMO systems into groups and refer to each group by name. Specify input groups as a structure. In this structure, field names are the group names, and field values are the input channels belonging to each group. For example:

sys.InputGroup.controls = [1 2]; sys.InputGroup.noise = [3 5];

creates input groups named controls and noise that include input channels 1, 2 and 3, 5, respectively. You can then extract the subsystem from the controls inputs to all outputs using:

```
sys(:,'controls')
```

Default: Struct with no fields

OutputName

Output channel names. Set OutputName to a string for single-output model. For a multioutput model, set OutputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign output names for multi-output models. For example, if **sys** is a two-output model, enter:

```
sys.OutputName = 'measurements';
```

```
The output names automatically expand to { 'measurements(1) '; 'measurements(2) ' }.
```

You can use the shorthand notation y to refer to the OutputName property. For example, sys.y is equivalent to sys.OutputName.

Output channel names have several uses, including:

- · Identifying channels on model display and plots
- Extracting subsystems of MIMO systems
- · Specifying connection points when interconnecting models

Default: Empty string ' ' for all output channels

OutputUnit

Output channel units. Use OutputUnit to keep track of output signal units. For a single-output model, set OutputUnit to a string. For a multi-output model, set OutputUnit to a cell array of strings. OutputUnit has no effect on system behavior.

Default: Empty string '' for all output channels

OutputGroup

Output channel groups. The OutputGroup property lets you assign the output channels of MIMO systems into groups and refer to each group by name. Specify output groups as a structure. In this structure, field names are the group names, and field values are the output channels belonging to each group. For example:

```
sys.OutputGroup.temperature = [1];
sys.InputGroup.measurement = [3 5];
```

creates output groups named temperature and measurement that include output channels 1, and 3, 5, respectively. You can then extract the subsystem from all inputs to the measurement outputs using:

```
sys('measurement',:)
```

Default: Struct with no fields

Name

System name. Set Name to a string to label the system.

Default: ' '

Notes

Any text that you want to associate with the system. Set **Notes** to a string or a cell array of strings.

Default: {}

UserData

Any type of data you want to associate with system. Set UserData to any MATLAB data type.

Default: []

SamplingGrid

Sampling grid for model arrays, specified as a data structure.

For model arrays that are derived by sampling one or more independent variables, this property tracks the variable values associated with each model in the array. This information appears when you display or plot the model array. Use this information to trace results back to the independent variables.

Set the field names of the data structure to the names of the sampling variables. Set the field values to the sampled variable values associated with each model in the array. All sampling variables should be numeric and scalar valued, and all arrays of sampled values should match the dimensions of the model array.

For example, suppose you create a 11-by-1 array of linear models, sysarr, by taking snapshots of a linear time-varying system at times t = 0:10. The following code stores the time samples with the linear models.

```
sysarr.SamplingGrid = struct('time',0:10)
```

Similarly, suppose you create a 6-by-9 model array, M, by independently sampling two variables, zeta and w. The following code attaches the (zeta,w) values to M.

```
[zeta,w] = ndgrid(<6 values of zeta>,<9 values of w>)
M.SamplingGrid = struct('zeta',zeta,'w',w)
```

When you display M, each entry in the array includes the corresponding ${\tt zeta}$ and w values.

For model arrays generated by linearizing a Simulink model at multiple parameter values or operating points, the software populates SamplingGrid automatically with the variable values that correspond to each entry in the array. For example, the Simulink Control Design commands linearize and slLinearizer populate SamplingGrid in this way.

Default: []

Examples

PDF Controller

Create a continuous-time controller with proportional and derivative gains and a filter on the derivative term. To do so, set the integral gain to zero. Set the other gains and the filter time constant to the desired values.

```
Kp = 1;
Ki = 0; % No integrator
Kd = 3;
Tf = 0.5;
C = pid(Kp,Ki,Kd,Tf)
C =
S
```

Kp + Kd * ----- Tf*s+1with Kp = 1, Kd = 3, Tf = 0.5 Continuous-time PDF controller in parallel form.

The display shows the controller type, formula, and parameter values, and verifies that the controller has no integrator term.

Discrete-Time PI Controller

Create a discrete-time PI controller with trapezoidal discretization formula.

To create a discrete-time PI controller, set the value of TS and the discretization formula using Name, Value syntax.

```
C1 = pid(5,2.4, 'Ts',0.1, 'IFormula', 'Trapezoidal') % Ts = 0.1s

C1 =

Kp + Ki * \frac{Ts^*(z+1)}{2^*(z-1)}

with Kp = 5, Ki = 2.4, Ts = 0.1

Sample time: 0.1 seconds

Discrete-time PI controller in parallel form.
```

Alternatively, you can create the same discrete-time controller by supplying Ts as the fifth input argument after all four PID parameters, Kp, Ki, Kd, and Tf. Since you only want a PI controller, set Kd and Tf to zero.

with Kp = 5, Ki = 2.4, Ts = 0.1

```
Sample time: 0.1 seconds
Discrete-time PI controller in parallel form.
```

The display shows that C1 and C2 are the same.

PID Controller with Named Input and Output

When you create a PID controller, set the dynamic system properties InputName and OutputName. This is useful, for example, when you interconnect the PID controller with other dynamic system models using the connect command.

The display does not show the input and output names for the PID controller, but you can examine the property values. For instance, verify the input name of the controller.

C.InputName

ans = 'e'

Array of PID Controllers

Create a 2-by-3 grid of PI controllers with proportional gain ranging from 1–2 across the array rows and integral gain ranging from 5–9 across columns.

To build the array of PID controllers, start with arrays representing the gains.

Kp = [1 1 1;2 2 2]; Ki = [5:2:9;5:2:9];

When you pass these arrays to the pid command, the command returns the array.

```
pi_array = pid(Kp,Ki,'Ts',0.1,'IFormula','BackwardEuler');
size(pi_array)
```

2x3 array of PID controller. Each PID has 1 output and 1 input.

Alternatively, use the stack command to build an array of PID controllers.

C = pid(1,5,0.1) % PID controller Cf = pid(1,5,0.1,0.5) % PID controller with filter pid_array = stack(2,C,Cf); % stack along 2nd array dimension C = $Kp + Ki * \frac{1}{\cdots} + Kd * s$ with Kp = 1, Ki = 5, Kd = 0.1 Continuous-time PID controller in parallel form. Cf = $Kp + Ki * \frac{1}{\cdots} + Kd * \frac{s}{\cdots} + \frac{s}{Tf*s+1}$ with Kp = 1, Ki = 5, Kd = 0.1, Tf = 0.5 Continuous-time PIDF controller in parallel form.

These commands return a 1-by-2 array of controllers.

size(pid_array)

1x2 array of PID controller. Each PID has 1 output and 1 input. All PID controllers in an array must have the same sample time, discrete integrator formulas, and dynamic system properties such as InputName and OutputName.

Convert PID Controller from Standard to Parallel Form

Convert a standard form pidstd controller to parallel form.

Standard PID form expresses the controller actions in terms of an overall proportional gain Kp, integral and derivative time constants Ti and Td, and filter divisor N. You can convert any standard-form controller to parallel form using the pid command. For example, consider the following standard-form controller.

Convert this controller to parallel form using pid.

C par = pid(C std)

```
C_par =

Kp + Ki * \frac{1}{\cdots} + Kd * \frac{s}{\cdots}

s = Tf*s+1

with Kp = 2, Ki = 0.667, Kd = 8, Tf = 0.08

Continuous-time PIDF controller in parallel form.
```

Convert Dynamic System to Parallel-Form PID Controller

Convert a continuous-time dynamic system that represents a PID controller to parallel pid form.

The following dynamic system, with an integrator and two zeros, is equivalent to a PID controller.

$$H(s) = \frac{3(s+1)(s+2)}{s}.$$

Create a zpk model of H. Then use the pid command to obtain H in terms of the PID gains Kp, Ki, and Kd.

```
H = zpk([-1,-2],0,3);
C = pid(H)
C =
Kp + Ki * \frac{1}{---} + Kd * s
with Kp = 9, Ki = 6, Kd = 3

Continuous-time PID controller in parallel form.
```

Convert Discrete-Time Dynamic System to Parallel-Form PID Controller

Convert a discrete-time dynamic system that represents a PID controller with derivative filter to parallel pid form.

Create a discrete-time zpk model that represents a PIDF controller (two zeros and two poles, including the integrator pole at z = 1).

sys = zpk([-0.5,-0.6],[1 -0.2],3,'Ts',0.1);

When you convert **sys** to PID form, the result depends on which discrete integrator formulas you specify for the conversion. For instance, use the default, **ForwardEuler**, for both the integrator and the derivative.

```
Cfe = pid(sys)

Cfe =

Kp + Ki * \frac{Ts}{z-1} + Kd * \frac{1}{Tf+Ts/(z-1)}

with Kp = 2.75, Ki = 60, Kd = 0.0208, Tf = 0.0833, Ts = 0.1

Sample time: 0.1 seconds

Discrete-time PIDF controller in parallel form.
```

Now convert using the Trapezoidal formula.

```
Ctrap = pid(sys, 'IFormula', 'Trapezoidal', 'DFormula', 'Trapezoidal')

Ctrap =

Kp + Ki * Ts*(z+1) 1

2*(z-1) 1

Tf+Ts/2*(z+1)/(z-1)
```

```
with Kp = -0.25, Ki = 60, Kd = 0.0208, Tf = 0.0333, Ts = 0.1
Sample time: 0.1 seconds
Discrete-time PIDF controller in parallel form.
```

The displays show the difference in resulting coefficient values and functional form.

For this particular dynamic system, you cannot write sys in parallel PID form using the BackwardEuler formula for the derivative filter. Doing so would result in Tf < 0, which is not permitted. In that case, pid returns an error.

Discretize a Continuous-Time PID Controller

Discretize a continuous-time PID controller and set integral and derivative filter formulas.

Create a continuous-time controller and discretize it using the zero-order-hold method of the c2d command.

```
Ccon = pid(1,2,3,4); % continuous-time PIDF controller

Cdis1 = c2d(Ccon,0.1,'zoh')

Cdis1 =

Kp + Ki * \frac{Ts}{2-1} + Kd * \frac{1}{Tf+Ts/(z-1)}

with Kp = 1, Ki = 2, Kd = 3.04, Tf = 4.05, Ts = 0.1

Sample time: 0.1 seconds

Discrete-time PIDF controller in parallel form.
```

The display shows that c2d computes new PID gains for the discrete-time controller.

The discrete integrator formulas of the discretized controller depend on the c2d discretization method, as described in "Tips". For the zoh method, both IFormula and DFormula are ForwardEuler.

```
Cdis1.IFormula
Cdis1.DFormula
ans =
ForwardEuler
ans =
ForwardEuler
```

If you want to use different formulas from the ones returned by **c2d**, then you can directly set the **Ts**, **IFormula**, and **DFormula** properties of the controller to the desired values.

```
Cdis2 = Ccon;
Cdis2.Ts = 0.1;
Cdis2.IFormula = 'BackwardEuler';
Cdis2.DFormula = 'BackwardEuler';
```

However, these commands do not compute new PID gains for the discretized controller. To see this, examine Cdis2 and compare the coefficients to Ccon and Cdis1.

Cdis2

```
Cdis2 =

Ts*z \qquad 1
Kp + Ki * ----- + Kd * ------
z-1 \qquad Tf+Ts*z/(z-1)
with Kp = 1, Ki = 2, Kd = 3, Tf = 4, Ts = 0.1
Sample time: 0.1 seconds

Discrete-time PIDF controller in parallel form.
```

- "Proportional-Integral-Derivative (PID) Controllers"
- "Discrete-Time Proportional-Integral-Derivative (PID) Controllers"

More About

Tips

- Use pid either to create a pid controller object from known PID gains and filter time constant, or to convert a dynamic system model to a pid object.
- To deisgn a PID controller for a particular plant, use pidtune or pidTuner. To create a tunable PID controller as a control design block, use ltiblock.pid.
- Create arrays of pid controller objects by:
 - Specifying array values for Kp,Ki,Kd, and Tf
 - · Specifying an array of dynamic systems sys to convert to pid controller objects
 - · Using stack to build arrays from individual controllers or smaller arrays

In an array of pid controllers, each controller must have the same sample time Ts and discrete integrator formulas IFormula and DFormula.

• To create or convert to a standard-form controller, use pidstd. Standard form expresses the controller actions in terms of an overall proportional gain K_p , integral and derivative times T_i and T_d , and filter divisor N:

$$C = K_p \left(1 + \frac{1}{T_i} \frac{1}{s} + \frac{T_d s}{\frac{T_d}{N} s + 1} \right).$$

- There are two ways to discretize a continuous-time pid controller:
 - Use the c2d command. c2d computes new parameter values for the discretized controller. The discrete integrator formulas of the discretized controller depend upon the c2d discretization method you use, as shown in the following table.

c2d Discretization Method	IFormula	DFormula
'zoh'	ForwardEuler	ForwardEuler
'foh'	Trapezoidal	Trapezoidal
'tustin'	Trapezoidal	Trapezoidal
'impulse'	ForwardEuler	ForwardEuler
'matched'	ForwardEuler	ForwardEuler

For more information about C2d discretization methods, See the C2d reference page. For more information about IFormula and DFormula, see "Properties" on page 1-563 .

- If you require different discrete integrator formulas, you can discretize the controller by directly setting Ts, IFormula, and DFormula to the desired values. (See "Discretize a Continuous-Time PID Controller" on page 1-576.) However, this method does not compute new gain and filter-constant values for the discretized controller. Therefore, this method might yield a poorer match between the continuous- and discrete-time pid controllers than using c2d.
- "What Are Model Objects?"

See Also

pidstd | pid2 | piddata | make2DOF | pidtune | pidTuner | ltiblock.pid |
genss | realp

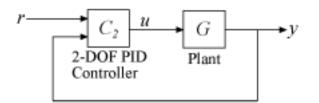
Introduced in R2010b

pid2

 $\label{eq:create 2-DOF PID controller in parallel form, convert to parallel-form 2-DOF PID controller$

pid2 controller objects represent two-degree-of-freedom (2-DOF) PID controllers in parallel form. Use pid2 either to create a pid2 controller object from known coefficients or to convert a dynamic system model to a pid2 object.

Two-degree-of-freedom (2-DOF) PID controllers include setpoint weighting on the proportional and derivative terms. A 2-DOF PID controller is capable of fast disturbance rejection without significant increase of overshoot in setpoint tracking. 2-DOF PID controllers are also useful to mitigate the influence of changes in the reference signal on the control signal. The following illustration shows atypical control architecture using a 2-DOF PID controller.



Syntax

```
C2 = pid2(Kp,Ki,Kd,Tf,b,c)
C2 = pid2(Kp,Ki,Kd,Tf,b,c,Ts)
C2 = pid2(sys)
C2 = pid2(____,Name,Value)
```

Description

C2 = pid2(Kp,Ki,Kd,Tf,b,c) creates a continuous-time 2-DOF PID controller with proportional, integral, and derivative gains Kp, Ki, and Kd and first-order derivative filter time constant Tf. The controller also has setpoint weighting b on the proportional

pid2

term, and setpoint weighting **c** on the derivative term. The relationship between the 2-DOF controller's output (u) and its two inputs (r and y) is given by:

$$u = K_p \left(br - y \right) + \frac{K_i}{s} \left(r - y \right) + \frac{K_d s}{T_f s + 1} \left(cr - y \right).$$

This representation is in *parallel form*. If all of the coefficients are real-valued, then the resulting C2 is a pid2 controller object. If one or more of these coefficients is tunable (realp or genmat), then C2 is a tunable generalized state-space (genss) model object.

C2 = pid2(Kp,Ki,Kd,Tf,b,c,Ts) creates a discrete-time 2-DOF PID controller with sample time Ts. The relationship between the controller's output and inputs is given by:

$$u = K_p (br - y) + K_i IF(z)(r - y) + \frac{K_d}{T_f + DF(z)} (cr - y).$$

IF(z) and DF(z) are the *discrete integrator formulas* for the integrator and derivative filter. By default,

$$IF(z) = DF(z) = \frac{T_s}{z-1}.$$

To choose different discrete integrator formulas, use the IFormula and DFormula properties. (See "Properties" on page 1-585 for more information). If DFormula = 'ForwardEuler' (the default value) and $Tf \neq 0$, then Ts and Tf must satisfy Tf > Ts/2. This requirement ensures a stable derivative filter pole.

C2 = pid2(sys) converts the dynamic system sys to a parallel form pid2 controller object.

C2 = pid2(_____, Name, Value) specifies additional properties as comma-separated pairs of Name, Value arguments.

Input Arguments

Кр

Proportional gain.

Kp can be:

- A real and finite value.
- An array of real and finite values.
- A tunable parameter (realp) or generalized matrix (genmat).
- A tunable surface for gain-scheduled tuning, created using tunableSurface (requires Robust Control Toolbox software).

When Kp = 0, the controller has no proportional action.

Default: 1

Ki

Integral gain.

Ki can be:

- A real and finite value.
- An array of real and finite values.
- A tunable parameter (realp) or generalized matrix (genmat).
- A tunable surface for gain-scheduled tuning, created using tunableSurface (requires Robust Control Toolbox software).

When Ki = 0, the controller has no integral action.

Default: 0

Kd

Derivative gain.

Kd can be:

- A real and finite value.
- An array of real and finite values.
- A tunable parameter (realp) or generalized matrix (genmat).
- A tunable surface for gain-scheduled tuning, created using tunableSurface (requires Robust Control Toolbox software).

When Kd = 0, the controller has no derivative action.

Default: 0

Τf

Time constant of the first-order derivative filter.

Tf can be:

- A real, finite, and nonnegative value.
- An array of real, finite, and nonnegative values.
- A tunable parameter (realp) or generalized matrix (genmat).
- A tunable surface for gain-scheduled tuning, created using tunableSurface (requires Robust Control Toolbox software).

When Tf = 0, the controller has no filter on the derivative action.

Default: 0

b

Setpoint weighting on proportional term.

b can be:

- A real, nonnegative, and finite value.
- An array of real, nonnegative, finite values.
- A tunable parameter (realp) or generalized matrix (genmat).
- A tunable surface for gain-scheduled tuning, created using tunableSurface (requires Robust Control Toolbox software).

When b = 0, changes in setpoint do not feed directly into the proportional term.

Default: 1

С

Setpoint weighting on derivative term.

c can be:

- A real, nonnegative, and finite value.
- An array of real, nonnegative, finite values.
- A tunable parameter (realp) or generalized matrix (genmat).
- A tunable surface for gain-scheduled tuning, created using tunableSurface (requires Robust Control Toolbox software).

When c = 0, changes in setpoint do not feed directly into the proportional term.

Default: 1

Ts

Sample time.

To create a discrete-time pid2 controller, provide a positive real value (Ts > 0). pid2 does not support discrete-time controller with undetermined sample time (Ts = -1).

 Ts must be a scalar value. In an array of pid2 controllers, each controller must have the same $\mathsf{Ts}.$

Default: 0 (continuous time)

sys

SISO dynamic system to convert to parallel pid2 form.

sys must be a two-input, one-output system. sys must represent a valid 2-DOF PID controller that can be written in parallel form with $Tf \ge 0$.

sys can also be an array of SISO dynamic systems.

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside single quotes (' '). You can specify several name and value pair arguments in any order as Name1, Value1, ..., NameN, ValueN.

Use Name, Value syntax to set the numerical integration formulas IFormula and DFormula of a discrete-time pid2 controller, or to set other object properties such as InputName and OutputName. For information about available properties of pid2 controller objects, see "Properties" on page 1-585.

Output Arguments

C2

2-DOF PID controller, returned as a pid2 controller object, an array of pid2 controller objects, a genss object, or a genss array.

- If all the coefficients have scalar numeric values, then C2 is a pid2 controller object.
- If one or more coefficients is a numeric array, C2 is an array of pid2 controller objects. The controller type (such as PI, PID, or PDF) depends upon the values of the gains. For example, when Kd = 0, but Kp and Ki are nonzero, C2 is a PI controller.
- If one or more coefficients is a tunable parameter (realp), generalized matrix (genmat), or tunable gain surface (tunableSurface), then C2 is a generalized state-space model (genss).

Properties

b, c

Setpoint weights on the proportional and derivative terms, respectively. **b** and **c** values are real, finite, and positive. When you create a 2-DOF PID controller using the pid2 command, the initial values of these properties are set by the **b**, and **c** input arguments, respectively.

Kp, Ki, Kd

PID controller gains.

Proportional, integral, and derivative gains, respectively. Kp, Ki, and Kd values are real and finite. When you create a 2-DOF PID controller using the pid2 command, the initial values of these properties are set by the Kp, Ki, and Kd input arguments, respectively.

Τf

Derivative filter time constant.

The Tf property stores the derivative filter time constant of the pid2 controller object. Tf is real, finite, and greater than or equal to zero. When you create a 2-DOF PID controller using the pid2 command, the initial value of this property is set by the Tf input argument.

IFormula

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Discrete integrator formula IF(z) for the integrator of the discrete-time pid2 controller C2. The relationship between the inputs and output of C2 is given by:

$$u = K_p (br - y) + K_i IF(z)(r - y) + \frac{K_d}{T_f + DF(z)} (cr - y).$$

IFormula can take the following values:

'ForwardEuler' —
$$IF(z) = \frac{T_s}{z-1}$$

This formula is best for small sample time, where the Nyquist limit is large compared to the bandwidth of the controller. For larger sample time, the ForwardEuler formula can result in instability, even when discretizing a system that is stable in continuous time.

'BackwardEuler' —
$$IF(z) = \frac{T_s z}{z-1}$$

An advantage of the **BackwardEuler** formula is that discretizing a stable continuoustime system using this formula always yields a stable discrete-time result.

$$Trapezoidal' - IF(z) = \frac{T_s}{2} \frac{z+1}{z-1}.$$

An advantage of the Trapezoidal formula is that discretizing a stable continuoustime system using this formula always yields a stable discrete-time result. Of all available integration formulas, the Trapezoidal formula yields the closest match between frequency-domain properties of the discretized system and the corresponding continuous-time system.

When C2 is a continuous-time controller, IFormula is ''.

Default: 'ForwardEuler'

DFormula

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Discrete integrator formula DF(z) for the derivative filter of the discrete-time pid2 controller C2. The relationship between the inputs and output of C2 is given by:

$$u = K_p (br - y) + K_i IF(z)(r - y) + \frac{K_d}{T_f + DF(z)} (cr - y).$$

DFormula can take the following values:

'ForwardEuler' —
$$DF(z) = \frac{T_s}{z-1}$$

This formula is best for small sample time, where the Nyquist limit is large compared to the bandwidth of the controller. For larger sample time, the ForwardEuler formula can result in instability, even when discretizing a system that is stable in continuous time.

'BackwardEuler' —
$$DF(z) = \frac{T_s z}{z-1}$$

An advantage of the BackwardEuler formula is that discretizing a stable continuoustime system using this formula always yields a stable discrete-time result.

'Trapezoidal' —
$$DF(z) = \frac{T_s}{2} \frac{z+1}{z-1}$$
.

An advantage of the Trapezoidal formula is that discretizing a stable continuoustime system using this formula always yields a stable discrete-time result. Of all available integration formulas, the Trapezoidal formula yields the closest match between frequency-domain properties of the discretized system and the corresponding continuous-time system. The Trapezoidal value for DFormula is not available for a pid2 controller with no derivative filter (Tf = 0).

When C2 is a continuous-time controller, DFormula is ''.

Default: 'ForwardEuler'

InputDelay

Time delay on the system input. InputDelay is always 0 for a pid2 controller object.

OutputDelay

Time delay on the system Output. OutputDelay is always 0 for a pid2 controller object.

Ts

Sample time. For continuous-time models, Ts = 0. For discrete-time models, Ts is a positive scalar representing the sampling period. This value is expressed in the unit specified by the TimeUnit property of the model. To denote a discrete-time model with unspecified sample time, set Ts = -1.

Changing this property does not discretize or resample the model. Use c2d and d2c to convert between continuous- and discrete-time representations. Use d2d to change the sample time of a discrete-time system.

Default: 0 (continuous time)

TimeUnit

String representing the unit of the time variable. This property specifies the units for the time variable, the sample time Ts, and any time delays in the model. Use any of the following values:

- 'nanoseconds'
- 'microseconds'
- 'milliseconds'
- 'seconds'
- 'minutes'

- 'hours'
- 'days'
- 'weeks'
- 'months'
- 'years'

Changing this property has no effect on other properties, and therefore changes the overall system behavior. Use chgTimeUnit to convert between time units without modifying system behavior.

Default: 'seconds'

InputName

Input channel names. Set InputName to a string for single-input model. For a multiinput model, set InputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign input names for multi-input models. For example, if **sys** is a two-input model, enter:

```
sys.InputName = 'controls';
```

The input names automatically expand to { 'controls(1) '; 'controls(2) '}.

You can use the shorthand notation u to refer to the InputName property. For example, sys.u is equivalent to sys.InputName.

Input channel names have several uses, including:

- · Identifying channels on model display and plots
- · Extracting subsystems of MIMO systems
- · Specifying connection points when interconnecting models

Default: Empty string ' ' for all input channels

InputUnit

Input channel units. Use InputUnit to keep track of input signal units. For a singleinput model, set InputUnit to a string. For a multi-input model, set InputUnit to a cell array of strings. InputUnit has no effect on system behavior. **Default:** Empty string ' ' for all input channels

InputGroup

Input channel groups. The InputGroup property lets you assign the input channels of MIMO systems into groups and refer to each group by name. Specify input groups as a structure. In this structure, field names are the group names, and field values are the input channels belonging to each group. For example:

```
sys.InputGroup.controls = [1 2];
sys.InputGroup.noise = [3 5];
```

creates input groups named controls and noise that include input channels 1, 2 and 3, 5, respectively. You can then extract the subsystem from the controls inputs to all outputs using:

sys(:,'controls')

Default: Struct with no fields

OutputName

Output channel names. Set OutputName to a string for single-output model. For a multioutput model, set OutputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign output names for multi-output models. For example, if **sys** is a two-output model, enter:

```
sys.OutputName = 'measurements';
```

The output names automatically expand to { 'measurements(1) '; 'measurements(2) ' }.

You can use the shorthand notation y to refer to the OutputName property. For example, sys.y is equivalent to sys.OutputName.

Output channel names have several uses, including:

- Identifying channels on model display and plots
- · Extracting subsystems of MIMO systems
- · Specifying connection points when interconnecting models

Default: Empty string ' ' for all output channels

OutputUnit

Output channel units. Use OutputUnit to keep track of output signal units. For a single-output model, set OutputUnit to a string. For a multi-output model, set OutputUnit to a cell array of strings. OutputUnit has no effect on system behavior.

Default: Empty string ' ' for all output channels

OutputGroup

Output channel groups. The OutputGroup property lets you assign the output channels of MIMO systems into groups and refer to each group by name. Specify output groups as a structure. In this structure, field names are the group names, and field values are the output channels belonging to each group. For example:

sys.OutputGroup.temperature = [1]; sys.InputGroup.measurement = [3 5];

creates output groups named temperature and measurement that include output channels 1, and 3, 5, respectively. You can then extract the subsystem from all inputs to the measurement outputs using:

sys('measurement',:)

Default: Struct with no fields

Name

System name. Set Name to a string to label the system.

Default: ' '

Notes

Any text that you want to associate with the system. Set **Notes** to a string or a cell array of strings.

Default: {}

UserData

Any type of data you want to associate with system. Set ${\tt UserData}$ to any MATLAB data type.

Default: []

SamplingGrid

Sampling grid for model arrays, specified as a data structure.

For model arrays that are derived by sampling one or more independent variables, this property tracks the variable values associated with each model in the array. This information appears when you display or plot the model array. Use this information to trace results back to the independent variables.

Set the field names of the data structure to the names of the sampling variables. Set the field values to the sampled variable values associated with each model in the array. All sampling variables should be numeric and scalar valued, and all arrays of sampled values should match the dimensions of the model array.

For example, suppose you create a 11-by-1 array of linear models, sysarr, by taking snapshots of a linear time-varying system at times t = 0:10. The following code stores the time samples with the linear models.

```
sysarr.SamplingGrid = struct('time',0:10)
```

Similarly, suppose you create a 6-by-9 model array, M, by independently sampling two variables, zeta and w. The following code attaches the (zeta,w) values to M.

```
[zeta,w] = ndgrid(<6 values of zeta>,<9 values of w>)
M.SamplingGrid = struct('zeta',zeta,'w',w)
```

When you display M, each entry in the array includes the corresponding zeta and w values.

М

```
25
s^2 + 3.5 s + 25
```

For model arrays generated by linearizing a Simulink model at multiple parameter values or operating points, the software populates SamplingGrid automatically with the variable values that correspond to each entry in the array. For example, the Simulink Control Design commands linearize and slLinearizer populate SamplingGrid in this way.

Default: []

Examples

2-DOF PDF Controller

Create a continuous-time 2-DOF controller with proportional and derivative gains and a filter on the derivative term. To do so, set the integral gain to zero. Set the other gains and the filter time constant to the desired values.

```
Kp = 1;
Ki = 0; % No integrator
Kd = 3;
Tf = 0.1;
b = 0.5; % setpoint weight on proportional term
c = 0.5; % setpoint weight on derivative term
C2 = pid2(Kp,Ki,Kd,Tf,b,c)
C2 =
u = Kp (b*r-y) + Kd = \frac{s}{-f^*s+1}
with Kp = 1, Kd = 3, Tf = 0.1, b = 0.5, c = 0.5
Continuous-time 2-DOF PDF controller in parallel form.
```

The display shows the controller type, formula, and parameter values, and verifies that the controller has no integrator term.

Discrete-Time 2-DOF PI Controller

Create a discrete-time 2-DOF PI controller using the trapezoidal discretization formula. Specify the formula using Name, Value syntax.

Setting Kd = 0 specifies a PI controller with no derivative term. As the display shows, the values of Tf and c are not used in this controller. The display also shows that the trapezoidal formula is used for the integrator.

2-DOF PID Controller with Named Inputs and Output

Create a 2-DOF PID controller, and set the dynamic system properties InputName and OutputName. Naming inputs and outpus is useful, for example, when you interconnect the PID controller with other dynamic system models using the connect command.

C2 = pid2(1,2,3,0,1,1,'InputName',{'r','y'},'OutputName','u')

```
C2 =

u = Kp (b*r-y) + Ki - -- (r-y) + Kd*s (c*r-y)
with Kp = 1, Ki = 2, Kd = 3, b = 1, c = 1

Continuous-time 2-DOF PID controller in parallel form.
```

A 2-DOF PID controller has two inputs and one output. Therefore, the 'InputName' property is an array of two strings, one for each input. The model display does not show the input and output names for the PID controller, but you can examine the property values to see them. For instance, verify the input name of the controller.

C2.InputName

```
ans =
'r'
'y'
```

Array of 2-DOF PID Controllers

Create a 2-by-3 grid of 2-DOF PI controllers with proportional gain ranging from 1-2 across the array rows and integral gain ranging from 5-9 across columns.

To build the array of PID controllers, start with arrays representing the gains.

Kp = [1 1 1;2 2 2]; Ki = [5:2:9;5:2:9];

When you pass these arrays to the pid2 command, the command returns the array of controllers.

```
pi_array = pid2(Kp,Ki,0,0,0.5,0,'Ts',0.1,'IFormula','BackwardEuler');
size(pi_array)
```

2x3 array of 2-DOF PID controller. Each PID has 1 output and 2 inputs. If you provide scalar values for some coefficients, pid2 automatically expands them and assigns the same value to all entries in the array. For instance, in this example, Kd = Tf = 0, so that all entries in the array are PI controllers. Also, all entries in the array have b = 0.5.

Access entries in the array using array indexing. For dynamic system arrays, the first two dimensions are the I/O dimensions of the model, and the remaining dimensions are the array dimensions. Therefore, the following command extracts the (2,3) entry in the array.

```
pi23 = pi\_array(:,:,2,3)
pi23 = Ts*z
u = Kp (b*r-y) + Ki ----- (r-y)
z-1
with Kp = 2, Ki = 9, b = 0.5, Ts = 0.1
Sample time: 0.1 seconds
Discrete-time 2-DOF PI controller in parallel form.
```

You can also build an array of PID controllers using the stack command.

C2 = pid2(1,5,0.1,0,0.5,0.5);	% PID controller
C2f = pid2(1,5,0.1,0.5,0.5,0.5);	<pre>% PID controller with filter</pre>
pid_array = stack(2,C2,C2f);	% stack along 2nd array dimension

These commands return a 1-by-2 array of controllers.

```
size(pid_array)
```

1x2 array of 2-DOF PID controller. Each PID has 1 output and 2 inputs.

All PID controllers in an array must have the same sample time, discrete integrator formulas, and dynamic system properties such as InputName and OutputName.

Convert 2-DOF PID Controller from Standard to Parallel Form

Convert a standard-form pidstd2 controller to parallel form.

pid2

Standard PID form expresses the controller actions in terms of an overall proportional gain Kp, integrator and derivative time constants Ti and Td, and filter divisor N. You can convert any 2-DOF standard-form controller to parallel form using the pid2 command. For example, consider the following standard-form controller.

Kp = 2; Ti = 3; Td = 4; N = 50; b = 0.1; c = 0.5; C2_std = pidstd2(Kp,Ti,Td,N,b,c)

 $C2_std =$

```
u = Kp * [(b*r-y) + ---- * --- * (r-y) + Td * ----- * (c*r-y)]
Ti s (Td/N)*s+1
```

with Kp = 2, Ti = 3, Td = 4, N = 50, b = 0.1, c = 0.5

Continuous-time 2-DOF PIDF controller in standard form

Convert this controller to parallel form using pid2.

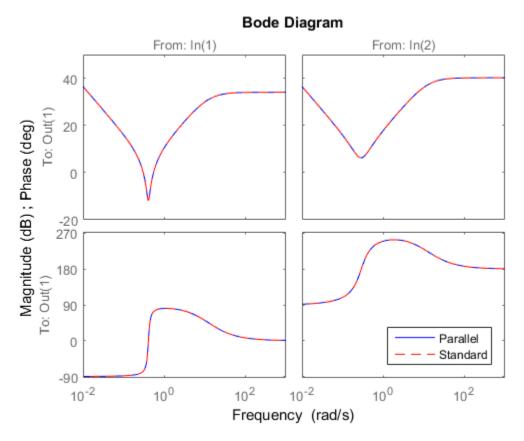
 $C2_par = pid2(C2_std)$

C2_par =

u = Kp (b*r-y) + Ki - (r-y) + Kd - (c*r-y)s Tf*s+1 with Kp = 2, Ki = 0.667, Kd = 8, Tf = 0.08, b = 0.1, c = 0.5 Continuous-time 2-DOF PIDF controller in parallel form.

A response plot confirms that the two forms are equivalent.

```
bodeplot(C2_par, 'b-',C2_std, 'r--')
legend('Parallel', 'Standard', 'Location', 'Southeast')
```



Convert Dynamic System to Parallel-Form PID Controller

Convert a continuous-time dynamic system that represents a PID controller to parallel pid form.

The following dynamic system, with an integrator and two zeros, is equivalent to a PID controller.

$$H(s) = \frac{3(s+1)(s+2)}{s}.$$

Create a zpk model of H. Then use the pid command to obtain H in terms of the PID gains Kp, Ki, and Kd.

Convert Dynamic System to 2-DOF Parallel-Form PID Controller

Convert a discrete-time dynamic system that represents a 2-DOF PID controller with derivative filter to parallel pid2 form.

The following state-space matrices represent a discrete-time 2-DOF PID controller with a sample time of 0.1 s.

```
A = [1,0;0,0.99];
B = [0.1,-0.1; -0.005,0.01];
C = [3,0.2];
D = [2.6,-5.2];
Ts = 0.1;
sys = ss(A,B,C,D,Ts);
```

When you convert **sys** to 2-DOF PID form, the result depends on which discrete integrator formulas you specify for the conversion. For instance, use the default, **ForwardEuler**, for both the integrator and the derivative.

```
C2fe = pid2(sys)

C2fe =

u = Kp (b*r-y) + Ki - \frac{Ts}{z-1} (r-y) + Kd - \frac{1}{Tf+Ts/(z-1)} (c*r-y)

with Kp = 5, Ki = 3, Kd = 2, Tf = 10, b = 0.5, c = 0.5, Ts = 0.1
```

```
Sample time: 0.1 seconds
Discrete-time 2-DOF PIDF controller in parallel form.
```

Now convert using the Trapezoidal formula.

C2trap = pid2(sys, 'IFormula', 'Trapezoidal', 'DFormula', 'Trapezoidal')

C2trap =

 $u = Kp (b*r-y) + Ki \frac{Ts*(z+1)}{2*(z-1)} (r-y) + Kd \frac{1}{Tf+Ts/2*(z+1)/(z-1)} (c*r-y) + Kd \frac{1}{Tf+Ts/2*(z+1)/(z-1)}$ with Kp = 4.85, Ki = 3, Kd = 2, Tf = 9.95, b = 0.485, c = 0.5, Ts = 0.1

Sample time: 0.1 seconds Discrete-time 2-DOF PIDF controller in parallel form.

The displays show the difference in resulting coefficient values and functional form.

Discretize a Continuous-Time 2-DOF PID Controller

Discretize a continuous-time 2-DOF PID controller and specify the integral and derivative filter formulas.

Create a continuous-time controller and discretize it using the zero-order-hold method of the C2d command.

```
C2con = pid2(10,5,3,0.5,1,1); % continuous-time 2-DOF PIDF controller
C2dis1 = c2d(C2con,0.1,'zoh')
```

C2dis1 = u = Kp (b*r-y) + Ki - (r-y) + Kd - (c*r-y) + (c*r-y) + Kd - (c*r-y) + The display shows that **c2d** computes new PID coefficients for the discrete-time controller.

The discrete integrator formulas of the discretized controller depend on the c2d discretization method, as described in "Tips". For the zoh method, both IFormula and DFormula are ForwardEuler.

C2dis1.IFormula C2dis1.DFormula ans = ForwardEuler ans = ForwardEuler

If you want to use different formulas from the ones returned by c2d, then you can directly set the Ts, IFormula, and DFormula properties of the controller to the desired values.

```
C2dis2 = C2con;
C2dis2.Ts = 0.1;
C2dis2.IFormula = 'BackwardEuler';
C2dis2.DFormula = 'BackwardEuler';
```

However, these commands do not compute new PID gains for the discretized controller. To see this, examine C2dis2 and compare the coefficients to C2con and C2dis1.

```
C2dis2
```

C2dis2 = u = Kp (b*r-y) + Ki - (r-y) + Kd - (c*r-y) z-1 Tf+Ts*z/(z-1) with Kp = 10, Ki = 5, Kd = 3, Tf = 0.5, b = 1, c = 1, Ts = 0.1

```
Sample time: 0.1 seconds
Discrete-time 2-DOF PIDF controller in parallel form.
```

- "Two-Degree-of-Freedom PID Controllers"
- "Discrete-Time Proportional-Integral-Derivative (PID) Controllers"

More About

Tips

- To design a PID controller for a particular plant, use pidtune or pidTuner. To create a tunable 2-DOF PID controller as a control design block, use ltiblock.pid2.
- To break a 2-DOF controller into two SISO control components, such as a feedback controller and a feedforward controller, use getComponents.
- Create arrays of pid2 controller objects by:
 - Specifying array values for one or more of the coefficients Kp, Ki, Kd, Tf, b, and c.
 - Specifying an array of dynamic systems sys to convert to pid2 controller objects.
 - Using stack to build arrays from individual controllers or smaller arrays.
 - Passing an array of plant models to pidtune.

In an array of pid2 controllers, each controller must have the same sample time Ts and discrete integrator formulas IFormula and DFormula.

To create or convert to a standard-form controller, use pidstd2. Standard form expresses the controller actions in terms of an overall proportional gain K_p , integral and derivative times T_i and T_d , and filter divisor N. For example, the relationship between the inputs and output of a continuous-time standard-form 2-DOF PID controller is given by:

$$u = K_p \left[(br - y) + \frac{1}{T_i s} (r - y) + \frac{T_d s}{\frac{T_d}{N} s + 1} (cr - y) \right].$$

• There are two ways to discretize a continuous-time pid2 controller:

• Use the c2d command. c2d computes new parameter values for the discretized controller. The discrete integrator formulas of the discretized controller depend upon the c2d discretization method you use, as shown in the following table.

c2d Discretization Method	IFormula	DFormula
'zoh'	ForwardEuler	ForwardEuler
'foh'	Trapezoidal	Trapezoidal
'tustin'	Trapezoidal	Trapezoidal
'impulse'	ForwardEuler	ForwardEuler
'matched'	ForwardEuler	ForwardEuler

For more information about C2d discretization methods, See the C2d reference page. For more information about <code>IFormula</code> and <code>DFormula</code>, see "Properties" on page 1-585 .

- If you require different discrete integrator formulas, you can discretize the controller by directly setting Ts, IFormula, and DFormula to the desired values. (See "Discretize a Continuous-Time 2-DOF PID Controller" on page 1-600.) However, this method does not compute new gain and filter-constant values for the discretized controller. Therefore, this method might yield a poorer match between the continuous- and discrete-time pid2 controllers than using c2d.
- "What Are Model Objects?"

See Also

pidstd2 | pid | piddata2 | getComponents | make1DOF | pidtune | pidTuner | ltiblock.pid2 | genss | realp

Introduced in R2015b

piddata

Access coefficients of parallel-form PID controller

Syntax

```
[Kp,Ki,Kd,Tf] = piddata(sys)
[Kp,Ki,Kd,Tf,Ts] = piddata(sys)
[Kp,Ki,Kd,Tf,Ts] = piddata(sys,J1,...,JN)
```

Description

[Kp,Ki,Kd,Tf] = piddata(sys) returns the PID gains Kp,Ki, Kd and the filter time constant Tf of the parallel-form controller represented by the dynamic system sys.

[Kp,Ki,Kd,Tf,Ts] = piddata(sys) also returns the sample time Ts.

[Kp,Ki,Kd,Tf,Ts] = piddata(sys,J1,...,JN) extracts the data for a subset of entries in sys, where sys is an N-dimensional array of dynamic systems. The indices J specify the array entry to extract.

Input Arguments

sys

SISO dynamic system or array of SISO dynamic systems. If **sys** is not a **pid** object, it must represent a valid PID controller that can be written in parallel PID form.

```
J
```

Integer indices of N entries in the array sys of dynamic systems. For example, suppose sys is a 4-by-5 (two-dimensional) array of pid controllers or dynamic system models that represent PID controllers. The following command extracts the data for entry (2,3) in the array.

[Kp,Ki,Kd,Tf,Ts] = piddata(sys,2,3);

Output Arguments

Кр

Proportional gain of the parallel-form PID controller represented by dynamic system ${\tt sys}.$

If sys is a pid controller object, the output Kp is equal to the Kp value of sys.

If sys is not a pid object, Kp is the proportional gain of a parallel PID controller equivalent to sys.

If sys is an array of dynamic systems, Kp is an array of the same dimensions as sys.

Ki

Integral gain of the parallel-form PID controller represented by dynamic system sys.

If sys is a pid controller object, then the output Ki is equal to the Ki value of sys.

If **sys** is not a **pid** object, then **Ki** is the integral gain of a parallel PID controller equivalent to **sys**.

If ${\tt sys}$ is an array of dynamic systems, then ${\tt Ki}$ is an array of the same dimensions as ${\tt sys}.$

Kd

Derivative gain of the parallel-form PID controller represented by dynamic system sys.

If sys is a pid controller object, then the output Kd is equal to the Kd value of sys.

If sys is not a pid object, then Kd is the derivative gain of a parallel PID controller equivalent to sys.

If ${\tt sys}$ is an array of dynamic systems, then ${\tt Kd}$ is an array of the same dimensions as ${\tt sys}.$

Τf

Filter time constant of the parallel-form PID controller represented by dynamic system ${\tt sys.}$

If sys is a pid controller object, the output Tf is equal to the Tf value of sys.

If **sys** is not a **pid** object, **Tf** is the filter time constant of a parallel PID controller equivalent to **sys**.

If sys is an array of dynamic systems, Tf is an array of the same dimensions as sys.

Ts

Sample time of the dynamic system **sys**. **Ts** is always a scalar value.

Examples

Extract the proportional, integral, and derivative gains and the filter time constant from a parallel-form pid controller.

For the following pid object:

sys = pid(1, 4, 0.3, 10);

you can extract the parameter values from sys by entering:

[Kp Ki Kd Tf] = piddata(sys);

Extract the parallel form proportional and integral gains from an equivalent standard-form PI controller.

For a standard-form PI controller, such as:

sys = pidstd(2,3);

you can extract the gains of an equivalent parallel-form PI controller by entering:

[Kp Ki] = piddata(sys)

These commands return the result:

Ki =

0.6667

Extract parameters from a dynamic system that represents a PID controller.

The dynamic system

$$H(z) = \frac{(z-0.5)(z-0.6)}{(z-1)(z+0.8)}$$

represents a discrete-time PID controller with a derivative filter. Use piddata to extract the parallel-form PID parameters.

H = zpk([0.5 0.6],[1,-0.8],1,0.1); % sample time Ts = 0.1s [Kp Ki Kd Tf Ts] = piddata(H);

the piddata function uses the default ForwardEuler discrete integrator formula for IFormula and DFormula to compute the parameter values.

Extract the gains from an array of PI controllers.

```
sys = pid(rand(2,3),rand(2,3)); % 2-by-3 array of PI controllers
[Kp Ki Kd Tf] = piddata(sys);
```

The parameters Kp, Ki, Kd, and Tf are also 2-by-3 arrays.

Use the index input J to extract the parameters of a subset of sys.

[Kp Ki Kd Tf] = piddata(sys,5);

More About

Tips

If sys is not a pid controller object, piddata returns the PID gains Kp, Ki, Kd and the filter time constant Tf of a parallel-form controller equivalent to sys.

For discrete-time sys, piddata returns the parameters of an equivalent parallel-form controller. This controller has discrete integrator formulas IFormula and DFormula set to ForwardEuler. See the pid reference page for more information about discrete integrator formulas.

See Also pid | pidstd | get

Introduced in R2010b

piddata2

Access coefficients of parallel-form 2-DOF PID controller

Syntax

```
[Kp,Ki,Kd,Tf,b,c] = piddata2(sys)
[Kp,Ki,Kd,Tf,b,c,Ts] = piddata2(sys)
[Kp,Ki,Kd,Tf,b,c,Ts] = piddata2(sys,J1,...,JN)
```

Description

[Kp,Ki,Kd,Tf,b,c] = piddata2(sys) returns the PID gains Kp,Ki, Kd, the filter time constant Tf, and the setpoint weights b and c of the parallel-form 2-DOF PID controller represented by the dynamic system sys.

If sys is a pid2 controller object, then each output argument is the corresponding coefficient in sys.

If **sys** is not a **pid2** object, then each output argument is the corresponding coefficient of the parallel-form 2-DOF PID controller that is equivalent to **sys**.

If **sys** is an array of dynamic systems, then each output argument is an array of the same dimensions as **sys**.

[Kp,Ki,Kd,Tf,b,c,Ts] = piddata2(sys) also returns the sample time Ts. For discrete-time sys that is not a pid2 object, piddata2 calculates the coefficient values using the default ForwardEuler discrete integrator formula for both IFormula and DFormula. See the pid2 reference page for more information about discrete integrator formulas.

[Kp,Ki,Kd,Tf,b,c,Ts] = piddata2(sys,J1,...,JN) extracts the data for a subset of entries in sys, where sys is an N-dimensional array of dynamic systems. The indices J specify the array entry to extract.

Examples

Extract Coefficients from Parallel-Form 2-DOF PID Controller

Typically, you extract coefficients from a controller obtained from another function, such as pidtune or getBlockValue. For this example, create a 2-DOF PID controller that has random coefficients.

rng('default'); % for reproducibility C2 = pid2(rand,rand,rand,rand,rand,rand);

Extract the PID coefficients, filter time constant, and setpoint weights.

[Kp,Ki,Kd,Tf,b,c] = piddata2(C2);

Extract Parallel-Form Gains from Standard-Form Controller

Create a 2-DOF PID controller in standard form.

```
C2 = pidstd2(2,3,4,10,0.5,0.5)
```

C2 =

 $u = Kp * [(b*r-y) + \frac{1}{1} + \frac{1}$

Compute the coefficients of an equivalent parallel-form PID controller.

[Kp,Ki,Kd,Tf,b,c] = piddata2(C2);

Check some of the cofficients to confirm that they are different from the standard-form coefficients.

Ki

Ki =

```
0.6667
Kd
Kd =
8
```

Extract 2-DOF PID Coefficients from Equivalent System

Extract coefficients from a two-input, one-output dynamic system that represents a valid 2-DOF parallel-form PID controller.

The following A, B, C, and D matrices form a discrete-time state-space model that represents a 2-DOF PID controller.

```
A = [1,0;0.09975,0.995];
B = [0.00625, -0.00625; 0.1245, -0.1241];
C = [0,4];
D = [2.875, -5.75];
sys = ss(A,B,C,D,0.1)
sys =
  a =
             x1
                      x2
                       0
   х1
              1
       0.09975
                   0.995
   х2
  b =
                         u2
              u1
        0.00625
                  -0.00625
   х1
                   -0.1241
   х2
         0.1245
  с =
       x1 x2
             4
        0
   у1
  d =
          u1
                  u2
   y1 2.875 -5.75
```

```
Sample time: 0.1 seconds
Discrete-time state-space model.
```

Extract the PID gains, filter time constant, and setpoint weights of the model.

[Kp,Ki,Kd,Tf,b,c,Ts] = piddata2(sys);

For a discrete-time system, piddata2 calculates the coefficient values using the default ForwardEuler discrete integrator formula for both IFormula and DFormula.

Extract Coefficients from 2-DOF PI Controller Array

Typically, you obtain an array of controllers by using pidtune on an array of plant models. For this example, create an 2-by-3 array of 2-DOF PI controllers with random values of Kp, Ki, and b.

```
rng('default');
C2 = pid2(rand(2,3),rand(2,3),0,0,rand(2,3),0);
```

Extract all the coefficients from the array.

[Kp,Ki,Kd,Tf,b,c] = piddata2(C2);

Each of the outputs is itself a 2-by-3 array. For example, examine Ki.

Κi

Ki =

0.2785	0.9575	0.1576
0.5469	0.9649	0.9706

Extract only the coefficients of entry (2,1) in the array.

[Kp21,Ki21,Kd21,Tf21,b21,c21] = piddata2(C2,2,1);

Each of these outputs is a scalar.

Ki21

Ki21 =

0.5469

Input Arguments

sys - 2-DOF PID controller

pid2 controller object | dynamic system model | dynamic system array

2-DOF PID controller in parallel form, specified as a pid2 controller object, a dynamic system model, or a dynamic system array. If sys is not a pid2 controller object, it must be a two-input, one-output model that represents a valid 2-DOF PID controller that can be written in parallel form.

J – Indices positive integers

Indices of entry to extract from a model array **sys**, specified as positive integers. Provide as many indices as there are array dimensions in **sys**. For example, suppose **sys** is a 4-by-5 (two-dimensional) array of **pid2** controllers or dynamic system models that represent 2-DOF PID controllers. The following command extracts the data for entry (2,3) in the array.

[Kp,Ki,Kd,Tf,b,c,Ts] = piddata2(sys,2,3);

Output Arguments

Kp — Proportional gain

scalar | array

Proportional gain of the parallel-form 2-DOF PID controller represented by **sys**, returned as a scalar or array.

If sys is a pid2 controller object, then Kp is the Kp value of sys.

If **sys** is not a **pid2** object, then **Kp** is the proportional gain of the parallel-form 2-DOF PID controller that is equivalent to **sys**.

If ${\tt sys}$ is an array of dynamic systems, then ${\tt Kp}$ is an array of the same dimensions as ${\tt sys}.$

Ki — Integral gain

scalar | array

Integral gain of the parallel-form 2-DOF PID controller represented by **sys**, returned as a scalar or array.

Kd - Derivative gain

scalar | array

Derivative gain of the parallel-form 2-DOF PID controller represented by **sys**, returned as a scalar or array.

Tf — Filter time constant

scalar | array

Filter time constant of the parallel-form 2-DOF PID controller represented by **sys**, returned as a scalar or array.

b - Setpoint weight on proportional term

scalar | array

Setpoint weight on the proportional term of the parallel-form 2-DOF PID controller represented by **sys**, returned as a scalar or array.

c - Setpoint weight on derivative term

scalar | array

Setpoint weight on the derivative term of the parallel-form 2-DOF PID controller represented by **sys**, returned as a scalar or array.

Ts — Sample time

scalar

Sample time of the pid2 controller, dynamic system sys, or dynamic system array, returned as a scalar.

See Also

pid2 | piddata | pidstddata2

Introduced in R2015b

pidstd

Create a PID controller in standard form, convert to standard-form PID controller

Syntax

```
C = pidstd(Kp,Ti,Td,N)
C = pidstd(Kp,Ti,Td,N,Ts)
C = pidstd(sys)
C = pidstd(Kp)
C = pidstd(Kp,Ti)
C = pidstd(Kp,Ti,Td)
C = pidstd(...,Name,Value)
C = pidstd
```

Description

C = pidstd(Kp,Ti,Td,N) creates a continuous-time PIDF (PID with first-order derivative filter) controller object in standard form. The controller has proportional gain Kp, integral and derivative times Ti and Td, and first-order derivative filter divisor N:

$$C = K_p \left(1 + \frac{1}{T_i} \frac{1}{s} + \frac{T_d s}{\frac{T_d}{N} s + 1} \right).$$

C = pidstd(Kp,Ti,Td,N,Ts) creates a discrete-time controller with sample time Ts. The discrete-time controller is:

$$C = K_p \left(1 + \frac{1}{T_i} IF(z) + \frac{T_d}{\frac{T_d}{N} + DF(z)} \right)$$

IF(z) and DF(z) are the *discrete integrator formulas* for the integrator and derivative filter. By default,

$$I\!F\left(z\right)=DF\left(z\right)=\frac{T_{s}}{z-1}.$$

To choose different discrete integrator formulas, use the IFormula and DFormula inputs. (See "Properties" on page 1-618 for more information about IFormula and DFormula). If DFormula = 'ForwardEuler' (the default value) and N \neq Inf, then Ts, Td, and N must satisfy Td/N > Ts/2. This requirement ensures a stable derivative filter pole.

C = pidstd(sys) converts the dynamic system sys to a standard form pidstd controller object.

C = pidstd(Kp) creates a continuous-time proportional (P) controller with Ti = Inf, Td = 0, and N = Inf.

 ${\tt C}={\tt pidstd(Kp,Ti)}$ creates a proportional and integral (PI) controller with ${\tt Td}=0$ and ${\tt N}={\tt Inf}.$

C = pidstd(Kp,Ti,Td) creates a proportional, integral, and derivative (PID) controller with N = Inf.

C = pidstd(...,Name,Value) creates a controller or converts a dynamic system to a pidstd controller object with additional options specified by one or more Name,Value pair arguments.

C = pidstd creates a P controller with Kp = 1.

Input Arguments

Кр

Proportional gain.

Kp must be a real and finite value.

For an array of pidstd controllers, Kp must be an array of real and finite values.

Default: 1

Τi

Integral time.

Ti must be a real and positive value. When Ti = Inf, the controller has no integral action.

For an array of pidstd controllers, Ti must be an array of real and positive values.

Default: Inf

Td

Derivative time.

Td must be a real, finite, and nonnegative value. When Td = 0, the controller has no derivative action.

For an array of ${\tt pidstd}$ controllers, ${\tt Td}$ must be an array of real, finite, and nonnegative values.

Default: 0

N

Derivative filter divisor.

N must be a real and positive value. When N = Inf, the controller has no derivative filter.

For an array of pidstd controllers, N must be an array of real and positive values.

Default: Inf

Ts

Sample time.

To create a discrete-time pidstd controller, provide a positive real value (Ts > 0).pidstd does not support discrete-time controller with undetermined sample time (Ts = -1).

 Ts must be a scalar value. In an array of pidstd controllers, each controller must have the same $\mathsf{Ts}.$

Default: 0 (continuous time)

sys

SISO dynamic system to convert to standard pidstd form.

sys must represent a valid controller that can be written in standard form with Ti > 0, $Td \ge 0$, and N > 0.

sys can also be an array of SISO dynamic systems.

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside single quotes (' '). You can specify several name and value pair arguments in any order as Name1, Value1, ..., NameN, ValueN.

Use Name, Value syntax to set the numerical integration formulas IFormula and DFormula of a discrete-time pidstd controller, or to set other object properties such as InputName and OutputName. For information about available properties of pidstd controller objects, see "Properties" on page 1-618.

Output Arguments

C

pidstd object representing a single-input, single-output PID controller in standard form.

The controller type (P, PI, PD, PDF, PID, PIDF) depends upon the values of Kp, Ti, Td, and N. For example, when Td = Inf and Kp and Ti are finite and nonzero, C is a PI controller. Enter getType(C) to obtain the controller type.

When the inputs Kp,Ti, Td, and N or the input ${\tt sys}$ are arrays, C is an array of <code>pidstd</code> objects.

Properties

Кр

Proportional gain. Kp must be real and finite.

Τi

Integral time. Ti must be real, finite, and greater than or equal to zero.

Τd

Derivative time. Td must be real, finite, and greater than or equal to zero.

N

•

Derivative filter divisor. N must be real, and greater than or equal to zero.

IFormula

Discrete integrator formula IF(z) for the integrator of the discrete-time pidstd controller C:

$$C = K_p \left(1 + \frac{1}{T_i} IF(z) + \frac{T_d}{\frac{T_d}{N} + DF(z)} \right)$$

IFormula can take the following values:

ForwardEuler' —
$$IF(z) = \frac{T_s}{z-1}$$
.

This formula is best for small sample time, where the Nyquist limit is large compared to the bandwidth of the controller. For larger sample time, the ForwardEuler formula can result in instability, even when discretizing a system that is stable in continuous time.

'BackwardEuler' —
$$IF(z) = \frac{T_s z}{z-1}$$

An advantage of the **BackwardEuler** formula is that discretizing a stable continuoustime system using this formula always yields a stable discrete-time result.

$$\label{eq:trapezoidal} {}^{\prime}-IF(z)=\frac{T_s}{2}\frac{z+1}{z-1}.$$

An advantage of the Trapezoidal formula is that discretizing a stable continuoustime system using this formula always yields a stable discrete-time result. Of all available integration formulas, the Trapezoidal formula yields the closest match between frequency-domain properties of the discretized system and the corresponding continuous-time system.

When C is a continuous-time controller, IFormula is ''.

Default: 'ForwardEuler'

DFormula

٠

Discrete integrator formula DF(z) for the derivative filter of the discrete-time pidstd controller C:

$$C = K_p \left(1 + \frac{1}{T_i} IF(z) + \frac{T_d}{\frac{T_d}{N} + DF(z)} \right).$$

DFormula can take the following values:

'ForwardEuler' —
$$DF(z) = \frac{T_s}{z-1}$$

This formula is best for small sample time, where the Nyquist limit is large compared to the bandwidth of the controller. For larger sample time, the ForwardEuler formula can result in instability, even when discretizing a system that is stable in continuous time.

'BackwardEuler' —
$$DF(z) = \frac{T_s z}{z-1}$$

An advantage of the BackwardEuler formula is that discretizing a stable continuoustime system using this formula always yields a stable discrete-time result.

'Trapezoidal' —
$$DF(z) = \frac{T_s}{2} \frac{z+1}{z-1}$$

An advantage of the Trapezoidal formula is that discretizing a stable continuoustime system using this formula always yields a stable discrete-time result. Of all available integration formulas, the Trapezoidal formula yields the closest match between frequency-domain properties of the discretized system and the corresponding continuous-time system. The Trapezoidal value for DFormula is not available for a pidstd controller with no derivative filter (N = Inf).

When C is a continuous-time controller, DFormula is ''.

Default: 'ForwardEuler'

InputDelay

Time delay on the system input. InputDelay is always 0 for a pidstd controller object.

OutputDelay

Time delay on the system Output. OutputDelay is always 0 for a pidstd controller object.

Ts

Sample time. For continuous-time models, Ts = 0. For discrete-time models, Ts is a positive scalar representing the sampling period. This value is expressed in the unit specified by the TimeUnit property of the model. To denote a discrete-time model with unspecified sample time, set Ts = -1.

Changing this property does not discretize or resample the model. Use c2d and d2c to convert between continuous- and discrete-time representations. Use d2d to change the sample time of a discrete-time system.

Default: 0 (continuous time)

TimeUnit

String representing the unit of the time variable. This property specifies the units for the time variable, the sample time Ts, and any time delays in the model. Use any of the following values:

- 'nanoseconds'
- 'microseconds'
- 'milliseconds'
- 'seconds'
- 'minutes'

- 'hours'
- 'days'
- 'weeks'
- 'months'
- 'years'

Changing this property has no effect on other properties, and therefore changes the overall system behavior. Use chgTimeUnit to convert between time units without modifying system behavior.

Default: 'seconds'

InputName

Input channel names. Set InputName to a string for single-input model. For a multiinput model, set InputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign input names for multi-input models. For example, if **sys** is a two-input model, enter:

```
sys.InputName = 'controls';
```

```
The input names automatically expand to { 'controls(1) '; 'controls(2) '}.
```

You can use the shorthand notation u to refer to the InputName property. For example, sys.u is equivalent to sys.InputName.

Input channel names have several uses, including:

- · Identifying channels on model display and plots
- · Extracting subsystems of MIMO systems
- · Specifying connection points when interconnecting models

Default: Empty string ' ' for all input channels

InputUnit

Input channel units. Use InputUnit to keep track of input signal units. For a singleinput model, set InputUnit to a string. For a multi-input model, set InputUnit to a cell array of strings. InputUnit has no effect on system behavior. Default: Empty string ' ' for all input channels

InputGroup

Input channel groups. The InputGroup property lets you assign the input channels of MIMO systems into groups and refer to each group by name. Specify input groups as a structure. In this structure, field names are the group names, and field values are the input channels belonging to each group. For example:

```
sys.InputGroup.controls = [1 2];
sys.InputGroup.noise = [3 5];
```

creates input groups named controls and noise that include input channels 1, 2 and 3, 5, respectively. You can then extract the subsystem from the controls inputs to all outputs using:

sys(:,'controls')

Default: Struct with no fields

OutputName

Output channel names. Set OutputName to a string for single-output model. For a multioutput model, set OutputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign output names for multi-output models. For example, if **sys** is a two-output model, enter:

```
sys.OutputName = 'measurements';
```

The output names automatically expand to { 'measurements(1) '; 'measurements(2) ' }.

You can use the shorthand notation y to refer to the OutputName property. For example, sys.y is equivalent to sys.OutputName.

Output channel names have several uses, including:

- · Identifying channels on model display and plots
- · Extracting subsystems of MIMO systems
- Specifying connection points when interconnecting models

Default: Empty string ' ' for all output channels

OutputUnit

Output channel units. Use OutputUnit to keep track of output signal units. For a single-output model, set OutputUnit to a string. For a multi-output model, set OutputUnit to a cell array of strings. OutputUnit has no effect on system behavior.

Default: Empty string ' ' for all output channels

OutputGroup

Output channel groups. The OutputGroup property lets you assign the output channels of MIMO systems into groups and refer to each group by name. Specify output groups as a structure. In this structure, field names are the group names, and field values are the output channels belonging to each group. For example:

sys.OutputGroup.temperature = [1]; sys.InputGroup.measurement = [3 5];

creates output groups named temperature and measurement that include output channels 1, and 3, 5, respectively. You can then extract the subsystem from all inputs to the measurement outputs using:

sys('measurement',:)

Default: Struct with no fields

Name

System name. Set Name to a string to label the system.

Default: ' '

Notes

Any text that you want to associate with the system. Set **Notes** to a string or a cell array of strings.

Default: { }

UserData

Any type of data you want to associate with system. Set UserData to any MATLAB data type.

Default: []

SamplingGrid

Sampling grid for model arrays, specified as a data structure.

For model arrays that are derived by sampling one or more independent variables, this property tracks the variable values associated with each model in the array. This information appears when you display or plot the model array. Use this information to trace results back to the independent variables.

Set the field names of the data structure to the names of the sampling variables. Set the field values to the sampled variable values associated with each model in the array. All sampling variables should be numeric and scalar valued, and all arrays of sampled values should match the dimensions of the model array.

For example, suppose you create a 11-by-1 array of linear models, sysarr, by taking snapshots of a linear time-varying system at times t = 0:10. The following code stores the time samples with the linear models.

```
sysarr.SamplingGrid = struct('time',0:10)
```

Similarly, suppose you create a 6-by-9 model array, M, by independently sampling two variables, zeta and w. The following code attaches the (zeta,w) values to M.

```
[zeta,w] = ndgrid(<6 values of zeta>,<9 values of w>)
M.SamplingGrid = struct('zeta',zeta,'w',w)
```

When you display $\tt M,$ each entry in the array includes the corresponding ${\tt zeta}$ and $\tt w$ values.

М

```
s^2 + 3.5 s + 25
```

For model arrays generated by linearizing a Simulink model at multiple parameter values or operating points, the software populates SamplingGrid automatically with the variable values that correspond to each entry in the array. For example, the Simulink Control Design commands linearize and slLinearizer populate SamplingGrid in this way.

Default: []

Examples

Create a continuous-time standard-form PDF controller with proportional gain 1, derivative time 3, and a filter divisor of 6.

```
Continuous-time PDF controller in standard form
```

The display shows the controller type, formula, and coefficient values.

Create a discrete-time PI controller with trapezoidal discretization formula.

To create a discrete-time controller, set the value of Ts using Name, Value syntax.

```
C = pidstd(1,0.5,'Ts',0.1,'IFormula','Trapezoidal') % Ts = 0.1s
```

This command produces the result:

Discrete-time PI controller in standard form:

Kp * (1 + ---- * -----) Ti 2*(z-1)

with Kp = 1, Ti = 0.5, Ts = 0.1

Alternatively, you can create the same discrete-time controller by supplying Ts as the fifth argument after all four PID parameters Kp, Ti, Td, and N.

C = pidstd(5,2.4,0,Inf,0.1,'IFormula','Trapezoidal');

Create a PID controller and set dynamic system properties ${\tt InputName}$ and ${\tt OutputName}.$

```
C = pidstd(1,0.5,3,'InputName','e','OutputName','u')
```

Create a 2-by-3 grid of PI controllers with proportional gain ranging from 1-2 and integral time ranging from 5-9.

Create a grid of PI controllers with proportional gain varying row to row and integral time varying column to column. To do so, start with arrays representing the gains.

Kp = [1 1 1;2 2 2]; Ti = [5:2:9;5:2:9]; pi_array = pidstd(Kp,Ti,'Ts',0.1,'IFormula','BackwardEuler');

These commands produce a 2-by-3 array of discrete-time pidstd objects. All pidstd objects in an array must have the same sample time, discrete integrator formulas, and dynamic system properties (such as InputName and OutputName).

Alternatively, you can use the stack command to build arrays of pidstd objects.

C = pidstd(1,5,0.1) % PID controller Cf = pidstd(1,5,0.1,0.5) % PID controller with filter pid_array = stack(2,C,Cf); % stack along 2nd array dimension

These commands produce a 1-by-2 array of controllers. Enter the command:

```
size(pid_array)
```

to see the result

1x2 array of PID controller. Each PID has 1 output and 1 input.

Convert a parallel-form pid controller to standard form.

Parallel PID form expresses the controller actions in terms of an proportional, integral, and derivative gains K_p , K_i , and K_d , and a filter time constant T_f . You can convert a parallel form controller parsys to standard form using pidstd, provided that:

- parsys is not a pure integrator (I) controller.
- The gains Kp, Ki, and Kd of parsys all have the same sign.

```
parsys = pid(2,3,4,5); % Standard-form controller
stdsys = pidstd(parsys)
```

These commands produce a parallel-form controller:

Continuous-time PIDF controller in standard form:

Kp * (1 + ---- * --- + Td * -----) Ti s (Td/N)*s+1

with Kp = 2, Ti = 0.66667, Td = 2, N = 0.4

Convert a continuous-time dynamic system that represents a PID controller to standard pidstd form.

The dynamic system

$$H(s) = \frac{3(s+1)(s+2)}{s}$$

represents a PID controller. Use pidstd to obtain H(s) to in terms of the standard-form PID parameters K_p , T_i , and T_d .

H = zpk([-1,-2],0,3); C = pidstd(H)

These commands produce the result:

Continuous-time PID controller in standard form:

with Kp = 9, Ti = 1.5, Td = 0.33333

Convert a discrete-time dynamic system that represents a PID controller with derivative filter to standard pidstd form.

% PIDF controller expressed in zpk form sys = zpk([-0.5,-0.6],[1 -0.2],3,'Ts',0.1)

The resulting pidstd object depends upon the discrete integrator formula you specify for IFormula and DFormula.

For example, if you use the default ForwardEuler for both formulas:

C = pidstd(sys)

you obtain the result:

Discrete-time PIDF controller in standard form:

 1
 Ts
 1

 Kp * (1 + ---- * ---- + Td * -----)
 Ti
 z-1

 Ti
 z-1
 (Td/N)+Ts/(z-1)

with Kp = 2.75, Ti = 0.045833, Td = 0.0075758, N = 0.090909, Ts = 0.1

For this particular sys, you cannot write sys in standard PID form using the BackwardEuler formula for the DFormula. Doing so would result in N < 0, which is not permitted. In that case, pidstd returns an error.

Similarly, you cannot write **sys** in standard form using the **Trapezoidal** formula for both integrators. Doing so would result in negative **Ti** and **Td**, which also returns an error.

Discretize a continuous-time pidstd controller.

First, discretize the controller using the 'zoh' method of c2d.

Cc = pidstd(1,2,3,4) % continuous-time pidf controller Cd1 = c2d(Cc,0.1,'zoh')

c2d computes new parameters for the discrete-time controller:

Discrete-time PIDF controller in standard form:

 1
 Ts
 1

 Kp * (1 + ---- * ---- + Td * ------)
 Ti

 Ti
 z-1
 (Td/N)+Ts/(z-1)

with Kp = 1, Ti = 2, Td = 3.2044, N = 4, Ts = 0.1

The resulting discrete-time controller uses ForwardEuler $(T_s/(z-1))$ for both IFormula and DFormula.

The discrete integrator formulas of the discretized controller depend upon the c2d discretization method, as described in "Tips" on page 1-630. To use a different IFormula and DFormula, directly set TS, IFormula, and DFormula to the desired values:

```
Cd2 = Cc;
Cd2.Ts = 0.1;
Cd2.IFormula = 'BackwardEuler';
Cd2.DFormula = 'BackwardEuler';
```

These commands do not compute new parameter values for the discretized controller. To see this, enter:

Cd2

to obtain the result:

Discrete-time PIDF controller in standard form:

Kp * $(1 + \frac{1}{Ti} + \frac{Ts*z}{z-1} + Td + \frac{1}{(Td/N)+Ts*z/(z-1)})$ with Kp = 1, Ti = 2, Td = 3, N = 4, Ts = 0.1

More About

Tips

- Use pidstd either to create a pidstd controller object from known PID gain, integral and derivative times, and filter divisor, or to convert a dynamic system model to a pidstd object.
- To tune a PID controller for a particular plant, use pidtune or pidTuner.

- Create arrays of pidstd controllers by:
 - Specifying array values for Kp,Ti,Td, and N
 - Specifying an array of dynamic systems **sys** to convert to standard PID form
 - Using stack to build arrays from individual controllers or smaller arrays

In an array of pidstd controllers, each controller must have the same sample time Ts and discrete integrator formulas IFormula and DFormula.

• To create or convert to a parallel-form controller, use pid. Parallel form expresses the controller actions in terms of proportional, integral, and derivative gains K_p , K_i and K_d , and a filter time constant T_f :

$$C = K_p + \frac{K_i}{s} + \frac{K_d s}{T_f s + 1}.$$

- There are two ways to discretize a continuous-time pidstd controller:
 - Use the c2d command. c2d computes new parameter values for the discretized controller. The discrete integrator formulas of the discretized controller depend upon the c2d discretization method you use, as shown in the following table.

c2d Discretization Method	IFormula	DFormula
'zoh'	ForwardEuler	ForwardEuler
'foh'	Trapezoidal	Trapezoidal
'tustin'	Trapezoidal	Trapezoidal
'impulse'	ForwardEuler	ForwardEuler
'matched'	ForwardEuler	ForwardEuler

For more information about C2d discretization methods, See the C2d reference page. For more information about <code>IFormula</code> and <code>DFormula</code>, see "Properties" on page 1-618 .

• If you require different discrete integrator formulas, you can discretize the controller by directly setting Ts, IFormula, and DFormula to the desired values. (See this example.) However, this method does not compute new gain and filter-constant values for the discretized controller. Therefore, this method might yield a poorer match between the continuous- and discrete-time pidstd controllers than using c2d.

• "What Are Model Objects?"

See Also

pidstd2 | pidstddata | pidtune | pidTuner

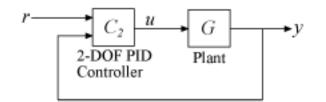
Introduced in R2010b

pidstd2

 $\label{eq:create 2-DOF PID controller in standard form, convert to standard-form 2-DOF PID controller$

pid2 controller objects represent two-degree-of-freedom (2-DOF) PID controllers in parallel form. Use pid2 either to create a pid2 controller object from known coefficients or to convert a dynamic system model to a pid2 object.

Two-degree-of-freedom (2-DOF) PID controllers include setpoint weighting on the proportional and derivative terms. A 2-DOF PID controller is capable of fast disturbance rejection without significant increase of overshoot in setpoint tracking. 2-DOF PID controllers are also useful to mitigate the influence of changes in the reference signal on the control signal. The following illustration shows atypical control architecture using a 2-DOF PID controller.



Syntax

```
C2 = pidstd2(Kp,Ti,Td,N,b,c)
C2 = pidstd2(Kp,Ti,Td,N,b,c,Ts)
C2 = pidstd2(sys)
C2 = pid2(____,Name,Value)
```

Description

C2 = pidstd2(Kp,Ti,Td,N,b,c) creates a continuous-time 2-DOF PID controller with proportional gain Kp, integrator and derivative time constants Ti, and Td,

and derivative filter divisor N. The controller also has setpoint weighting b on the proportional term, and setpoint weighting c on the derivative term. The relationship between the 2-DOF controller's output (u) and its two inputs (r and y) is given by:

$$u = K_p \left[(br - y) + \frac{1}{T_i s} (r - y) + \frac{T_d s}{\frac{T_d}{N} s + 1} (cr - y) \right].$$

This representation is in *standard form*. If all of the coefficients are real-valued, then the resulting C2 is a pidstd2 controller object. If one or more of these coefficients is tunable (realp or genmat), then C2 is a tunable generalized state-space (genss) model object.

C2 = pidstd2(Kp,Ti,Td,N,b,c,Ts) creates a discrete-time 2-DOF PID controller with sample time Ts. The relationship between the controller's output and inputs is given by:

$$u = K_p \left[(br - y) + \frac{1}{T_i} IF(z)(r - y) + \frac{T_d}{\frac{T_d}{N} + DF(z)} (cr - y) \right].$$

IF(z) and DF(z) are the *discrete integrator formulas* for the integrator and derivative filter. By default,

$$IF(z) = DF(z) = \frac{T_s}{z-1}.$$

To choose different discrete integrator formulas, use the IFormula and DFormula properties. (See "Properties" on page 1-638 for more information). If DFormula = 'ForwardEuler' (the default value) and N \neq Inf, then Ts, Td, and N must satisfy Td/ N > Ts/2. This requirement ensures a stable derivative filter pole.

C2 = pidstd2(sys) converts the dynamic system sys to a standard form pidstd2 controller object.

C2 = pid2(_____, Name, Value) specifies additional properties as comma-separated pairs of Name, Value arguments.

Input Arguments

Кр

Proportional gain.

Kp can be:

- A real and finite value.
- An array of real and finite values.
- A tunable parameter (realp) or generalized matrix (genmat).
- A tunable surface for gain-scheduled tuning, created using tunableSurface (requires Robust Control Toolbox software).

Default: 1

Τi

Integrator time.

Ti can be:

- A real and positive value.
- · An array of real and positive values.
- A tunable parameter (realp) or generalized matrix (genmat).
- A tunable surface for gain-scheduled tuning, created using tunableSurface (requires Robust Control Toolbox software).

When Ti = Inf, the controller has no integral action.

Default: Inf

Тd

Derivative time.

Td can be:

- A real, finite, and nonnegative value.
- An array of real, finite, and nonnegative values.
- A tunable parameter (realp) or generalized matrix (genmat).

• A tunable surface for gain-scheduled tuning, created using tunableSurface (requires Robust Control Toolbox software).

When Td = 0, the controller has no derivative action.

Default: 0

Ν

Derivative filter divisor.

N can be:

- A real and positive value.
- · An array of real and positive values.
- A tunable parameter (realp) or generalized matrix (genmat).
- A tunable surface for gain-scheduled tuning, created using tunableSurface (requires Robust Control Toolbox software).

When N = Inf, the controller has no filter on the derivative action.

Default: Inf

b

Setpoint weighting on proportional term.

b can be:

- A real, nonnegative, and finite value.
- An array of real, nonnegative, finite values.
- A tunable parameter (realp) or generalized matrix (genmat).
- A tunable surface for gain-scheduled tuning, created using tunableSurface (requires Robust Control Toolbox software).

When b = 0, changes in setpoint do not feed directly into the proportional term.

Default: 1

C

Setpoint weighting on derivative term.

c can be:

- A real, nonnegative, and finite value.
- An array of real, nonnegative, finite values.
- A tunable parameter (realp) or generalized matrix (genmat).
- A tunable surface for gain-scheduled tuning, created using tunableSurface (requires Robust Control Toolbox software).

When c = 0, changes in setpoint do not feed directly into the proportional term.

Default: 1

Ts

Sample time.

To create a discrete-time pidstd2 controller, provide a positive real value (Ts > 0).pidstd2 does not support discrete-time controller with undetermined sample time (Ts = -1).

 Ts must be a scalar value. In an array of pidstd2 controllers, each controller must have the same $\mathsf{Ts}.$

Default: 0 (continuous time)

sys

SISO dynamic system to convert to standard ${\tt pidstd2}$ form.

sys be a two-input, one-output system. sys must represent a valid 2-DOF controller that can be written in standard form with Ti > 0, $Td \ge 0$, and N > 0.

sys can also be an array of SISO dynamic systems.

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside single quotes (' '). You can specify several name and value pair arguments in any order as Name1, Value1, ..., NameN, ValueN.

Use Name, Value syntax to set the numerical integration formulas IFormula and DFormula of a discrete-time pidstd2 controller, or to set other object properties such as InputName and OutputName. For information about available properties of pidstd2 controller objects, see "Properties" on page 1-638.

Output Arguments

C2

2-DOF PID controller, returned as a pidstd2 controller object, an array of pidstd2 controller objects, a genss object, or a genss array.

- If all the coefficients have scalar numeric values, then C2 is a pidstd2 controller object.
- If one or more coefficients is a numeric array, C2 is an array of pidstd2 controller objects. The controller type (such as PI, PID, or PDF) depends upon the values of the gains. For example, when Td = 0, but Kp and Ti are nonzero and finite, C2 is a PI controller.
- If one or more coefficients is a tunable parameter (realp), generalized matrix (genmat), or tunable gain surface (tunableSurface), then C2 is a generalized state-space model (genss).

Properties

b, c

Setpoint weights on the proportional and derivative terms, respectively. **b** and **c** values are real, finite, and positive. When you create a 2-DOF PID controller using the pidstd2 command, the initial values of these properties are set by the **b**, and **c** input arguments, respectively.

Кр

Proportional gain.

The value of Kp is real and finite. When you create a 2-DOF PID controller using the pidstd2 command, the initial value of this property is set by the Kp input argument.

Τi

Integrator time. Ti is real and positive. When you create a 2-DOF PID controller using the pidstd2 command, the initial value of this property is set by the Ti input argument. When Ti = Inf, the controller has no integral action.

Td

Derivative time. Td is real, finite, and nonnegative. When you create a 2-DOF PID controller using the pidstd2 command, the initial value of this property is set by the Td input argument. When Td = 0, the controller has no derivative action.

Ν

•

Derivative filter divisor. N must be real and positive. When you create a 2-DOF PID controller using the pidstd2 command, the initial value of this property is set by the N input argument.

IFormula

Discrete integrator formula IF(z) for the integrator of the discrete-time pidstd2 controller C2. The relationship between the inputs and output of C2 is given by:

$$u = K_p \left[(br - y) + \frac{1}{T_i} IF(z)(r - y) + \frac{T_d}{\frac{T_d}{N} + DF(z)} (cr - y) \right].$$

IFormula can take the following values:

$$ForwardEuler' - IF(z) = \frac{T_s}{z-1}.$$

This formula is best for small sample time, where the Nyquist limit is large compared to the bandwidth of the controller. For larger sample time, the ForwardEuler formula can result in instability, even when discretizing a system that is stable in continuous time.

'BackwardEuler' —
$$IF(z) = \frac{T_s z}{z-1}$$

An advantage of the **BackwardEuler** formula is that discretizing a stable continuoustime system using this formula always yields a stable discrete-time result.

$$\mathsf{'Trapezoidal'} - IF(z) = \frac{T_s}{2} \frac{z+1}{z-1}.$$

An advantage of the Trapezoidal formula is that discretizing a stable continuoustime system using this formula always yields a stable discrete-time result. Of all available integration formulas, the Trapezoidal formula yields the closest match between frequency-domain properties of the discretized system and the corresponding continuous-time system.

When C2 is a continuous-time controller, IFormula is ''.

Default: 'ForwardEuler'

DFormula

Discrete integrator formula DF(z) for the derivative filter of the discrete-time pidstd2 controller C2. The relationship between the inputs and output of C2 is given by:

$$u = K_p \left[(br - y) + \frac{1}{T_i} IF(z)(r - y) + \frac{T_d}{\frac{T_d}{N} + DF(z)} (cr - y) \right].$$

DFormula can take the following values:

ForwardEuler' —
$$DF(z) = \frac{T_s}{z-1}$$
.

This formula is best for small sample time, where the Nyquist limit is large compared to the bandwidth of the controller. For larger sample time, the ForwardEuler formula can result in instability, even when discretizing a system that is stable in continuous time.

'BackwardEuler' —
$$DF(z) = \frac{T_s z}{z-1}$$
.

An advantage of the BackwardEuler formula is that discretizing a stable continuoustime system using this formula always yields a stable discrete-time result.

$$Trapezoidal' - DF(z) = \frac{T_s}{2} \frac{z+1}{z-1}.$$

An advantage of the Trapezoidal formula is that discretizing a stable continuoustime system using this formula always yields a stable discrete-time result. Of all available integration formulas, the Trapezoidal formula yields the closest match between frequency-domain properties of the discretized system and the corresponding continuous-time system.

The Trapezoidal value for DFormula is not available for a pidstd2 controller with no derivative filter (N = Inf).

When C2 is a continuous-time controller, DFormula is ''.

Default: 'ForwardEuler'

InputDelay

Time delay on the system input. InputDelay is always 0 for a pidstd2 controller object.

OutputDelay

Time delay on the system Output. OutputDelay is always 0 for a pidstd2 controller object.

Ts

Sample time. For continuous-time models, Ts = 0. For discrete-time models, Ts is a positive scalar representing the sampling period. This value is expressed in the unit specified by the TimeUnit property of the model. To denote a discrete-time model with unspecified sample time, set Ts = -1.

Changing this property does not discretize or resample the model. Use c2d and d2c to convert between continuous- and discrete-time representations. Use d2d to change the sample time of a discrete-time system.

Default: 0 (continuous time)

TimeUnit

String representing the unit of the time variable. This property specifies the units for the time variable, the sample time Ts, and any time delays in the model. Use any of the following values:

- 'nanoseconds'
- 'microseconds'
- 'milliseconds'
- 'seconds'
- 'minutes'
- 'hours'
- 'days'
- 'weeks'
- 'months'
- 'years'

Changing this property has no effect on other properties, and therefore changes the overall system behavior. Use chgTimeUnit to convert between time units without modifying system behavior.

Default: 'seconds'

InputName

Input channel names. Set InputName to a string for single-input model. For a multiinput model, set InputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign input names for multi-input models. For example, if **sys** is a two-input model, enter:

sys.InputName = 'controls';

The input names automatically expand to { 'controls(1) '; 'controls(2) '}.

You can use the shorthand notation u to refer to the InputName property. For example, sys.u is equivalent to sys.InputName.

Input channel names have several uses, including:

- · Identifying channels on model display and plots
- · Extracting subsystems of MIMO systems
- · Specifying connection points when interconnecting models

Default: Empty string ' ' for all input channels

InputUnit

Input channel units. Use InputUnit to keep track of input signal units. For a singleinput model, set InputUnit to a string. For a multi-input model, set InputUnit to a cell array of strings. InputUnit has no effect on system behavior.

Default: Empty string ' ' for all input channels

InputGroup

Input channel groups. The InputGroup property lets you assign the input channels of MIMO systems into groups and refer to each group by name. Specify input groups as a structure. In this structure, field names are the group names, and field values are the input channels belonging to each group. For example:

sys.InputGroup.controls = [1 2]; sys.InputGroup.noise = [3 5];

creates input groups named controls and noise that include input channels 1, 2 and 3, 5, respectively. You can then extract the subsystem from the controls inputs to all outputs using:

```
sys(:,'controls')
```

Default: Struct with no fields

OutputName

Output channel names. Set OutputName to a string for single-output model. For a multioutput model, set OutputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign output names for multi-output models. For example, if **sys** is a two-output model, enter:

```
sys.OutputName = 'measurements';
```

The output names automatically expand to { 'measurements(1) '; 'measurements(2) ' }.

You can use the shorthand notation y to refer to the OutputName property. For example, sys.y is equivalent to sys.OutputName.

Output channel names have several uses, including:

- Identifying channels on model display and plots
- · Extracting subsystems of MIMO systems
- · Specifying connection points when interconnecting models

Default: Empty string ' ' for all output channels

OutputUnit

Output channel units. Use OutputUnit to keep track of output signal units. For a single-output model, set OutputUnit to a string. For a multi-output model, set OutputUnit to a cell array of strings. OutputUnit has no effect on system behavior.

Default: Empty string ' ' for all output channels

OutputGroup

Output channel groups. The OutputGroup property lets you assign the output channels of MIMO systems into groups and refer to each group by name. Specify output groups as a structure. In this structure, field names are the group names, and field values are the output channels belonging to each group. For example:

```
sys.OutputGroup.temperature = [1];
sys.InputGroup.measurement = [3 5];
```

creates output groups named temperature and measurement that include output channels 1, and 3, 5, respectively. You can then extract the subsystem from all inputs to the measurement outputs using:

```
sys('measurement',:)
```

Default: Struct with no fields

Name

System name. Set Name to a string to label the system.

Default: ' '

Notes

Any text that you want to associate with the system. Set **Notes** to a string or a cell array of strings.

Default: {}

UserData

Any type of data you want to associate with system. Set UserData to any MATLAB data type.

Default: []

SamplingGrid

Sampling grid for model arrays, specified as a data structure.

For model arrays that are derived by sampling one or more independent variables, this property tracks the variable values associated with each model in the array. This information appears when you display or plot the model array. Use this information to trace results back to the independent variables.

Set the field names of the data structure to the names of the sampling variables. Set the field values to the sampled variable values associated with each model in the array. All sampling variables should be numeric and scalar valued, and all arrays of sampled values should match the dimensions of the model array.

For example, suppose you create a 11-by-1 array of linear models, sysarr, by taking snapshots of a linear time-varying system at times t = 0:10. The following code stores the time samples with the linear models.

sysarr.SamplingGrid = struct('time',0:10)

Similarly, suppose you create a 6-by-9 model array, M, by independently sampling two variables, zeta and w. The following code attaches the (zeta,w) values to M.

```
[zeta,w] = ndgrid(<6 values of zeta>,<9 values of w>)
M.SamplingGrid = struct('zeta',zeta,'w',w)
```

When you display M, each entry in the array includes the corresponding ${\tt zeta}$ and w values.

M M(:,:,1,1) [zeta=0.3, w=5] = 25 s^2 + 3 s + 25

```
M(:,:,2,1) [zeta=0.35, w=5] =
25
s^2 + 3.5 s + 25
```

• • •

For model arrays generated by linearizing a Simulink model at multiple parameter values or operating points, the software populates SamplingGrid automatically with the variable values that correspond to each entry in the array. For example, the Simulink Control Design commands linearize and slLinearizer populate SamplingGrid in this way.

Default: []

Examples

2-DOF PDF Controller

Create a continuous-time 2-DOF PDF controller in standard form. To do so, set the integral time constant to Inf. Set the other gains and the filter divisor to the desired values.

```
Kp = 1;
Ti = Inf; % No integrator
Td = 3;
N = 6;
b = 0.5; % setpoint weight on proportional term
c = 0.5; % setpoint weight on derivative term
C2 = pidstd2(Kp,Ti,Td,N,b,c)
C2 =
u = Kp * [(b*r-y) + Td * ----- * (c*r-y)]
(Td/N)*s+1
with Kp = 1, Td = 3, N = 6, b = 0.5, c = 0.5
Continuous-time 2-DOF PDF controller in standard form
```

The display shows the controller type, formula, and parameter values, and verifies that the controller has no integrator term.

Discrete-Time 2-DOF PI Controller in Standard Form

Create a discrete-time 2-DOF PI controller in standard form, using the trapezoidal discretization formula. Specify the formula using Name, Value syntax.

```
Kp = 1;
Ti = 2.4;
Td = 0;
N = Inf;
b = 0.5;
c = 0;
Ts = 0.1;
C2 = pidstd2(Kp,Ti,Td,N,b,c,Ts, 'IFormula', 'Trapezoidal')
C2 =
u = Kp * [(b*r-y) + \frac{1}{1-1-1} * \frac{Ts*(z+1)}{1-1-1-1} * (r-y)]
Ti 2*(z-1)
with Kp = 1, Ti = 2.4, b = 0.5, Ts = 0.1
Sample time: 0.1 seconds
Discrete-time 2-DOF PI controller in standard form
```

Setting Td = 0 specifies a PI controller with no derivative term. As the display shows, the values of N and c are not used in this controller. The display also shows that the trapezoidal formula is used for the integrator.

2-DOF PID Controller with Named Inputs and Output

Create a 2-DOF PID controller in standard form, and set the dynamic system properties InputName and OutputName. Naming inputs and outpus is useful, for example, when you interconnect the PID controller with other dynamic system models using the connect command.

C2 = pidstd2(1,2,3,10,1,1,'InputName',{'r','y'},'OutputName','u')

 $\begin{array}{l} \text{C2 =} \\ u = \text{Kp } * \left[(b \text{*}r \text{-}y) + \frac{1}{1} & \frac{1}{$

A 2-DOF PID controller has two inputs and one output. Therefore, the 'InputName' property is an array of two strings, one for each input. The model display does not show the input and output names for the PID controller, but you can examine the property values to see them. For instance, verify the input name of the controller.

C2.InputName

ans = 'r' 'y'

Array of 2-DOF PID Controllers

Create a 2-by-3 grid of 2-DOF PI controllers in standard form. The proportional gain ranges from 1-2 across the array rows, and the integrator time constant ranges from 5-9 across columns.

To build the array of PID controllers, start with arrays representing the gains.

Kp = [1 1 1;2 2 2]; Ti = [5:2:9;5:2:9];

When you pass these arrays to the pidstd2 command, the command returns the array of controllers.

```
pi_array = pidstd2(Kp,Ti,0,Inf,0.5,0,'Ts',0.1,'IFormula','BackwardEuler');
size(pi_array)
```

2x3 array of 2-DOF PID controller. Each PID has 1 output and 2 inputs. If you provide scalar values for some coefficients, pidstd2 automatically expands them and assigns the same value to all entries in the array. For instance, in this example, Td = 0, so that all entries in the array are PI controllers. Also, all entries in the array have b = 0.5.

Access entries in the array using array indexing. For dynamic system arrays, the first two dimensions are the I/O dimensions of the model, and the remaining dimensions are the array dimensions. Therefore, the following command extracts the (2,3) entry in the array.

```
pi23 = pi_array(:,:,2,3)
pi23 =
u = Kp * [(b*r-y) + \frac{1}{Ti} x^{-1} x^{-1} (r-y)]
with Kp = 2, Ti = 9, b = 0.5, Ts = 0.1
Sample time: 0.1 seconds
Discrete-time 2-DOF PI controller in standard form
```

You can also build an array of PID controllers using the stack command.

C2 = pidstd2(1,5,0.1,Inf,0.5,0.5);	% PID controller
C2f = pidstd2(1,5,0.1,0.5,0.5,0.5);	<pre>% PID controller with filter</pre>
pid_array = stack(2,C2,C2f);	% stack along 2nd array dimension

These commands return a 1-by-2 array of controllers.

```
size(pid_array)
```

1x2 array of 2-DOF PID controller. Each PID has 1 output and 2 inputs.

All PID controllers in an array must have the same sample time, discrete integrator formulas, and dynamic system properties such as InputName and OutputName.

Convert 2-DOF PID Controller from Parallel to Standard Form

Convert a parallel-form pid2 controller to standard form.

Parallel PID form expresses the controller actions in terms of proportional, integral, and derivative gains Kp, Ki, and Kd, and filter time constant Tf. You can convert a parallel-form pid2 controller to standard form using the pidstd2 command, provided that both of the following are true:

- The pid2 controller can be expressed in valid standard form.
- The gains Kp, Ki, and Kd of the pid2 controller all have the same sign.

For example, consider the following parallel-form controller.

Kp = 2; Ki = 3; Kd = 4; Tf = 2; b = 0.1; c = 0.5; C2_par = pid2(Kp,Ki,Kd,Tf,b,c)

C2 par =

u = Kp (b*r-y) + Ki --- (r-y) + Kd ------ (c*r-y) s Tf*s+1

with Kp = 2, Ki = 3, Kd = 4, Tf = 2, b = 0.1, c = 0.5

Continuous-time 2-DOF PIDF controller in parallel form.

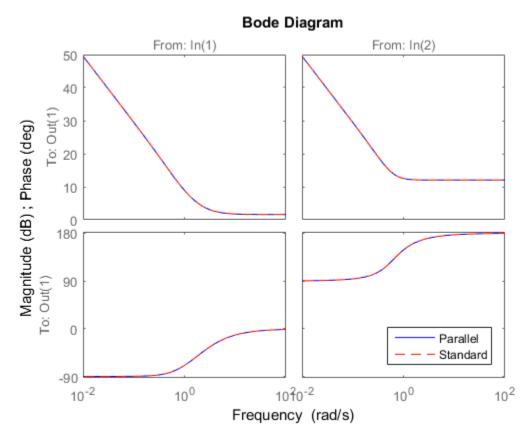
Convert this controller to parallel form using pidstd2.

```
C2_std = pidstd2(C2_par)
```

 $C2_std = \frac{1}{u} = Kp * [(b*r-y) + \frac{1}{1} + \frac{1}{1} + \frac{s}{1} +$

The display confirms the new standard form. A response plot confirms that the two forms are equivalent.

```
bodeplot(C2_par,'b-',C2_std,'r--')
legend('Parallel','Standard','Location','Southeast')
```



Convert Dynamic System to Standard-Form 2-DOF PID Controller

Convert a two-input, one-output continuous-time dynamic system that represents a 2-DOF PID controller to a standard-form pidstd2 controller.

The following state-space matrices represent a 2-DOF PID controller.

A = [0,0;0,-8.181]; B = [1,-1;-0.1109,8.181]; C = [0.2301,10.66]; D = [0.8905,-11.79]; sys = ss(A,B,C,D);

Rewrite sys in terms of the standard-form PID parameters Kp, Ti, Td, and N, and the setpoint weights b and c.

```
C2 = pidstd2(sys)
C2 = u = Kp * [(b*r-y) + \frac{1}{1} + \frac{1}{1} + \frac{s}{1} +
```

Convert Discrete-Time Dynamic System to 2-DOF Standard-Form PID Controller

Convert a discrete-time dynamic system that represents a 2-DOF PID controller with derivative filter to standard pidstd2 form.

The following state-space matrices represent a discrete-time 2-DOF PID controller with a sample time of 0.05 s.

```
A = [1,0;0,0.6643];
B = [0.05,-0.05; -0.004553,0.3357];
C = [0.2301,10.66];
D = [0.8905,-11.79];
Ts = 0.05;
sys = ss(A,B,C,D,Ts);
```

When you convert **sys** to 2-DOF PID form, the result depends on which discrete integrator formulas you specify for the conversion. For instance, use the default, **ForwardEuler**, for both the integrator and the derivative.

C2fe = pidstd2(sys)

```
C2fe =

u = Kp * [(b*r-y) + \frac{1}{Ti} * \frac{Ts}{z-1} * (r-y) + Td * \frac{1}{(Td/N)+Ts/(z-1)} * (c*r-y)]
with Kp = 1.13, Ti = 4.91, Td = 1.41, N = 9.43, b = 0.66, c = 0.0136, Ts = 0.05

Sample time: 0.05 seconds

Discrete-time 2-DOF PIDF controller in standard form

Now convert using the Trapezoidal formula.

C2trap = pidstd2(sys, 'IFormula', 'Trapezoidal', 'DFormula', 'Trapezoidal')

C2trap =

u = Kp * [(b*r-y) + \frac{1}{Ti} * \frac{Ts*(z+1)}{2*(z-1)} * (r-y) + Td * \frac{1}{(Td/N)+Ts/2*(z+1)/(z-1)} * (c*r-y)]
with Kp = 1.12, Ti = 4.89, Td = 1.41, N = 11.4, b = 0.658, c = 0.0136, Ts = 0.05

Sample time: 0.05 seconds

Discrete-time 2-DOF PIDF controller in standard form
```

The displays show the difference in resulting coefficient values and functional form.

For some dynamic systems, attempting to use the Trapezoidal or BackwardEuler integrator formulas yields invalid results, such as negative Ti, Td, or N values. In such cases, pidstd2 returns an error.

Discretize a Standard-Form 2-DOF PID Controller

Discretize a continuous-time standard-form 2-DOF PID controller and specify the integral and derivative filter formulas.

Create a continuous-time pidstd2 controller and discretize it using the zero-order-hold method of the c2d command.

```
C2con = pidstd2(10,5,3,0.5,1,1); % continuous-time 2-DOF PIDF controller
C2dis1 = c2d(C2con,0.1,'zoh')
```

```
C2dis1 =
```

 $u = Kp * [(b*r-y) + \frac{1}{Ti} \\ Ti \\ z-1 \\ x \\ (r-y) + Td \\ (Td/N)+Ts/(z-1) \\ (Td/N)+Ts/(z-1) \\ x \\ (true) \\ (Td/N)+Ts/(z-1) \\ x \\ (true) \\ (true)$

The display shows that **c2d** computes new PID coefficients for the discrete-time controller.

The discrete integrator formulas of the discretized controller depend on the c2d discretization method, as described in "Tips". For the zoh method, both IFormula and DFormula are ForwardEuler.

```
C2dis1.IFormula
C2dis1.DFormula
ans =
ForwardEuler
ans =
ForwardEuler
```

If you want to use different formulas from the ones returned by **C2d**, then you can directly set the **Ts**, **IFormula**, and **DFormula** properties of the controller to the desired values.

```
C2dis2 = C2con;
C2dis2.Ts = 0.1;
C2dis2.IFormula = 'BackwardEuler';
C2dis2.DFormula = 'BackwardEuler';
```

However, these commands do not compute new coefficients for the discretized controller. To see this, examine C2dis2 and compare the coefficients to C2con and C2dis1.

C2dis2

```
C2dis2 =

u = Kp * [(b*r-y) + \frac{1}{Ti} + \frac{Ts*z}{z-1} + (r-y) + Td * \frac{1}{(Td/N)+Ts*z/(z-1)} * (c*r-y)]
with Kp = 10, Ti = 5, Td = 3, N = 0.5, b = 1, c = 1, Ts = 0.1

Sample time: 0.1 seconds

Discrete-time 2-DOF PIDF controller in standard form
```

- "Two-Degree-of-Freedom PID Controllers"
- "Discrete-Time Proportional-Integral-Derivative (PID) Controllers"

More About

Tips

- To design a PID controller for a particular plant, use pidtune or pidTuner. To create a tunable 2-DOF PID controller as a control design block, use ltiblock.pid2.
- To break a 2-DOF controller into two SISO control components, such as a feedback controller and a feedforward controller, use getComponents.
- Create arrays of pidstd2 controllers by:
 - Specifying array values for one or more of the coefficients Kp, Ti, Td, N, b, and c.
 - Specifying an array of dynamic systems **sys** to convert to **pid2** controller objects.
 - Using stack to build arrays from individual controllers or smaller arrays.
 - Passing an array of plant models to pidtune.

In an array of pidstd2 controllers, each controller must have the same sample time Ts and discrete integrator formulas IFormula and DFormula.

• To create or convert to a parallel-form controller, use pid2. Parallel form expresses the controller actions in terms of proportional, integral, and derivative gains K_p , K_i and K_d , and a filter time constant T_f . For example, the relationship between the inputs and output of a continuous-time parallel-form 2-DOF PID controller is given by:

$$u = K_p \left(br - y \right) + \frac{K_i}{s} \left(r - y \right) + \frac{K_d s}{T_f s + 1} \left(cr - y \right).$$

- There are two ways to discretize a continuous-time pidstd2 controller:
 - Use the c2d command. c2d computes new parameter values for the discretized controller. The discrete integrator formulas of the discretized controller depend upon the c2d discretization method you use, as shown in the following table.

c2d Discretization Method	IFormula	DFormula
'zoh'	ForwardEuler	ForwardEuler
'foh'	Trapezoidal	Trapezoidal
'tustin'	Trapezoidal	Trapezoidal
'impulse'	ForwardEuler	ForwardEuler
'matched'	ForwardEuler	ForwardEuler

For more information about C2d discretization methods, See the C2d reference page. For more information about <code>IFormula</code> and <code>DFormula</code>, see "Properties" on page 1-638 .

- If you require different discrete integrator formulas, you can discretize the controller by directly setting Ts, IFormula, and DFormula to the desired values. (See "Discretize a Standard-Form 2-DOF PID Controller" on page 1-653.) However, this method does not compute new gain and filter-constant values for the discretized controller. Therefore, this method might yield a poorer match between the continuous- and discrete-time pidstd2 controllers than using c2d.
- "What Are Model Objects?"

See Also

pid2 | pidstddata2 | pidtune | pidTuner | getComponents

Introduced in R2015b

pidstddata

Access coefficients of standard-form PID controller

Syntax

```
[Kp,Ti,Td,N] = pidstddata(sys)
[Kp,Ti,Td,N,Ts] = pidstddata(sys)
[Kp,Ti,Td,N,Ts] = pidstddata(sys, J1,...,JN)
```

Description

[Kp,Ti,Td,N] = pidstddata(sys) returns the proportional gain Kp, integral time Ti, derivative time Td, and filter divisor N of the standard-form controller represented by the dynamic system sys.

[Kp,Ti,Td,N,Ts] = pidstddata(sys) also returns the sample time Ts.

[Kp,Ti,Td,N,Ts] = pidstddata(sys, J1,...,JN) extracts the data for a subset of entries in the array of sys dynamic systems. The indices J specify the array entries to extract.

Input Arguments

sys

SISO dynamic system or array of SISO dynamic systems. If **sys** is not a **pidstd** object, it must represent a valid PID controller that can be written in standard PID form.

J

Integer indices of N entries in the array sys of dynamic systems.

Output Arguments

Кр

Proportional gain of the standard-form PID controller represented by dynamic system ${\tt sys.}$

If sys is a pidstd controller object, the output Kp is equal to the Kp value of sys.

If **sys** is not a **pidstd** object, **Kp** is the proportional gain of a standard-form PID controller equivalent to **sys**.

If sys is an array of dynamic systems, Kp is an array of the same dimensions as sys.

Ti

Integral time constant of the standard-form PID controller represented by dynamic system ${\tt sys}.$

If sys is a pidstd controller object, the output Ti is equal to the Ti value of sys.

If **sys** is not a **pidstd** object, **Ti** is the integral time constant of a standard-form PID controller equivalent to **sys**.

If sys is an array of dynamic systems, Ti is an array of the same dimensions as sys.

Td

Derivative time constant of the standard-form PID controller represented by dynamic system ${\tt sys}.$

If sys is a pidstd controller object, the output Td is equal to the Td value of sys.

If sys is not a pidstd object, Td is the derivative time constant of a standard-form PID controller equivalent to sys.

If sys is an array of dynamic systems, Td is an array of the same dimensions as sys.

N

Filter divisor of the standard-form PID controller represented by dynamic system sys.

If sys is a pidstd controller object, the output N is equal to the N value of sys.

If **sys** is not a **pidstd** object, N is the filter time constant of a standard-form PID controller equivalent to **sys**.

If sys is an array of dynamic systems, N is an array of the same dimensions as sys.

Ts

Sample time of the dynamic system sys. Ts is always a scalar value.

Examples

Extract the proportional, integral, and derivative gains and the filter time constant from a standard-form pidstd controller.

For the following pidstd object:

sys = pidstd(1,4,0.3,10);

you can extract the parameter values from sys by entering:

[Kp Ti Td N] = pidstddata(sys);

Extract the standard-form proportional and integral gains from an equivalent parallel-form PI controller.

For a standard-form PI controller, such as:

sys = pid(2,3);

you can extract the gains of an equivalent parallel-form PI controller by entering:

[Kp Ti] = pidstddata(sys)

These commands return the result:

Kp =

2

Ti =

0.6667

Extract parameters from a dynamic system that represents a PID controller.

The dynamic system

$$H(z) = \frac{(z-0.5)(z-0.6)}{(z-1)(z+0.8)}$$

represents a discrete-time PID controller with a derivative filter. Use pidstddata to extract the standard-form PID parameters.

```
H = zpk([0.5 0.6],[1,-0.8],1,0.1); % sample time Ts = 0.1s
[Kp Ti Td N Ts] = pidstddata(H);
```

the pidstddata function uses the default ForwardEuler discrete integrator formula for Iformula and Dformula to compute the parameter values.

Extract the gains from an array of PI controllers.

```
sys = pidstd(rand(2,3),rand(2,3)); % 2-by-3 array of PI controllers
[Kp Ti Td N] = pidstddata(sys);
```

The parameters Kp, Ti, Td, and N are also 2-by-3 arrays.

Use the index input J to extract the parameters of a subset of sys.

[Kp Ti Td N] = pidstddata(sys,5);

More About

Tips

If sys is not a pidstd controller object, pidstddata returns Kp, Ti, Td and N values of a standard-form controller equivalent to sys.

For discrete-time sys, piddata returns parameters of an equivalent pidstd controller. This controller has discrete integrator formulas Iformula and Dformula set to ForwardEuler. See the pidstd reference page for more information about discrete integrator formulas.

See Also pidstd | pid | get

Introduced in R2010b

pidstddata2

Access coefficients of standard-form 2-DOF PID controller

Syntax

```
[Kp,Ti,Td,N,b,c] = pidstddata2(sys)
[Kp,Ti,Td,N,b,c,Ts] = pidstddata2(sys)
[Kp,Ti,Td,N,b,c,Ts] = pidstddata2(sys,J1,...,JN)
```

Description

[Kp,Ti,Td,N,b,c] = pidstddata2(sys) returns the proportional gain Kp, integral time Ti, derivative time Td, the filter divisor N, and the setpoint weights b and c of the standard-form 2-DOF PID controller represented by the dynamic system sys.

If **sys** is a **pidstd2** controller object, then each output argument is the corresponding coefficient in **sys**.

If **sys** is not a **pidstd2** object, then each output argument is the corresponding coefficient of the standard-form 2-DOF PID controller that is equivalent to **sys**.

If **sys** is an array of dynamic systems, then each output argument is an array of the same dimensions as **sys**.

[Kp,Ti,Td,N,b,c,Ts] = pidstddata2(sys) also returns the sample time Ts. For discrete-time sys that is not a pidstd2 object, pidstddata2 calculates the coefficient values using the default ForwardEuler discrete integrator formula for both IFormula and DFormula. See the pidstd2 reference page for more information about discrete integrator formulas.

[Kp,Ti,Td,N,b,c,Ts] = pidstddata2(sys,J1,...,JN) extracts the data for a subset of entries in sys, where sys is an N-dimensional array of dynamic systems. The indices J specify the array entry to extract.

Examples

Extract Coefficients from Standard-Form 2-DOF PID Controller

Typically, you extract coefficients from a controller obtained from another function, such as pidtune or getBlockValue. For this example, create a standard-form 2-DOF PID controller that has random coefficients.

rng('default'); % for reproducibility C2 = pidstd2(rand,rand,rand,rand,rand,rand);

Extract the PID coefficients, filter divisor, and setpoint weights.

[Kp,Ti,Td,N,b,c] = pidstddata2(C2);

Extract Standard-Form Coefficients from Parallel-Form Controller

Create a 2-DOF PID controller in parallel form.

```
C2 = pid2(2,3,4,10,0.5,0.5)
```

C2 =

u = Kp (b*r-y) + Ki --- (r-y) + Kd ----- (c*r-y) s Tf*s+1

with Kp = 2, Ki = 3, Kd = 4, Tf = 10, b = 0.5, c = 0.5

Continuous-time 2-DOF PIDF controller in parallel form.

Compute the coefficients of an equivalent parallel-form PID controller.

[Kp,Ti,Td,N,b,c] = pidstddata2(C2);

Check some of the cofficients to confirm that they are different from the parallel-form coefficients.

Τi

Ti =

```
0.6667
Td
Td =
2
```

Extract Standard-Form 2-DOF PID Coefficients from Equivalent System

Extract coefficients from a two-input, one-output dynamic system that represents a valid 2-DOF standard-form PID controller.

The following A, B, C, and D matrices form a discrete-time state-space model that represents a 2-DOF PID controller in standard form.

```
A = [1,0;0,0.5];
B = [0.1, -0.1; -0.25, 0.5];
C = [4, 400];
D = [220, -440];
sys = ss(A,B,C,D,0.1)
sys =
  a =
             х2
        x1
         1
   х1
              0
         0 0.5
   х2
  b =
                  u2
          u1
         0.1
                -0.1
   х1
   х2
       -0.25
                0.5
  с =
        x1
             x2
         4 400
   y1
  d =
                u2
         u1
        220 -440
   y1
```

```
Sample time: 0.1 seconds
Discrete-time state-space model.
```

Extract the PID coefficients, filter divisor, and setpoint weights of the model.

[Kp,Ti,Td,N,b,c,Ts] = pidstddata2(sys);

For a discrete-time system, pidstddata2 calculates the coefficient values using the default ForwardEuler discrete integrator formula for both IFormula and DFormula.

Extract Standard-Form Coefficients from 2-DOF PI Controller Array

Typically, you obtain an array of controllers by using pidtune on an array of plant models. For this example, create an 2-by-3 array of standard-form 2-DOF PI controllers with random values of Kp, Ti, and b.

rng('default'); C2 = pidstd2(rand(2,3),rand(2,3),0,10,rand(2,3),0);

Extract all the coefficients from the array.

[Kp,Ti,Td,N,b,c] = pidstddata2(C2);

Each of the outputs is itself a 2-by-3 array. For example, examine Ki.

Τi

Ti =

0.2785	0.9575	0.1576
0.5469	0.9649	0.9706

Extract only the coefficients of entry (2,1) in the array.

[Kp21,Ti21,Td21,N21,b21,c21] = pidstddata2(C2,2,1);

Each of these outputs is a scalar.

Ti21

Ti21 =

0.5469

Input Arguments

sys - 2-DOF PID controller

pidstd2 controller object | dynamic system model | dynamic system array

2-DOF PID controller in standard form, specified as a pidstd2 controller object, a dynamic system model, or a dynamic system array. If sys is not a pidstd2 controller object, it must be a two-input, one-output model that represents a valid 2-DOF PID controller that can be written in standard form.

J – Indices positive integers

Indices of entry to extract from a model array SyS, specified as positive integers. Provide as many indices as there are array dimensions in SyS. For example, suppose SyS is a 4-by-5 (two-dimensional) array of pidstd2 controllers or dynamic system models that represent 2-DOF PID controllers. The following command extracts the data for entry (2,3) in the array.

[Kp,Ti,Td,N,b,c,Ts] = piddstdata2(sys,2,3);

Output Arguments

Kp — Proportional gain

scalar | array

Proportional gain of the standard-form 2-DOF PID controller represented by **sys**, returned as a scalar or array.

If sys is a pidstd2 controller object, then Kp is the Kp value of sys.

If sys is not a pidstd2 object, then Kp is the proportional gain of the standard-form 2-DOF PID controller that is equivalent to sys.

If **sys** is an array of dynamic systems, then **Kp** is an array of the same dimensions as **sys**.

Ti — Integral time constant

scalar | array

Integral time constant of the standard-form 2-DOF PID controller represented by **sys**, returned as a scalar or array.

Td — Derivative time constant

scalar | array

Derivative time constant of the standard-form 2-DOF PID controller represented by **sys**, returned as a scalar or array.

N — Filter divisor

scalar | array

Filter divisor of the parallel-form 2-DOF PID controller represented by **sys**, returned as a scalar or array.

b - Setpoint weight on proportional term

scalar | array

Setpoint weight on the proportional term of the standard-form 2-DOF PID controller represented by **sys**, returned as a scalar or array.

c - Setpoint weight on derivative term

scalar | array

Setpoint weight on the derivative term of the standard-form 2-DOF PID controller represented by **sys**, returned as a scalar or array.

Ts — Sample time

scalar

Sample time of the pidstd2 controller, dynamic system sys, or dynamic system array, returned as a scalar.

See Also

piddata2 | pidstd2 | pidstddata

Introduced in R2015b

pidtool

Open PID Tuner for PID tuning

Note: pidtool has been removed. Use pidTuner instead.

Introduced in R2010b

pidtune

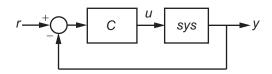
PID tuning algorithm for linear plant model

Syntax

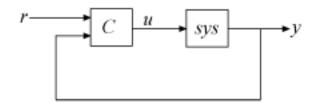
```
C = pidtune(sys,type)
C = pidtune(sys,CO)
C = pidtune(sys,type,wc)
C = pidtune(sys,CO,wc)
C = pidtune(sys,...,opts)
[C,info] = pidtune(...)
```

Description

C = pidtune(sys,type) designs a PID controller of type type for the plant sys. If type specifies a one-degree-of-freedom (1-DOF) PID controller, then the controller is designed for the unit feedback loop as illustrated:



If type specifies a two-degree-of-freedom (2-DOF) PID controller, then pidtune designs a 2-DOF controller as in the feedback loop of this illustration:



pidtune tunes the parameters of the PID controller **C** to balance performance (response time) and robustness (stability margins).

C = pidtune(sys, CO) designs a controller of the same type and form as the controller CO. If sys and CO are discrete-time models, C has the same discrete integrator formulas as CO.

```
C = pidtune(sys,type,wc) and C = pidtune(sys,CO,wc) specify a target value wc for the first 0 dB gain crossover frequency of the open-loop response.
```

C = pidtune(sys,...,opts) uses additional tuning options, such as the target phase margin. Use pidtuneOptions to specify the option set opts.

[C,info] = pidtune(...) returns the data structure info, which contains information about closed-loop stability, the selected open-loop gain crossover frequency, and the actual phase margin.

Input Arguments

sys

Single-input, single-output dynamic system model of the plant for controller design. **sys** can be:

- Any type of SISO dynamic system model, including Numeric LTI models and identified models. If **sys** is a tunable or uncertain model, **pidtune** designs a controller for the current or nominal value of **sys**.
- A continuous- or discrete-time model.
- Stable, unstable, or integrating. A plant with unstable poles, however, might not be stabilizable under PID control.
- A model that includes any type of time delay. A plant with long time delays, however, might not achieve adequate performance under PID control.
- An array of plant models. If **sys** is an array, **pidtune** designs a separate controller for each plant in the array.

If the plant has unstable poles, and **sys** is one of the following:

• A frd model

• A ss model with internal time delays that cannot be converted to I/O delays

you must use pidtuneOptions to specify the number of unstable poles in the plant, if any.

type

Controller type of the controller to design, specified as a string. The term *controller type* refers to which terms are present in the controller action. For example, a PI controller has only a proportional and an integral term, while a PIDF controller contains proportional, integrator, and filtered derivative terms. The **type** string can take the values summarized below. For more detailed information about these controller types, see "PID Controller Types for Tuning"

1-DOF Controllers

- 'P' Proportional only
- 'I' Integral only
- 'PI' Proportional and integral
- 'PD' Proportional and derivative
- 'PDF' Proportional and derivative with first-order filter on derivative term
- 'PID' Proportional, integral, and derivative
- <code>'PIDF'</code> Proportional, integral, and derivative with first-order filter on derivative term

2-DOF Controllers

- 'PI2' 2-DOF proportional and integral
- 'PD2' 2-DOF proportional and derivative
- <code>'PDF2'</code> 2-DOF proportional and derivative with first-order filter on derivative term
- 'PID2' 2-DOF proportional, integral, and derivative
- <code>'PIDF2'</code> 2-DOF proportional, integral, and derivative with first-order filter on derivative term

For more information about 2-DOF PID controllers generally, see "Two-Degree-of-Freedom PID Controllers".

2-DOF Controllers with Fixed Setpoint Weights

- I PD' 2-DOF PID with b = 0, c = 0
- 'I-PDF' 2-DOF PIDF with b = 0, c = 0
- ID-P' 2-DOF PID with b = 0, c = 1
- ' IDF-P' 2-DOF PIDF with b = 0, c = 1
- 'PI-D' -2-DOF PID with b = 1, c = 0
- 'PI-DF' -2-DOF PIDF with b = 1, c = 0

For more detailed information about fixed-setpoint-weight 2-DOF PID controllers, see "PID Controller Types for Tuning".

Controller Form

When you use the type input, pidtune designs a controller in parallel (pid or pid2) form. Use the input CO instead of type if you want to design a controller in standard (pidstd or pidstd2) form.

If sys is a discrete-time model with sample time Ts, pidtune designs a discrete-time controller with the same Ts. The controller has the ForwardEuler discrete integrator formula for both integral and derivative actions. Use the input CO instead of type if you want to design a controller having a different discrete integrator formula.

For more information about PID controller forms and formulas, see:

- "Proportional-Integral-Derivative (PID) Controllers"
- "Two-Degree-of-Freedom PID Controllers"
- "Discrete-Time Proportional-Integral-Derivative (PID) Controllers"

CO

PID controller setting properties of the designed controller, specified as a pid, pidstd, pid2, or pidstd2 object. If you provide C0, pidtune:

- Designs a controller of the type represented by CO.
- Returns a pid controller, if CO is a pid controller.
- Returns a pidstd controller, if CO is a pidstd controller.
- Returns a 2-DOF pid2 controller, if C0 is a pid2 controller.
- Returns a 2-DOF pidstd2 controller, if C0 is a pidstd2 controller.
- Returns a controller with the same Iformula and Dformula values as CO, if sys is a discrete-time system. See the pid, pid2, pidstd, and pidstd2 reference pages for more information about Iformula and Dformula.

wc

Target value for the 0 dB gain crossover frequency of the tuned open-loop response. Specify wc in units of radians/TimeUnit, where TimeUnit is the time unit of sys. The crossover frequency wc roughly sets the control bandwidth. The closed-loop response time is approximately 1/wc.

Increase wc to speed up the response. Decrease wc to improve stability. When you omit wc, pidtune automatically chooses a value, based on the plant dynamics, that achieves a balance between response and stability.

opts

Option set specifying additional tuning options for the pidtune design algorithm, such as target phase margin or design focus. Use pidtuneOptions to create opts.

Output Arguments

C

Controller designed for sys. If sys is an array of linear models, pidtune designs a controller for each linear model and returns an array of PID controllers.

Controller form:

- If the second argument to pidtune is type, C is a pid or pid2 controller.
- If the second argument to pidtune is CO:
 - C is a pid controller, if CO is a pid object.

- C is a pidstd controller, if CO is a pidstd object.
- C is a pid2 controller, if CO is a pid2 object.
- C is a pidstd2 controller, if CO is a pidstd2 object.

Controller type:

- If the second argument to pidtune is type, C generally has the specified type.
- If the second argument to pidtune is CO, C generally has the same type as CO.

In either case, however, where the algorithm can achieve adequate performance and robustness using a lower-order controller than specified with type or CO, pidtune returns a C having fewer actions than specified. For example, C can be a PI controller even though type is 'PIDF'.

Time domain:

- C has the same time domain as sys.
- If sys is a discrete-time model, C has the same sample time as sys.
- If you specify CO, C has the same Iformula and Dformula as CO. If no CO is specified, both Iformula and Dformula are Forward Euler. See the pid, pid2, pidstd, and pidstd2 reference pages for more information about Iformula and Dformula.

If you specify CO, C also obtains model properties such as InputName and OutputName from CO. For more information about model properties, see the reference pages for each type of dynamic system model.

info

Data structure containing information about performance and robustness of the tuned PID loop. The fields of info are:

- **Stable** Boolean value indicating closed-loop stability. **Stable** is 1 if the closed loop is stable, and 0 otherwise.
- CrossoverFrequency First 0 dB crossover frequency of the open-loop system C*sys, in rad/TimeUnit, where TimeUnit is the time units specified in the TimeUnit property of sys.
- PhaseMargin Phase margin of the tuned PID loop, in degrees.

If **sys** is an array of plant models, **info** is an array of data structures containing information about each tuned PID loop.

Examples

PID Controller Design at the Command Line

This example shows how to design a PID controller for the plant given by:

$$sys = \frac{1}{(s+1)^3}.$$

As a first pass, create a model of the plant and design a simple PI controller for it.

```
sys = zpk([],[-1 -1 -1],1);
[C_pi,info] = pidtune(sys,'PI')
```

```
C_pi =

Kp + Ki * ---

s

with Kp = 1.14, Ki = 0.454

Continuous-time PI controller in parallel form.

info =

Stable: 1

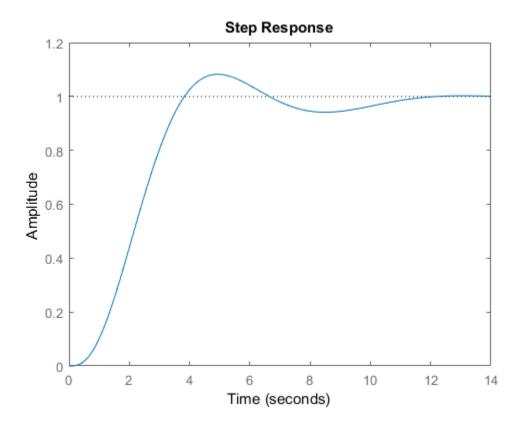
CrossoverFrequency: 0.5205

PhaseMargin: 60.0000
```

C_pi is a pid controller object that represents a PI controller. The fields of info show that the tuning algorithm chooses an open-loop crossover frequency of about 0.52 rad/s.

Examine the closed-loop step response (reference tracking) of the controlled system.

T_pi = feedback(C_pi*sys, 1); step(T_pi)



To improve the response time, you can set a higher target crossover frequency than the result that pidtune automatically selects, 0.52. Increase the crossover frequency to 1.0.

[C_pi_fast,info] = pidtune(sys,'PI',1.0)

```
C_pi_fast =

Kp + Ki * ----

s

with Kp = 2.83, Ki = 0.0495
```

```
Continuous-time PI controller in parallel form.

info =

Stable: 1

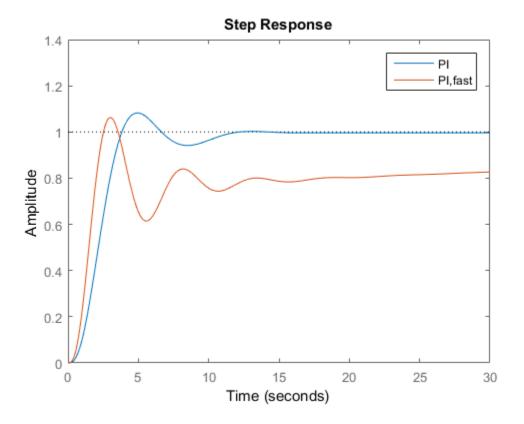
CrossoverFrequency: 1

PhaseMargin: 43.9973
```

The new controller achieves the higher crossover frequency, but at the cost of a reduced phase margin.

Compare the closed-loop step response with the two controllers.

```
T_pi_fast = feedback(C_pi_fast*sys,1);
step(T_pi,T_pi_fast)
axis([0 30 0 1.4])
legend('PI','PI,fast')
```



This reduction in performance results because the PI controller does not have enough degrees of freedom to achieve a good phase margin at a crossover frequency of 1.0 rad/s. Adding a derivative action improves the response.

Design a PIDF controller for GC with the target crossover frequency of 1.0 rad/s.

```
[C_pidf_fast,info] = pidtune(sys,'PIDF',1.0)
```

 with Kp = 2.72, Ki = 0.985, Kd = 1.72, Tf = 0.00875

Continuous-time PIDF controller in parallel form.

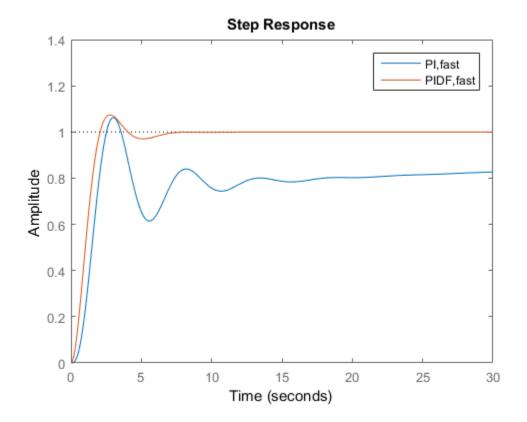
info =

```
Stable: 1
CrossoverFrequency: 1
PhaseMargin: 60.0000
```

The fields of info show that the derivative action in the controller allows the tuning algorithm to design a more aggressive controller that achieves the target crossover frequency with a good phase margin.

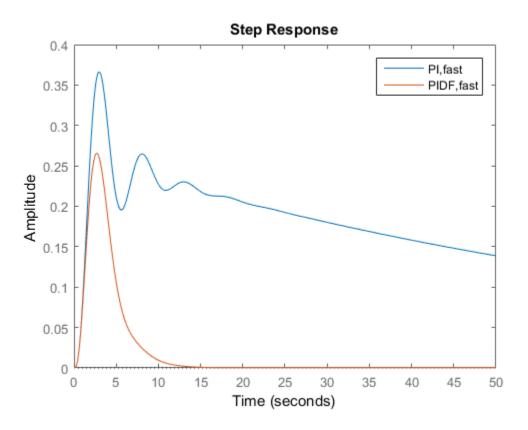
Compare the closed-loop step response and disturbance rejection for the fast PI and PIDF controllers.

```
T_pidf_fast = feedback(C_pidf_fast*sys,1);
step(T_pi_fast, T_pidf_fast);
axis([0 30 0 1.4]);
legend('PI,fast','PIDF,fast');
```



You can compare the input (load) disturbance rejection of the controlled system with the fast PI and PIDF controllers. To do so, plot the response of the closed-loop transfer function from the plant input to the plant output.

```
S_pi_fast = feedback(sys,C_pi_fast);
S_pidf_fast = feedback(sys,C_pidf_fast);
step(S_pi_fast,S_pidf_fast);
axis([0 50 0 0.4]);
legend('PI,fast','PIDF,fast');
```



This plot shows that the PIDF controller also provides faster disturbance rejection.

Design Standard-Form PID Controller

Design a PID controller in standard form for the plant defined by

$$sys = \frac{1}{\left(s+1\right)^3}.$$

To design a controller in standard form, use a standard-form controller as the CO argument to pidtune.

Specify Integrator Discretization Method

Design a discrete-time PI controller using a specified method to discretize the integrator.

If your plant is in discrete time, pidtune automatically returns a discrete-time controller using the default Forward Euler integration method. To specify a different integration method, use pid or pidstd to create a discrete-time controller having the desired integration method.

Using CO as an input causes pidtune to design a controller C of the same form, type, and discretization method as CO. The display shows that the integral term of C uses the Backward Euler integration method.

Specify a Trapezoidal integrator and compare the resulting controller.

Design 2-DOF PID Controller

Design a 2-DOF PID Controller for the plant given by the transfer function:

$$G(s) = \frac{1}{s^2 + 0.5s + 0.1}.$$

Use a target bandwidth of 1.5 rad/s.

```
wc = 1.5;
G = tf(1,[1 0.5 0.1]);
C2 = pidtune(G,'PID2',wc)
C2 =
u = Kp (b*r-y) + Ki --- (r-y) + Kd*s (c*r-y)
s
with Kp = 1.26, Ki = 0.255, Kd = 1.38, b = 0.665, c = 0
Continuous-time 2-DOF PID controller in parallel form.
```

Using the type string 'PID2' causes pidtune to generate a 2-DOF controller, represented as a pid2 object. The display confirms this result. The display also shows

that pidtune tunes all controller coefficients, including the setpoint weights **b** and **c**, to balance performance and robustness.

Alternatives

For interactive PID tuning, use the PID Tuner GUI (pidTuner). See "PID Controller Design for Fast Reference Tracking" for an example of designing a controller using the PID Tuner GUI.

The PID Tuner GUI cannot design controllers for multiple plants at once.

More About

Tips

By default, pidtune with the type input returns a pid controller in parallel form. To design a controller in standard form, use a pidstd controller as input argument CO. For more information about parallel and standard controller forms, see the pid and pidstd reference pages.

Algorithms

For information about the MathWorks $^{\circledast}$ PID tuning algorithm, see "PID Tuning Algorithm".

- "PID Controller Types for Tuning"
- "PID Tuning Algorithm"

References

Åström, K. J. and Hägglund, T. *Advanced PID Control*, Research Triangle Park, NC: Instrumentation, Systems, and Automation Society, 2006.

See Also

pid | pid2 | pidstd | pidstd2 | pidtuneOptions | pidTuner

Introduced in R2010b

pidtuneOptions

Define options for the pidtune command

Syntax

opt = pidtuneOptions
opt = pidtuneOptions(Name,Value)

Description

opt = pidtuneOptions returns the default option set for the pidtune command.

opt = pidtuneOptions(Name,Value) creates an option set with the options specified
by one or more Name,Value pair arguments.

Input Arguments

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside single quotes (' '). You can specify several name and value pair arguments in any order as Name1, Value1, ..., NameN, ValueN.

'PhaseMargin'

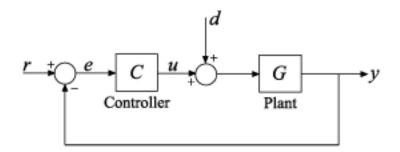
Target phase margin in degrees. pidtune attempts to design a controller such that the phase margin is at least the value specified for PhaseMargin. The selected crossover frequency could restrict the achievable phase margin. Typically, higher phase margin improves stability and overshoot, but limits bandwidth and response speed.

Default: 60

'DesignFocus'

Closed-loop performance objective to favor in the design. For a given target phase margin, pidtune chooses a controller design that balances the two measures of

performance, reference tracking and disturbance rejection. When you change the **DesignFocus** option, the tuning algorithm attempts to adjust the PID gains to favor either reference tracking or disturbance rejection while achieving the same target phase margin. In the control architecture assumed by **pidtune**, shown in the following diagram, reference tracking is the response at y to signals at r, and disturbance rejection is the suppression at y of signals at d.



The DesignFocus option can take the following values:

- 'balanced' (default) For a given robustness, tune the controller to balance reference tracking and disturbance rejection.
- 'reference-tracking' Tune the controller to favor reference tracking, if possible.
- 'disturbance-rejection' Tune the controller to favor disturbance rejection, if possible.

The more tunable parameters there are in the system, the more likely it is that the PID algorithm can achieve the desired design focus without sacrificing robustness. For example, setting the design focus is more likely to be effective for PID controllers than for P or PI controllers. In all cases, how much you can fine-tune the performance of the system depends strongly on the properties of your plant.

For an example illustrating the effect of this option, see "Tune PID Controller to Favor Reference Tracking or Disturbance Rejection (Command Line)".

Default: 'balanced'

'NumUnstablePoles'

Number of unstable poles in the plant. When your plant is a frd model or a state-space model with internal delays, you must specify the number of open-loop unstable poles (if any). Incorrect values might result in PID controllers that fail to stabilize the real plant. (pidtune ignores this option for other model types.)

Unstable poles are poles located at:

- $\operatorname{Re}(s) > 0$, for continuous-time plants
- |z| > 1, for discrete-time plants

A pure integrator in the plant (s = 0) or (|z| > 1) does not count as an unstable pole for NumUnstablePoles. If your plant is a frd model of a plant with a pure integrator, for best results, ensure that your frequency response data covers a low enough frequency to capture the integrator slope.

Default: 0

Output Arguments

opt

Object containing the specified options for pidtune.

Examples

Tune a PIDF controller with a target phase margin of 45 degrees, favoring the disturbance-rejection measure of performance.

```
sys = tf(1,[1 3 3 1]);
opts = pidtuneOptions('PhaseMargin',45,'DesignFocus','disturbance-rejection');
[C,info] = pidtune(sys,'pid',opts);
```

More About

Tips

• When using the pidtune command to design a PID controller for a plant with unstable poles, if your plant model is one of the following:

- A frd model
- A ${\tt ss}$ model with internal delays that cannot be converted to I/O delays

then use pidtuneOptions to specify the number of unstable poles in the plant.

• "PID Tuning Algorithm"

See Also

pidtune

Introduced in R2010b

pidTuner

Open PID Tuner for PID tuning

Syntax

```
pidTuner(sys,type)
pidTuner(sys,Cbase)
pidTuner(sys)
pidTuner
```

Description

pidTuner(sys,type) launches the PID Tuner GUI and designs a controller of type type for plant sys.

pidTuner(sys, Cbase) launches the GUI with a baseline controller Cbase so that you can compare performance between the designed controller and the baseline controller. If Cbase is a pid, pidstd, pid2 or pidstd2 controller object, the PID Tuner designs a controller of the same form, type, and discrete integrator formulas as Cbase.

pidTuner(sys) designs a parallel-form PI controller.

pidTuner launches the GUI with default plant of 1 and proportional (P) controller of 1.

Input Arguments

sys

Plant model for controller design. sys can be:

- Any SISO LTI system (such as ss, tf, zpk, or frd).
- Any System Identification Toolbox SISO linear model (idtf, idfrd, idgrey, idpoly, idproc, or idss).
- A continuous- or discrete-time model.
- Stable, unstable, or integrating. However, you might not be able to stabilize a plant with unstable poles under PID control.

• A model that includes any type of time delay. A plant with long time delays, however, might not achieve adequate performance under PID control.

If the plant has unstable poles, and sys is either:

- A frd model
- A ss model with internal time delays that cannot be converted to I/O delays

then you must specify the number of unstable poles in the plant. To do this, after opening

the PID Tuner GUI, in the **Plant** menu, select import. In the Import Linear System dialog box, reimport sys, specifying the number of unstable poles where prompted.

type

Controller type of the controller to design, specified as a string. The term *controller type* refers to which terms are present in the controller action. For example, a PI controller has only a proportional and an integral term, while a PIDF controller contains proportional, integrator, and filtered derivative terms. The **type** string can take the values summarized below. For more detailed information about these controller types, see "PID Controller Types for Tuning"

1-DOF Controllers

- 'P' Proportional only
- 'I' Integral only
- 'PI' Proportional and integral
- 'PD' Proportional and derivative
- PDF' Proportional and derivative with first-order filter on derivative term
- 'PID' Proportional, integral, and derivative
- <code>'PIDF'</code> Proportional, integral, and derivative with first-order filter on derivative term

2-DOF Controllers

• 'PI2' — 2-DOF proportional and integral

- 'PD2' 2-DOF proportional and derivative
- <code>'PDF2'</code> 2-DOF proportional and derivative with first-order filter on derivative term
- 'PID2' 2-DOF proportional, integral, and derivative
- <code>'PIDF2'</code> 2-DOF proportional, integral, and derivative with first-order filter on derivative term

For more information about 2-DOF PID controllers generally, see "Two-Degree-of-Freedom PID Controllers".

2-DOF Controllers with Fixed Setpoint Weights

- I PD' 2-DOF PID with b = 0, c = 0
- 'I-PDF' 2-DOF PIDF with b = 0, c = 0
- 'ID-P' 2-DOF PID with *b* = 0, *c* = 1
- ' IDF P ' 2-DOF PIDF with b = 0, c = 1
- 'PI-D' 2-DOF PID with b = 1, c = 0
- 'PI-DF' -2-DOF PIDF with b = 1, c = 0

For more detailed information about fixed-setpoint-weight 2-DOF PID controllers, see "PID Controller Types for Tuning".

Controller Form

When you use the type input, the PID Tuner designs a controller in parallel form. If you want to design a controller in standard form, Use the input Cbase instead of type, or select Standard from the **Form** menu. For more information about parallel and standard forms, see the pid and pidstd reference pages.

If **sys** is a discrete-time model with sample time **Ts**, the PID Tuner designs a discretetime **pid** controller using the **ForwardEuler** discrete integrator formula. To design a controller having a different discrete integrator formula:

• Use the input argument Cbase instead of type. PID Tuner reads controller type, form, and discrete integrator formulas from the baseline controller Cbase.

• In PID Tuner, click **Options** to open the Controller Options dialog box. Select discrete integrator formulas from the **Integral Formula** and **Derivative Formula** menus.

For more information about discrete integrator formulas, see the pid and pidstd reference pages.

Cbase

A dynamic system representing a baseline controller, permitting comparison of the performance of the designed controller to the performance of **Cbase**.

If Cbase is a pid or pidstd object, the PID Tuner also uses it to configure the type, form, and discrete integrator formulas of the designed controller. The designed controller:

- Is the type represented by Cbase.
- Is a parallel-form controller, if Cbase is a pid controller object.
- Is a standard-form controller, if Cbase is a pidstd controller object.
- Is a parallel-form 2-DOF controller, if Cbase is a pid2 controller object.
- Is a standard-form 2-DOF controller, if Cbase is a pidstd2 controller object.
- Has the same Iformula and Dformula values as Cbase. For more information about Iformula and Dformula, see the pid and pidstd reference pages .

If **Cbase** is any other dynamic system, the PID Tuner designs a parallel-form PI controller. You can change the controller form and type using the **Form** and **Type** menus after launching the PID Tuner.

Examples

Interactive PID Tuning of Parallel-Form Controller

Launch the PID Tuner to design a parallel-form PIDF controller for a discrete-time plant:

```
Gc = zpk([],[-1 -1 -1],1);
Gd = c2d(Gc,0.1); % Create discrete-time plant
pidTuner(Gd,'pidf') % Launch PID Tuner
```

Interactive PID Tuning of Standard-Form Controller Using Integrator Discretization Method

Design a standard-form PIDF controller using BackwardEuler discrete integrator formula:

```
Gc = zpk([],[-1 -1 -1],1);
Gd = c2d(Gc,0.1); % Create discrete-time plant
% Create baseline controller.
Cbase = pidstd(1,2,3,4,'Ts',0.1,...
'IFormula','BackwardEuler','DFormula','BackwardEuler')
pidTuner(Gd,Cbase) % Launch PID Tuner
```

The PID Tuner designs a controller for Gd having the same form, type, and discrete integrator formulas as Cbase. For comparison, you can display the response plots of Cbase with the response plots of the designed controller by clicking the Show baseline checkbox on the PID Tuner GUI.

Alternatives

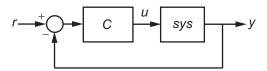
You can open PID Tuner from the MATLAB desktop, in the **Apps** tab. When you do so, use the **Plant** menu in PID Tuner to specify your plant model.

For PID tuning at the command line, use pidtune. The pidtune command can design a controller for multiple plants at once.

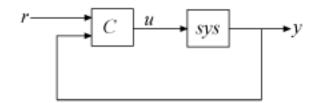
More About

Tips

• If type or Cbase specifies a one-degree-of-freedom (1-DOF) PID controller, then pidTuner designs a controller for the unit feedback loop as illustrated:



• If type or Cbase specifies a two-degree-of-freedom (2-DOF) PID controller, then pidTuner designs a 2-DOF controller as in the feedback loop of this illustration:



- The PID Tuner has a default target phase margin of 60 degrees and automatically tunes the PID gains to balance performance (response time) and robustness (stability margins). Use the **Response time** or **Bandwidth** and **Phase Margin** sliders to tune the controller's performance to your requirements. Increasing performance typically decreases robustness, and vice versa.
- Select response plots from the **Response** menu to analyze the controller's performance.
- If you provide Cbase, check Show baseline to display the response of the baseline controller.
- For more detailed information about using the PID Tuner, see "Designing PID Controllers with the PID Tuner".

Algorithms

For information about the MathWorks PID tuning algorithm, see "PID Tuning Algorithm".

- "Designing PID Controllers with the PID Tuner"
- "PID Controller Types for Tuning"

References

Åström, K. J. and Hägglund, T. *Advanced PID Control*, Research Triangle Park, NC: Instrumentation, Systems, and Automation Society, 2006.

See Also

pid | pidstd | pid2 | pidstd2 | pidtune

Introduced in R2014b

place

Pole placement design

Syntax

```
K = place(A,B,p)
[K,prec,message] = place(A,B,p)
```

Description

Given the single- or multi-input system

 $\dot{x} = Ax + Bu$

and a vector **p** of desired self-conjugate closed-loop pole locations, **place** computes a gain matrix K such that the state feedback u = -Kx places the closed-loop poles at the locations **p**. In other words, the eigenvalues of A - BK match the entries of **p** (up to the ordering).

K = place(A, B, p) places the desired closed-loop poles p by computing a state-feedback gain matrix K. All the inputs of the plant are assumed to be control inputs. The length of p must match the row size of A. place works for multi-input systems and is based on the algorithm from [1]. This algorithm uses the extra degrees of freedom to find a solution that minimizes the sensitivity of the closed-loop poles to perturbations in A or B.

[K, prec, message] = place(A, B, p) returns prec, an estimate of how closely the eigenvalues of A - BK match the specified locations p (prec measures the number of accurate decimal digits in the actual closed-loop poles). If some nonzero closed-loop pole is more than 10% off from the desired location, message contains a warning message.

You can also use place for estimator gain selection by transposing the A matrix and substituting C $^{\prime}$ for B.

1 = place(A',C',p).'

Examples

Pole Placement Design

Consider a state-space system (a,b,c,d) with two inputs, three outputs, and three states. You can compute the feedback gain matrix needed to place the closed-loop poles at $p = [-1 \ -1.23 \ -5.0]$ by

p = [-1 -1.23 -5.0]; K = place(a,b,p)

More About

Algorithms

place uses the algorithm of [1] which, for multi-input systems, optimizes the choice of eigenvectors for a robust solution.

In high-order problems, some choices of pole locations result in very large gains. The sensitivity problems attached with large gains suggest caution in the use of pole placement techniques. See [2] for results from numerical testing.

References

- [1] Kautsky, J., N.K. Nichols, and P. Van Dooren, "Robust Pole Assignment in Linear State Feedback," *International Journal of Control*, 41 (1985), pp. 1129-1155.
- [2] Laub, A.J. and M. Wette, Algorithms and Software for Pole Assignment and Observers, UCRL-15646 Rev. 1, EE Dept., Univ. of Calif., Santa Barbara, CA, Sept. 1984.

See Also

Introduced before R2006a

pole

Compute poles of dynamic system

Syntax

pole(sys)

Description

pole(sys) computes the poles p of the SISO or MIMO dynamic system model sys.

If **sys** has internal delays, poles are obtained by first setting all internal delays to zero (creating a zero-order Padé approximation) so that the system has a finite number of zeros. For some systems, setting delays to 0 creates singular algebraic loops, which result in either improper or ill-defined, zero-delay approximations. For these systems, **pole** returns an error. This error does not imply a problem with the model **sys** itself.

Limitations

Multiple poles are numerically sensitive and cannot be computed to high accuracy. A pole λ with multiplicity *m* typically gives rise to a cluster of computed poles distributed on a circle with center λ and radius of order

 $\rho \approx \varepsilon^{1/m}$

where ε is the relative machine precision (eps).

More About

Algorithms

For state-space models, the poles are the eigenvalues of the A matrix, or the generalized eigenvalues of $A - \lambda E$ in the descriptor case.

For SISO transfer functions or zero-pole-gain models, the poles are simply the denominator roots (see roots).

For MIMO transfer functions (or zero-pole-gain models), the poles are computed as the union of the poles for each SISO entry. If some columns or rows have a common denominator, the roots of this denominator are counted only once.

See Also

pzmap | zero | damp | esort | dsort

Introduced before R2006a

prescale

Optimal scaling of state-space models

Syntax

```
scaledsys = prescale(sys)
scaledsys = prescale(sys,focus)
[scaledsys,info] = prescale(...)
prescale(sys)
```

Description

scaledsys = prescale(sys) scales the entries of the state vector of a state-space
model sys to maximize the accuracy of subsequent frequency-domain analysis. The
scaled model scaledsys is equivalent to sys.

scaledsys = prescale(sys,focus) specifies a frequency interval focus =
{fmin,fmax} (in rad/TimeUnit, where TimeUnit is the system's time units specified
in the TimeUnit property of sys) over which to maximize accuracy. This is useful
when sys has a combination of slow and fast dynamics and scaling cannot achieve high
accuracy over the entire dynamic range. By default, prescale attempts to maximize
accuracy in the frequency band with dominant dynamics.

[scaledsys, info] = prescale(...) also returns a structure info with the fields shown in the following table.

SL	Left scaling factors
SR	Right scaling factors
Freqs	Frequencies used to test accuracy
RelAcc	Guaranteed relative accuracy at these frequencies

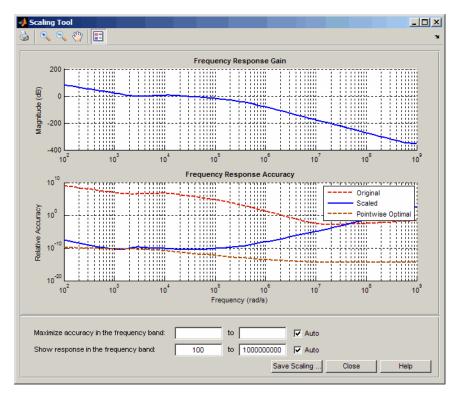
The test frequencies lie in the frequency interval ${\tt focus}$ when specified. The scaled statespace matrices are

$$\begin{split} A_s &= T_L A T_R \\ B_s &= T_L B \\ C_s &= C T_R \\ E_s &= T_L E T_R \end{split}$$

where $T_L = diag(SL)$ and $T_R = diag(SR)$. T_L and T_R are inverse of each other for explicit models (E = []).

prescale(sys) opens an interactive GUI for:

- Visualizing accuracy trade-offs for sys.
- Adjusting the frequency interval where the accuracy of sys is maximized.



For more information on scaling and using the Scaling Tool GUI, see "Scaling State-Space Models".

More About

Tips

Most frequency-domain analysis commands perform automatic scaling equivalent to scaledsys = prescale(sys).

You do not need to scale for time-domain simulations and doing so may invalidate the initial condition x0 used in initial and lsim simulations.

See Also

ss

Introduced in R2008b

pzmap

Pole-zero plot of dynamic system

Syntax

```
pzmap(sys)
pzmap(sys1,sys2,...,sysN)
[p,z] = pzmap(sys)
```

Description

pzmap(sys) creates a pole-zero plot of the continuous- or discrete-time dynamic system model sys. For SISO systems, pzmap plots the transfer function poles and zeros. For MIMO systems, it plots the system poles and transmission zeros. The poles are plotted as x's and the zeros are plotted as o's.

pzmap(sys1,sys2,...,sysN) creates the pole-zero plot of multiple models on a single figure. The models can have different numbers of inputs and outputs and can be a mix of continuous and discrete systems.

[p,z] = pzmap(sys) returns the system poles and (transmission) zeros in the column vectors p and z. No plot is drawn on the screen.

You can use the functions **sgrid** or **zgrid** to plot lines of constant damping ratio and natural frequency in the *s*- or *z*-plane.

Examples

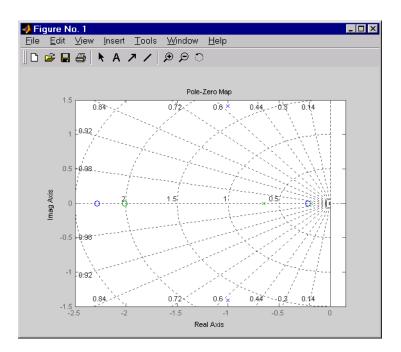
Example 1

Pole-Zero Plot of Dynamic System

Plot the poles and zeros of the continuous-time system

$$H(s) = \frac{2s^2 + 5s + 1}{s^2 + 2s + 3}$$

```
H = tf([2 5 1],[1 2 3]); sgrid
pzmap(H)
grid on
```



Example 2

Plot the pzmap for a 2-input-output discrete-time IDSS model.

A = [0.1 0; 0.2 0.9]; B = [.1 .2; 0.1 .02]; C = [10 20; 2 -5]; D = [1 2; 0 1]; sys = idss(A,B,C,D, 'Ts', 0.1);

More About

Tips

You can change the properties of your plot, for example the units. For information on the ways to change properties of your plots, see "Ways to Customize Plots".

Algorithms

pzmap uses a combination of pole and zero.

See Also

pole | sgrid | zgrid | zero | iopzmap | damp | esort | dsort | rlocus

Introduced before R2006a

pzplot

Pole-zero map of dynamic system model with plot customization options

Syntax

```
h = pzplot(sys)
pzplot(sys1,sys2,...)
pzplot(AX,...)
pzplot(..., plotoptions)
```

Description

h = pzplot(sys) computes the poles and (transmission) zeros of the dynamic system model sys and plots them in the complex plane. The poles are plotted as x's and the zeros are plotted as o's. It also returns the plot handle h. You can use this handle to customize the plot with the getoptions and setoptions commands. Type

help pzoptions

for a list of available plot options.

pzplot(sys1,sys2,...) shows the poles and zeros of multiple models sys1,sys2,... on a single plot. You can specify distinctive colors for each model, as in

pzplot(sys1,'r',sys2,'y',sys3,'g')

pzplot(AX,...) plots into the axes with handle AX.

 ${\tt pzplot(..., plotoptions)}$ plots the poles and zeros with the options specified in plotoptions. Type

help pzoptions

for more detail.

The function **sgrid** or **zgrid** can be used to plot lines of constant damping ratio and natural frequency in the *s*- or *z*-plane.

For arrays sys of dynamic system models, pzmap plots the poles and zeros of each model in the array on the same diagram.

Examples

Use the plot handle to change the color of the plot's title.

```
sys = rss(3,2,2);
h = pzplot(sys);
p = getoptions(h); % Get options for plot.
p.Title.Color = [1,0,0]; % Change title color in options.
setoptions(h,p); % Apply options to plot.
```

More About

Tips

You can change the properties of your plot, for example the units. For information on the ways to change properties of your plots, see "Ways to Customize Plots".

See Also

pzmap | setoptions | iopzplot | getoptions

Introduced before R2006a

pzoptions

Create list of pole/zero plot options

Syntax

```
P = pzoptions
P = pzoption('cstprefs')
```

Description

P = **pzoptions** returns a list of available options for pole/zero plots (pole/zero, inputoutput pole/zero and root locus) with default values set.. You can use these options to customize the pole/zero plot appearance from the command line.

P = pzoption('cstprefs') initializes the plot options with the options you selected in the Control System and System Identification Toolbox Preferences Editor. For more information about the editor, see "Toolbox Preferences Editor" in the User's Guide documentation.

Option	Description
Title, XLabel, YLabel	Label text and style
TickLabel	Tick label style
Grid	Show or hide the grid Specified as one of the following strings: 'off' 'on' Default : 'off'
GridColor	Color of the grid lines Specified as one of the following: Vector of RGB values in the range [0,1] color string 'none'. Default: [0.15,0.15,0.15]
XlimMode, YlimMode	Limit modes
Xlim, Ylim	Axes limits

This table summarizes the available pole/zero plot options.

Option	Description
IOGrouping	Grouping of input-output pairs Specified as one of the following strings: 'none' 'inputs' 'outputs' 'all' Default : 'none'
InputLabels, OutputLabels	Input and output label styles
InputVisible, OutputVisible	Visibility of input and output channels

Option	Description
FreqUnits	Frequency units, specified as one of the following strings:
	• 'Hz'
	• 'rad/second'
	• 'rpm'
	• 'kHz'
	• 'MHz'
	• 'GHz'
	 'rad/nanosecond'
	 'rad/microsecond'
	 'rad/millisecond'
	• 'rad/minute'
	• 'rad/hour'
	• 'rad/day'
	<pre>• 'rad/week'</pre>
	<pre>• 'rad/month'</pre>
	• 'rad/year'
	 'cycles/nanosecond'
	 'cycles/microsecond'
	 'cycles/millisecond'
	• 'cycles/hour'
	• 'cycles/day'
	 'cycles/week'
	 'cycles/month'
	• 'cycles/year'
	Default: 'rad/s'
	You can also specify 'auto' which uses frequency units rad/TimeUnit relative

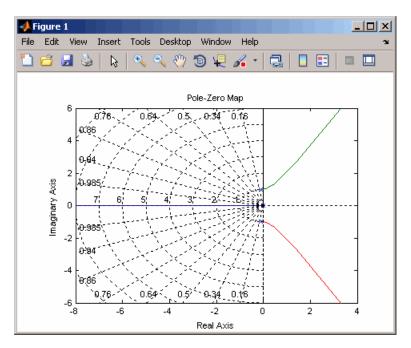
Option	Description
	to system time units specified in the TimeUnit property. For multiple systems with different time units, the units of the first system are used.
TimeUnits	Time units, specified as one of the following strings: 'nanoseconds'
	 'microseconds'
	 'milliseconds'
	• 'seconds'
	• 'minutes'
	• 'hours'
	• 'days'
	• 'weeks'
	• 'months'
	• 'years'
	Default: 'seconds'
	You can also specify 'auto' which uses time units specified in the TimeUnit property of the input system. For multiple systems with different time units, the units of the first system is used.
ConfidenceRegionNumberSD	Number of standard deviations to use when displaying the confidence region characteristic for identified models (valid only iopzplot).

Examples

In this example, you enable the grid option before creating a plot.

```
P = pzoptions; % Create set of plot options P
P.Grid = 'on'; % Set the grid to on in options
h = rlocusplot(tf(1,[1,.2,1,0]),P);
```

The following root locus plot is created with the grid enabled.



See Also

iopzplot | pzplot | setoptions | getoptions

Introduced in R2008a

realp

Real tunable parameter

Syntax

p = realp(paramname,initvalue)

Description

p = realp(paramname, initvalue) creates a tunable real-valued parameter with
name specified by the string paramname and initial value initvalue. Tunable real
parameters can be scalar- or matrix- valued.

Input Arguments

paramname

String specifying the name of the <code>realp</code> parameter p. This input argument sets the value of the Name property of p.

initvalue

Initial numeric value of the parameter p. initvalue can be a real scalar value or a 2dimensional matrix.

Output Arguments

р

realp parameter object.

Properties

Name

String containing the name of the realp parameter object. The value of Name is set by the paramname input argument to realp and cannot be changed.

Value

Value of the tunable parameter.

Value can be a real scalar value or a 2-dimensional matrix. The initial value is set by the initvalue input argument. The dimensions of Value are fixed on creation of the realp object.

Minimum

Lower bound for the parameter value. The dimension of the Minimum property matches the dimension of the Value property.

For matrix-valued parameters, use indexing to specify lower bounds on individual elements:

p = realp('K',eye(2)); p.Minimum([1 4]) = -5;

Use scalar expansion to set the same lower bound for all matrix elements:

p.Minimum = -5;

Default: - Inf for all entries

Maximum

Upper bound for the parameter value. The dimension of the Maximum property matches the dimension of the Value property.

For matrix-valued parameters, use indexing to specify upper bounds on individual elements:

p = realp('K',eye(2)); p.Maximum([1 4]) = 5;

Use scalar expansion to set the same upper bound for all matrix elements:

p.Maximum = 5;

Default: Inf for all entries

Free

Boolean value specifying whether the parameter is free to be tuned. Set the Free property to 1 (true) for tunable parameters, and 0 (false) for fixed parameters.

The dimension of the Free property matches the dimension of the Value property.

Default: 1 (true) for all entries

Examples

Tunable Low-Pass Filter

This example shows how to create the low-pass filter F = a/(s + a) with one tunable parameter *a*.

You cannot use ltiblock.tf to represent F, because the numerator and denominator coefficients of an ltiblock.tf block are independent. Instead, construct F using the tunable real parameter object realp.

1 Create a tunable real parameter.

a = realp('a',10);

The realp object **a** is a tunable parameter with initial value 10.

2 Use tf to create the tunable filter F:

F = tf(a,[1 a]);

F is a genss object which has the tunable parameter a in its Blocks property. You can connect F with other tunable or numeric models to create more complex models of control systems. For an example, see "Control System with Tunable Components".

Parametric Diagonal Matrix

This example shows how to create a parametric matrix whose off-diagonal terms are fixed to zero, and whose diagonal terms are tunable parameters.

1 Create a parametric matrix whose initial value is the identity matrix.

p = realp('P', eye(2));

p is a 2-by-2 parametric matrix. Because the initial value is the identity matrix, the off-diagonal initial values are zero.

2 Fix the values of the off-diagonal elements by setting the Free property to false.

p.Free(1,2) = false; p.Free(2,1) = false;

More About

Tips

- Use arithmetic operators (+, -, *, /, \, and ^) to combine realp objects into rational expressions or matrix expressions. You can use the resulting expressions in model-creation functions such as tf, zpk, and ss to create tunable models. For more information about tunable models, see "Models with Tunable Coefficients" in the *Control System Toolbox User's Guide*.
- "Models with Tunable Coefficients"

See Also

genss | genmat | tf | ss

Introduced in R2011a

reg

Form regulator given state-feedback and estimator gains

Syntax

```
rsys = reg(sys,K,L)
rsys = reg(sys,K,L,sensors,known,controls)
```

Description

rsys = reg(sys,K,L) forms a dynamic regulator or compensator rsys given a state-space model sys of the plant, a state-feedback gain matrix K, and an estimator gain matrix L. The gains K and L are typically designed using pole placement or LQG techniques. The function reg handles both continuous- and discrete-time cases.

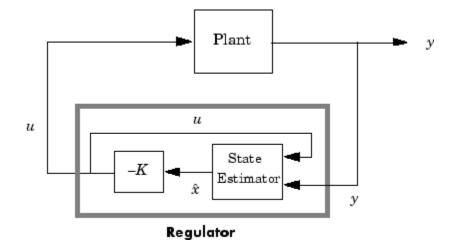
This syntax assumes that all inputs of **sys** are controls, and all outputs are measured. The regulator rsys is obtained by connecting the state-feedback law u = -Kx and the state estimator with gain matrix L (see estim). For a plant with equations

$$\dot{x} = Ax + Bu$$
$$y = Cx + Du$$

this yields the regulator

$$\dot{\hat{x}} = [A - LC - (B - LD)K]\hat{x} + Ly$$
$$u = -K\hat{x}$$

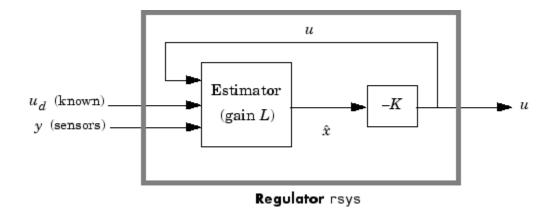
This regulator should be connected to the plant using *positive* feedback.



rsys = reg(sys,K,L,sensors,known,controls) handles more general regulation
problems where:

- The plant inputs consist of controls u, known inputs u_d , and stochastic inputs w.
- Only a subset *y* of the plant outputs is measured.

The index vectors sensors, known, and controls specify y, u_d , and u as subsets of the outputs and inputs of sys. The resulting regulator uses $[u_d; y]$ as inputs to generate the commands u (see next figure).



Examples

Given a continuous-time state-space model

```
sys = ss(A,B,C,D)
```

with seven outputs and four inputs, suppose you have designed:

- A state-feedback controller gain K using inputs 1, 2, and 4 of the plant as control inputs
- A state estimator with gain L using outputs 4, 7, and 1 of the plant as sensors, and input 3 of the plant as an additional known input

You can then connect the controller and estimator and form the complete regulation system by $% \mathcal{A}(\mathcal{A})$

```
controls = [1,2,4];
sensors = [4,7,1];
known = [3];
regulator = reg(sys,K,L,sensors,known,controls)
```

See Also

estim | kalman | lqr | dlqr | place | lqgreg

replaceBlock

Replace or update Control Design Blocks in Generalized LTI model

Syntax

```
Mnew = replaceBlock(M,Block1,Value1,...,BlockN,ValueN)
Mnew = replaceBlock(M,blockvalues)
Mnew = replaceBlock(...,mode)
```

Description

Mnew = replaceBlock(M,Block1,Value1,...,BlockN,ValueN) replaces the Control Design Blocks Block1,...,BlockN of M with the specified values Value1,...,ValueN. M is a Generalized LTI model or a Generalized matrix.

Mnew = replaceBlock(M,blockvalues) specifies the block names and replacement values as field names and values of the structure blockvalues.

Mnew = replaceBlock(...,mode) performs block replacement on an array of models
M using the substitution mode specified by the string mode.

Input Arguments

Μ

Generalized LTI model, Generalized matrix, or array of such models.

Block1,...,BlockN

Names of Control Design Blocks in M. The replaceBlock command replaces each listed block of M with the corresponding values Value1,...,ValueN that you supply.

If a specified ${\tt Block}$ is not a block of M, ${\tt replaceBlock}$ that block and the corresponding value.

Value1,...,ValueN

Replacement values for the corresponding blocks Block1,...,BlockN.

The replacement value for a block can be any value compatible with the size of the block, including a different Control Design Block, a numeric matrix, or an LTI model. If any value is [], the corresponding block is replaced by its nominal (current) value.

blockvalues

Structure specifying blocks of ${\tt M}$ to replace and the values with which to replace those blocks.

The field names of **blockvalues** match names of Control Design Blocks of M. Use the field values to specify the replacement values for the corresponding blocks of M. The replacement values may be numeric values, Numeric LTI models, Control Design Blocks, or Generalized LTI models.

mode

String specifying the block replacement mode for an input array ${\tt M}$ of Generalized matrices or LTI models.

mode can take the following values:

• '-once' (default) — Vectorized block replacement across the model array M. Each block is replaced by a single value, but the value may change from model to model across the array.

For vectorized block replacement, use a structure array for the input blockvalues, or cell arrays for the Value1,...,ValueN inputs. For example, if M is a 2-by-3 array of models:

- Mnew = replaceBlock(M,blockvalues, '-once'), where blockvalues is a 2-by-3 structure array, specifies one set of block values blockvalues(k) for each model M(:,:,k) in the array.
- Mnew = replaceBlock(M,Block,Value, '-once'), where Value is a 2-by-3 cell array, replaces Block by Value{k} in the model M(:,:,k) in the array.
- '-batch' Batch block replacement. Each block is replaced by an array of values, and the same array of values is used for each model in M. The resulting array of model Mnew is of size [size(M) Asize], where Asize is the size of the replacement value.

When the input M is a single model, '-once' and '-batch' return identical results.

Default: '-once'

Output Arguments

Mnew

Matrix or linear model or matrix where the specified blocks are replaced by the specified replacement values.

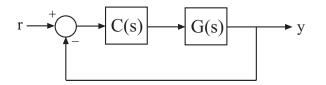
Mnew is a numeric array or numeric LTI model when all the specified replacement values are numeric values or numeric LTI models.

Examples

Replace Control Design Block with Numeric Values

This example shows how to replace a tunable PID controller (ltiblock.pid) in a Generalized LTI model by a pure gain, a numeric PI controller, or the current value of the tunable controller.

1 Create a Generalized LTI model of the following system:



where the plant $G(s) = \frac{(s-1)}{(s+1)^3}$, and *C* is a tunable PID controller.

G = zpk(1,[-1,-1,-1],1); C = ltiblock.pid('C','pid'); Try = feedback(G*C,1) **2** Replace **C** by a pure gain of 5.

T1 = replaceBlock(Try, 'C',5);

T1 is a ss model that equals feedback(G*5,1).

3 Replace C by a PI controller with proportional gain of 5 and integral gain of 0.1.

```
C2 = pid(5,0.1);
T2 = replaceBlock(Try,'C',C2);
```

T2 is a ss model that equals feedback(G*C2,1).

4 Replace C by its current (nominal) value.

```
T3 = replaceBlock(Try, 'C',[]);
```

T3 is a ss model where C has been replaced by getValue(C).

Study Parameter Variation by Sampling Tunable Model

This example shows how to sample a parametric model of a second-order filter across a grid of parameter values using replaceBlock.

Consider the second-order filter represented by:

$$F(s) = \frac{\omega_n^2}{s^2 + 2\zeta\omega_n s + \omega_n^2}$$

Sample this filter at varying values of the damping constant ζ and the natural frequency ω_n . Create a parametric model of the filter by using tunable elements for ζ and ω_n .

```
wn = realp('wn',3);
zeta = realp('zeta',0.8);
F = tf(wn^2,[1 2*zeta*wn wn^2])
F =
Generalized continuous-time state-space model with 1 outputs, 1 inputs, 2 states, and
wn: Scalar parameter, 5 occurrences.
zeta: Scalar parameter, 1 occurrences.
```

Type "ss(F)" to see the current value, "get(F)" to see all properties, and "F.Blocks"

F is a genss model with two tunable Control Design Blocks, the realp blocks wn and zeta. The blocks wn and zeta have initial values of 3 and 0.8, respectively.

Sample F over a 2-by-3 grid of (wn, zeta) values.

```
wnvals = [3;5];
zetavals = [0.6 0.8 1.0];
[wngrid,zetagrid] = ndgrid(wnvals,zetavals);
Fsample = replaceBlock(F,'wn',wngrid,'zeta',zetagrid);
```

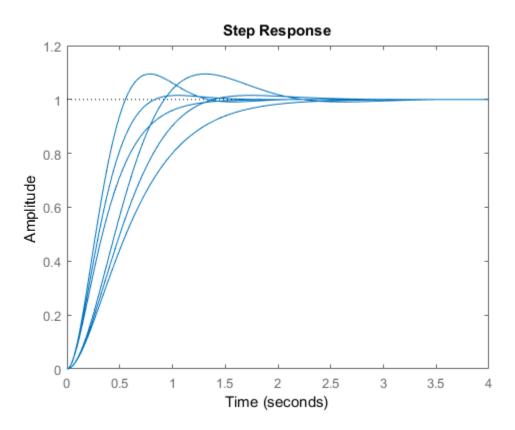
The ndgrid command produces a full 2-by-3 grid of parameter combinations. Fsample is a 2-by-3 array of state-space models. Each entry in the array is a state-space model that represents F evaluated at the corresponding (wn, zeta) pair. For example, Fsample(:,:,2,3) has wn = 5 and zeta = 1.0.

Set the SamplingGrid property of the model array to help keep track of which set of parameter values corresponds to which entry in the array. To do so, create a grid of parameter values that matches the dimensions of the array. Then, assign these values to Fsample.SamplingGrid in a structure with the parameter names.

```
Fsample.SamplingGrid = struct('wn',wngrid,'zeta',zetagrid);
```

When you display Fsample, the parameter values in Fsample.SamplingGrid are displayed along with the each transfer function in the array. The parameter information is also available in response plots. For instance, examine the step response of Fsample.

stepplot(Fsample)



The step response plots show the variation in the natural frequency and damping constant across the six models in the array. When you click on one of the responses in the plot, the datatip includes the wn and zeta values as specified in Fsample.SamplingGrid.

More About

Tips

• Use replaceBlock to perform parameter studies by sampling Generalized LTI models across a grid of parameters, or to evaluate tunable models for specific values of the tunable blocks. See "Examples" on page 1-722.

- "Generalized Matrices"
- "Generalized and Uncertain LTI Models"
- "Models with Tunable Coefficients"

See Also

getValue | genss | genmat | nblocks

Introduced in R2011a

repsys

Replicate and tile models

Syntax

```
rsys = repsys(sys,[M N])
rsys = repsys(sys,N)
rsys = repsys(sys,[M N S1,...,Sk])
```

Description

rsys = repsys(sys,[M N]) replicates the model sys into an M-by-N tiling pattern. The resulting model rsys has size(sys,1)*M outputs and size(sys,2)*N inputs.

```
rsys = repsys(sys,N) creates an N-by-N tiling.
```

rsys = repsys(sys,[M N S1,...,Sk]) replicates and tiles sys along both I/O and array dimensions to produce a model array. The indices S specify the array dimensions. The size of the array is [size(sys,1)*M, size(sys,2)*N, size(sys,3)*S1, ...].

Input Arguments

sys

Model to replicate.

М

Number of replications of sys along the output dimension.

Ν

Number of replications of sys along the input dimension.

S

Numbers of replications of sys along array dimensions.

Output Arguments

rsys

Model having size(sys, 1) *M outputs and size(sys, 2) *N inputs.

If you provide array dimensions S1,...,Sk, rsys is an array of dynamic systems which each have size(sys,1)*M outputs and size(sys,2)*N inputs. The size of rsys is [size(sys,1)*M, size(sys,2)*N, size(sys,3)*S1, ...].

Examples

Replicate a SISO transfer function to create a MIMO transfer function that has three inputs and two outputs.

sys = tf(2,[1 3]);
rsys = repsys(sys,[2 3]);

The preceding commands produce the same result as:

sys = tf(2,[1 3]); rsys = [sys sys sys; sys sys sys];

Replicate a SISO transfer function into a 3-by-4 array of two-input, one-output transfer functions.

```
sys = tf(2,[1 3]);
rsys = repsys(sys, [1 2 3 4]);
```

To check the size of rsys, enter:

size(rsys)

This command produces the result:

3x4 array of transfer functions. Each model has 1 outputs and 2 inputs.

More About

Tips

rsys = repsys(sys,N) produces the same result as rsys = repsys(sys,[N N]). To produce a diagonal tiling, use rsys = sys*eye(N).

See Also

append

Introduced in R2010b

reshape

Change shape of model array

Syntax

```
sys = reshape(sys,s1,s2,...,sk)
sys = reshape(sys,[s1 s2 ... sk])
```

Description

sys = reshape(sys,s1,s2,...,sk) (or, equivalently, sys = reshape(sys,[s1 s2 ... sk])) reshapes the LTI array sys into an s1-by-s2-by-...-by-sk model array. With either syntax, there must be s1*s2*...*sk models in sys to begin with.

Examples

Change the shape of a model array from 2x3 to 6x1.

```
% Create a 2x3 model array.
sys = rss(4,1,1,2,3);
% Confirm the size of the array.
size(sys)
```

This input produces the following output:

2x3 array of state-space models Each model has 1 output, 1 input, and 4 states.

Change the shape of the array.

```
sys1 = reshape(sys,6,1);
size(sys1)
```

This input produces the following output:

6x1 array of state-space models Each model has 1 output, 1 input, and 4 states.

See Also size | ndims

rlocus

Root locus plot of dynamic system

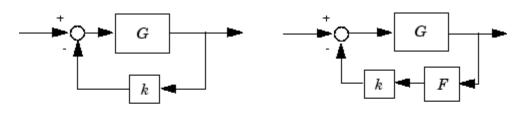
Syntax

```
rlocus(sys)
rlocus(sys1,sys2,...)
[r,k] = rlocus(sys)
r = rlocus(sys,k)
```

Description

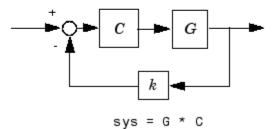
rlocus computes the root locus of a SISO open-loop model. The root locus gives the closed-loop pole trajectories as a function of the feedback gain k (assuming negative feedback). Root loci are used to study the effects of varying feedback gains on closed-loop pole locations. In turn, these locations provide indirect information on the time and frequency responses.

rlocus(sys) calculates and plots the root locus of the open-loop SISO model sys. This function can be applied to any of the following *negative* feedback loops by setting sys appropriately.



sys = G

sys = F * G



If sys has transfer function

$$h(s) = \frac{n(s)}{d(s)}$$

the closed-loop poles are the roots of

$$d(s) + kn(s) = 0$$

rlocus adaptively selects a set of positive gains k to produce a smooth plot. Alternatively,

rlocus(sys,k)

uses the user-specified vector ${\sf k}$ of gains to plot the root locus.

rlocus(sys1,sys2,...) draws the root loci of multiple LTI models sys1, sys2,... on a single plot. You can specify a color, line style, and marker for each model, as in

rlocus(sys1,'r',sys2,'y:',sys3,'gx').

[r,k] = rlocus(sys) and r = rlocus(sys,k) return the vector k of selected gains and the complex root locations r for these gains. The matrix r has length(k) columns and its jth column lists the closed-loop roots for the gain k(j).

Examples

Root Locus Plot of Dynamic System

Plot the root-locus of the following system.

$$h(s) = \frac{2s^2 + 5s + 1}{s^2 + 2s + 3}.$$

h = tf([2 5 1],[1 2 3]);
rlocus(h)

Root Locus 1.5 1 Imaginary Axis (seconds⁻¹) 0.5 0 -0.5 -1 -1.5 [∟] -2.5 -2 -1.5 -1 -0.5 0.5 0 Real Axis (seconds⁻¹)

You can use the right-click menu for rlocus to add grid lines, zoom in or out, and invoke the Property Editor to customize the plot. Also, click anywhere on the curve to activate a data marker that displays the gain value, pole, damping, overshoot, and frequency at the selected point.

More About

Tips

You can change the properties of your plot, for example the units. For information on the ways to change properties of your plots, see "Ways to Customize Plots".

See Also pole | pzmap

rlocusplot

Plot root locus and return plot handle

Syntax

```
h = rlocusplot(sys)
rlocusplot(sys,k)
rlocusplot(sys1,sys2,...)
rlocusplot(AX,...)
rlocusplot(..., plotoptions)
```

Description

h = rlocusplot(sys) computes and plots the root locus of the single-input, singleoutput LTI model sys. It also returns the plot handle h. You can use this handle to customize the plot with the getoptions and setoptions commands. Type

help pzoptions

for a list of available plot options.

See **rlocus** for a discussion of the feedback structure and algorithms used to calculate the root locus.

rlocusplot(sys,k) uses a user-specified vector k of gain values.

```
rlocusplot(sys1,sys2,...) draws the root loci of multiple LTI models sys1,
sys2,... on a single plot. You can specify a color, line style, and marker for each model, as
in
```

```
rlocusplot(sys1,'r',sys2,'y:',sys3,'gx')
```

rlocusplot(AX,...) plots into the axes with handle AX.

rlocusplot(..., plotoptions) plots the root locus with the options specified in
plotoptions. Type

help pzoptions

for more details.

Examples

Use the plot handle to change the title of the plot.

```
sys = rss(3);
h = rlocusplot(sys);
p = getoptions(h); % Get options for plot.
p.Title.String = 'My Title'; % Change title in options.
setoptions(h,p); % Apply options to plot.
```

More About

Tips

You can change the properties of your plot, for example the units. For information on the ways to change properties of your plots, see "Ways to Customize Plots".

See Also

getoptions | rlocus | pzoptions | setoptions

rss

Generate random continuous test model

Syntax

rss(n) rss(n,p) rss(n,p,m,s1,...,sn)

Description

rss(n) generates an n-th order model with one input and one output and returns the model in the state-space object sys. The poles of sys are random and stable with the possible exception of poles at s = 0 (integrators).

rss(n,p) generates an nth order model with one input and p outputs, and rss(n,p,m) generates an n-th order model with m inputs and p outputs. The output sys is always a state-space model.

rss(n,p,m,s1,...,sn) generates an s1-by-...-by-sn array of n-th order state-space models with m inputs and p outputs.

Use tf, frd, or zpk to convert the state-space object sys to transfer function, frequency response, or zero-pole-gain form.

Examples

Obtain a random continuous LTI model with three states, two inputs, and two outputs by typing

sys = rss(3, 2, 2)a = x1 х2 xЗ -0.541750.09729 0.08304 x1 0.09729 -0.89491 0.58707 х2 0.08304 0.58707 -1.95271хЗ

b =

	x1 x2 x3	u1 -0.88844 0 -0.07162	u2 -2.41459 -0.69435 -1.39139	
с =				
		x1	x2	x3
	y1	0.32965	0.14718	0
	у2	0.59854	-0.10144	0.02805
d =				
		u1	u2	
	y1	-0.87631	-0.32758	
	у2	0	0	

Continuous-time system.

See Also

drss | frd | tf | zpk

series

Series connection of two models

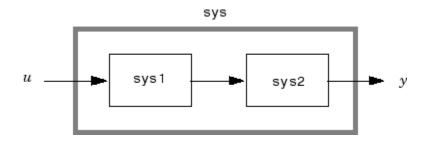
Syntax

```
series
sys = series(sys1,sys2)
sys = series(sys1,sys2,outputs1,inputs2)
```

Description

series connects two model objects in series. This function accepts any type of model. The two systems must be either both continuous or both discrete with identical sample time. Static gains are neutral and can be specified as regular matrices.

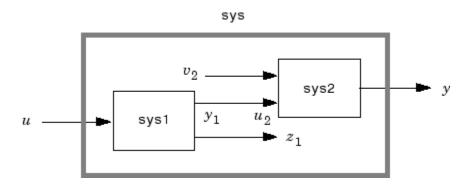
sys = series(sys1,sys2) forms the basic series connection shown below.



This command is equivalent to the direct multiplication

sys = sys2 * sys1

sys = series(sys1,sys2,outputs1,inputs2) forms the more general series
connection.



The index vectors outputs1 and inputs2 indicate which outputs y_1 of sys1 and which inputs u_2 of sys2 should be connected. The resulting model sys has u as input and y as output.

Examples

Consider a state-space system **sys1** with five inputs and four outputs and another system **sys2** with two inputs and three outputs. Connect the two systems in series by connecting outputs 2 and 4 of **sys1** with inputs 1 and 2 of **sys2**.

outputs1 = [2 4]; inputs2 = [1 2]; sys = series(sys1,sys2,outputs1,inputs2)

See Also

append | feedback | parallel

set

Set or modify model properties

Syntax

```
set(sys,'Property',Value)
set(sys,'Property1',Value1,'Property2',Value2,...)
sysnew = set(____)
set(sys,'Property')
```

Description

set is used to set or modify the properties of a dynamic system model. Like its Handle Graphics[®] counterpart, **set** uses property name/property value pairs to update property values.

set(sys, 'Property', Value) assigns the value Value to the property of the model sys specified by the string 'Property'. This string can be the full property name (for example, 'UserData') or any unambiguous case-insensitive abbreviation (for example, 'user'). The specified property must be compatible with the model type. For example, if sys is a transfer function, Variable is a valid property but StateName is not. For a complete list of available system properties for any linear model type, see the reference page for that model type. This syntax is equivalent to sys.Property = Value.

set(sys, 'Property1', Value1, 'Property2', Value2,...) sets multiple property
values with a single statement. Each property name/property value pair updates one
particular property.

sysnew = set(____) returns the modified dynamic system model, and can be used with any of the previous syntaxes.

set(sys, 'Property') displays help for the property specified by 'Property'.

Examples

Consider the SISO state-space model created by

sys = ss(1,2,3,4);

You can add an input delay of 0.1 second, label the input as torque, reset the *D* matrix to zero, and store its DC gain in the 'Userdata' property by

```
set(sys,'inputd',0.1,'inputn','torque','d',0,'user',dcgain(sys))
```

Note that **set** does not require any output argument. Check the result with **get** by typing

get(sys)

```
a: 1
            b: 2
            c: 3
            d: 0
            e: []
    StateName: {''}
InternalDelay: [0x1 double]
           Ts: 0
   InputDelay: 0.1
  OutputDelay: 0
    InputName: {'torque'}
   OutputName: {''}
   InputGroup: [1x1 struct]
  OutputGroup: [1x1 struct]
         Name: ''
        Notes: {}
     UserData: -2
```

More About

Tips

For discrete-time transfer functions, the convention used to represent the numerator and denominator depends on the choice of variable (see tf for details). Like tf, the syntax for set changes to remain consistent with the choice of variable. For example, if the Variable property is set to 'z' (the default),

set(h, 'num', [1 2], 'den', [1 3 4])

produces the transfer function

$$h\left(z\right) = \frac{z+2}{z^2+3z+4}$$

However, if you change the Variable to $'z^-1'$ by

set(h,'Variable','z^-1'),

the same command

set(h, 'num', [1 2], 'den', [1 3 4])

now interprets the row vectors $[1 \ 2]$ and $[1 \ 3 \ 4]$ as the polynomials $1 + 2z^{-1}$ and $1 + 3z^{-1} + 4z^{-2}$ and produces:

$$\bar{h}\left(z^{-1}\right) = \frac{1 + 2z^{-1}}{1 + 3z^{-1} + 4z^{-2}} = zh\left(z\right)$$

Note Because the resulting transfer functions are different, make sure to use the convention consistent with your choice of variable.

• "What Are Model Objects?"

See Also

get | frd | ss | tf | zpk

setDelayModel

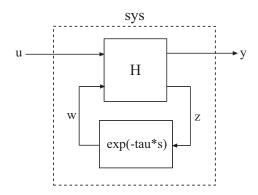
Construct state-space model with internal delays

Syntax

```
sys = setDelayModel(H,tau)
sys = setDelayModel(A,B1,B2,C1,C2,D11,D12,D21,D22,tau)
```

Description

sys = setDelayModel(H,tau) constructs the state-space model sys obtained by LFT interconnection of the state-space model H with the vector of internal delays tau, as shown:



sys = setDelayModel(A,B1,B2,C1,C2,D11,D12,D21,D22,tau) constructs the state-space model sys described by the following equations:

$$\begin{aligned} \frac{dx(t)}{dt} &= Ax(t) + B_1 u(t) + B_2 w(t) \\ y(t) &= C_1 x(t) + D_{11} u(t) + D_{12} w(t) \\ z(t) &= C_2 x(t) + D_{21} u(t) + D_{22} w(t) \\ w(t) &= z(t - \tau). \end{aligned}$$

tau (τ) is the vector of internal delays in sys.

Input Arguments

H

State-space (ss) model to interconnect with internal delays tau.

tau

Vector of internal delays of sys.

For continuous-time models, express tau in seconds.

For discrete-time models, express $\verb"tau"$ as integer values that represent multiples of the sample time.

A, B1, B2, C1, C2, D11, D12, D21, D22

Set of state-space matrices that, with the internal delay vector tau, explicitly describe the state-space model sys.

Output Arguments

sys

State-space (ss) model with internal delays tau.

More About

Tips

- **setDelayModel** is an advanced operation and is not the natural way to construct models with internal delays. See "Time Delays in Linear Systems" for recommended ways of creating internal delays.
- The syntax sys = setDelayModel(A,B1,B2,C1,C2,D11,D12,D21,D22,tau) constructs a continuous-time model. You can construct the discrete-time model described by the state-space equations

$$\begin{aligned} x[k+1] &= Ax[k] + B_1 u[k] + B_2 w[k] \\ y[k] &= C_1 x[k] + D_{11} u[k] + D_{12} w[k] \\ z[k] &= C_2 x[k] + D_{21} u[k] + D_{22} w[k] \\ w[k] &= z[k-\tau]. \end{aligned}$$

To do so, first construct SyS using SyS = setDelayModel(A,B1,B2,C1,C2,D11,D12,D21,D22,tau). Then, use SyS.TS to set the sample time.

- "Internal Delays"
- "Time Delays in Linear Systems"

See Also

getDelayModel | lft | ss

Introduced in R2007a

setoptions

Set plot options for response plot

Syntax

```
setoptions(h, PlotOpts)
setoptions(h, 'Property1', 'value1', ...)
setoptions(h, PlotOpts, 'Property1', 'value1', ...)
```

Description

setoptions(h, PlotOpts) sets preferences for response plot using the plot handle. h
is the plot handle, PlotOpts is a plot options handle containing information about plot
options.

There are two ways to create a plot options handle:

• Use getoptions, which accepts a plot handle and returns a plot options handle.

p = getoptions(h)

- · Create a default plot options handle using one of the following commands:
 - bodeoptions Bode plots
 - hsvoptions Hankel singular values plots
 - nicholsoptions Nichols plots
 - nyquistoptions Nyquist plots
 - pzoptions Pole/zero plots
 - sigmaoptions Sigma plots
 - timeoptions Time plots (step, initial, impulse, etc.)

For example,

p = bodeoptions

returns a plot options handle for Bode plots.

setoptions(h, 'Property1', 'value1', ...) assigns values to property pairs
instead of using PlotOpts. To find out what properties and values are available for a
particular plot, type help <function>options. For example, for Bode plots type

help bodeoptions

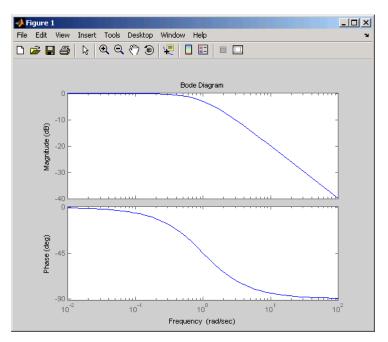
For a list of the properties and values available for each plot type, see "Properties and Values Reference".

setoptions(h, PlotOpts, 'Property1', 'value1', ...) first assigns plot properties as defined in @PlotOptions, and then overrides any properties governed by the specified property/value pairs.

Examples

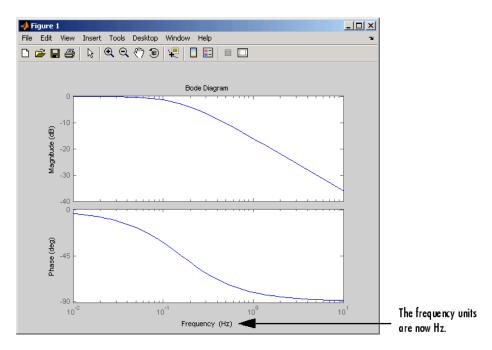
To change frequency units, first create a Bode plot.

```
sys=tf(1,[1 1]);
h=bodeplot(sys) % Create a Bode plot with plot handle h.
```



Now, change the frequency units from rad/s to Hz.

p=getoptions(h); % Create a plot options handle p. p.FreqUnits = 'Hz'; % Modify frequency units. setoptions(h,p); % Apply plot options to the Bode plot and % render.



To change the frequency units using property/value pairs, use this code.

```
sys=tf(1,[1 1]);
h=bodeplot(sys);
setoptions(h,'FreqUnits','Hz');
```

The result is the same as the first example.

See Also

getoptions

setBlockValue

Modify value of Control Design Block in Generalized Model

Syntax

```
M = setBlockValue(MO,blockname,val)
M = setBlockValue(MO,blockvalues)
M = setBlockValue(MO,Mref)
```

Description

M = setBlockValue(MO,blockname,val) modifies the current or nominal value of the Control Design Block blockname in the Generalized Model MO to the value specified by val.

M = setBlockValue(MO,blockvalues) modifies the value of several Control Design Blocks at once. The structure blockvalues specifies the blocks and replacement values. Blocks of MO not listed in blockvalues are unchanged.

M = setBlockValue(MO,Mref) takes replacement values from Control Design blocks in the Generalized Model Mref. This syntax modifies the Control Design Blocks in MO to match the current values of all corresponding blocks in Mref.

Use this syntax to propagate block values, such as tuned parameter values, from one parametric model to other models that depend on the same parameters.

Input Arguments

MO

Generalized Model containing the blocks whose current or nominal value is modified to val. For the syntax M = setBlockValue(MO,Mref) MO can be a single Control Design Block whose value is modified to match the value of the corresponding block in Mref.

blockname

Name of the Control Design Block in the model ${\tt MO}$ whose current or nominal value is modified.

To get a list of the Control Design Blocks in MO, enter MO.Blocks.

val

Replacement value for the current or nominal value of the Control Design Block, blockname. The value val can be any value that is compatible with blockname without changing the size, type, or sample time of blockname.

For example, you can set the value of a tunable PID block (ltiblock.pid) to a pid controller model, or to a transfer function (tf) model that represents a PID controller.

blockvalues

Structure specifying Control Design Blocks of MO to modify, and the corresponding replacement values. The fields of the structure are the names of the blocks to modify. The value of each field specifies the replacement current or nominal value for the corresponding block.

Mref

Generalized Model that shares some Control Design Blocks with MO. The values of these blocks in Mref are used to update their counterparts in MO.

Output Arguments

Μ

Generalized Model obtained from MO by updating the values of the specified blocks.

Examples

Update Controller Model with Tuned Values

Propagate the values of tuned parameters to other Control Design Blocks.

You can use the Robust Control Toolbox tuning commands such as **systune**, **looptune**, or **hinfstruct** to tune blocks in a closed-loop model of a control system. If you do so,

the tuned controller parameters are embedded in a Generalized LTI Model. You can use setBlockValue to propagate those parameters to a controller model.

Create a tunable model of the closed-loop response of a control system, and tune the parameters using hinfstruct.

```
G = tf([1,0.0007],[1,0.00034,0.00086]);
Cpi = ltiblock.pid('Cpi','pi');
a = realp('a',10);
F0 = tf(a,[1 a]);
C0 = Cpi*F0;
T0 = feedback(G*C0,1);
```

```
T = hinfstruct(T0);
```

The controller model C0 is a Generalized LTI model with two tunable blocks, Cpi and a. The closed-loop model T0 is also a Generalized LTI model with the same blocks. The model T contains the tuned values of these blocks.

Propagate the tuned values of the controller in T to the controller model CO.

```
C = setBlockValue(CO,T)
C =
Generalized continuous-time state-space model with 1 outputs,
1 inputs, 2 states, and the following blocks:
    Cpi: Parametric PID controller, 1 occurrences.
    a: Scalar parameter, 2 occurrences.
Type "ss(C)" to see the current value, "get(C)" to see all properties,
and "C.Blocks" to interact with the blocks.
```

C is still a Generalized model. The current value of the Control Design Blocks in C are set to the values the corresponding blocks of T.

Obtain a Numeric LTI model of the controller with the tuned values using getValue.

```
CVal = getValue(CO,T);
```

This command returns a numerical state-space model of the tuned controller.

See Also

```
getValue | getBlockValue | showBlockValue | genss | systume | looptume |
hinfstruct
```

Introduced in R2011b

setValue

Modify current value of Control Design Block

Syntax

```
blk = setValue(blk0,val)
```

Description

blk = setValue(blk0,val) modifies the parameter values in the tunable Control Design Block, blk0, to best match the values specified by val. An exact match can only occur when val is compatible with the structure of blk0.

Input Arguments

blk0

Control Design Block whose value is modified.

val

Specifies the replacement parameters values for blk0. The value val can be any value that is compatible with blk0 without changing the size, type, or sample time of blk0. For example, if blk0 is a ltiblock.pid block, valid types for val include ltiblock.pid, a numeric pid controller model, or a numeric tf model that represents a PID controller. setValue uses the parameter values of val to set the current value of blockname.

Output Arguments

blk

Control Design Block of the same type as blk0, whose parameters are updated to best match the parameters of val.

See Also getValue | setBlockValue | getBlockValue

Introduced in R2011b

sgrid

Generate s-plane grid of constant damping factors and natural frequencies

Syntax

sgrid sgrid(z,wn)

Description

sgrid generates, for pole-zero and root locus plots, a grid of constant damping factors from zero to one in steps of 0.1 and natural frequencies from zero to 10 rad/sec in steps of one rad/sec, and plots the grid over the current axis. If the current axis contains a continuous *s*-plane root locus diagram or pole-zero map, **sgrid** draws the grid over the plot.

sgrid(z,wn) plots a grid of constant damping factor and natural frequency lines for the damping factors and natural frequencies in the vectors z and wn, respectively. If the current axis contains a continuous *s*-plane root locus diagram or pole-zero map, sgrid(z,wn) draws the grid over the plot.

Alternatively, you can select **Grid** from the right-click menu to generate the same splane grid.

Examples

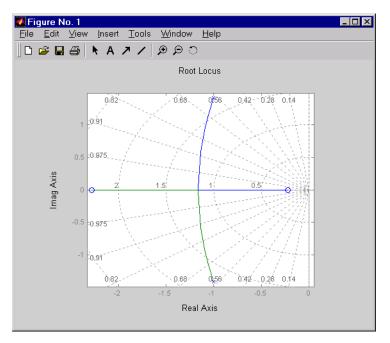
Plot s-plane grid lines on the root locus for the following system.

$$H(s) = \frac{2s^2 + 5s + 1}{s^2 + 2s + 3}$$

You can do this by typing

H = tf([2 5 1],[1 2 3]) Transfer function:

```
2 s^2 + 5 s + 1
s^2 + 2 s + 3
rlocus(H)
sgrid
```



See Also zgrid | pzmap | rlocus

Introduced before R2006a

showBlockValue

Display current value of Control Design Blocks in Generalized Model

Syntax

showBlockValue(M)

Description

showBlockValue(M) displays the current values of all Control Design Blocks in the Generalized Model, M. (For uncertain blocks, the "current value" is the nominal value of the block.)

Input Arguments

М

Generalized Model.

Examples

Create a tunable genss model, and display the current value of its tunable elements.

```
G = zpk([],[-1,-1],1);
C = ltiblock.pid('C','PID');
a = realp('a',10);
F = tf(a,[1 a]);
T = feedback(G*C,1)*F;
showBlockValue(T)
C =
Continuous-time I-only controller:
1
```

Ki * --s With Ki = 0.001 a = 10

More About

Tips

- Displaying the current values of a model is useful, for example, after you have tuned the free parameters of the model using a Robust Control Toolbox tuning command such as looptune.
- **showBlockValue** displays the current values of all Control Design Blocks in a model, including tunable, uncertain, and switch blocks. To display the current values of only the tunable blocks, use **showTunable**.

See Also

genss | getBlockValue | setBlockValue | showTunable

Introduced in R2011b

showTunable

Display current value of tunable Control Design Blocks in Generalized Model

Syntax

showTunable(M)

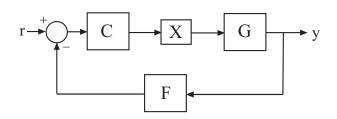
Description

showTunable(M) displays the current values of all tunable Control Design Blocks in a generalized LTI model. Tunable control design blocks are parametric blocks such as realp, ltiblock.tf, and ltiblock.pid.

Examples

Display Block Values of Tuned Control System Model

Tune the following control system using **systune**, and display the values of the tunable blocks.



The control structure includes a PI controller ${\tt C}$ and a tunable low-pass filter in the feedback path. The plant ${\tt G}$ is a third-order system.

Create models of the system components and connect them together to create a tunable closed-loop model of the control system.

```
s = tf('s');
num = 33000*(s^2 - 200*s + 90000);
den = (s + 12.5)*(s^2 + 25*s + 63000);
G = num/den;
C0 = ltiblock.pid('C','pi');
a = realp('a',1);
F0 = tf(a,[1 a]);
X = AnalysisPoint('X');
T0 = feedback(G*X*C0,F0);
T0.InputName = 'r';
T0.OutputName = 'y';
```

TO is a genss model that has two tunable blocks, the PI controller, C, and the parameter, a. TO also contains the switch block X.

Create a tuning requirement that forces the output y to track the input r, and tune the system to meet that requirement.

```
Req = TuningGoal.Tracking('r','y',0.05);
[T,fSoft,~] = systume(T0,Req);
```

systume finds values for the tunable parameters that optimally meet the tracking requirement. The output T is a genss model with the same Control Design Blocks as TO. The current values of those blocks are the tuned values.

Examine the tuned values of the tunable blocks of the control system.

a = 68.6

showTunable displays the values of the tunable blocks only. If you use showBlockValue instead, the display also includes the switch block X.

Input Arguments

M — Input model generalized LTI model

Input model of which to display tunable block values, specified as a generalized LTI model such as a **genss** model.

More About

Tips

- Displaying the current values of tunable blocks is useful, for example, after you have tuned the free parameters of the model using a Robust Control Toolbox tuning command such as systume.
- **showTunable** displays the current values of the tunable blocks only. To display the current values of all Control Design Blocks in a model, including tunable, uncertain, and switch blocks, use **showBlockValue**.
- "Generalized Models"
- "Control Design Blocks"

See Also

genss | getBlockValue | setBlockValue | showBlockValue | systune

Introduced in R2012b

sigma

Singular values plot of dynamic system

Syntax

```
sigma(sys)
sigma(sys,w)
sigma(sys,[],type)
sigma(sys,w,type)
sigma(sys1,sys2,...,sysN,w,type)
sigma(sys1,'PlotStyle1',...,sysN,'PlotStyleN',w,type)
sv = sigma(sys,w)
[sv,w] = sigma(sys)
```

Description

sigma calculates the singular values of the frequency response of a dynamic system sys. For an FRD model, sigma computes the singular values of sys.Response at the frequencies, sys.frequency. For continuous-time TF, SS, or ZPK models with transfer function H(s), sigma computes the singular values of $H(j\omega)$ as a function of the frequency ω . For discrete-time TF, SS, or ZPK models with transfer function H(z) and sample time T_s , sigma computes the singular values of

 $H(e^{j\omega T_s})$

for frequencies ω between 0 and the Nyquist frequency $\omega_N = \pi/T_s$.

The singular values of the frequency response extend the Bode magnitude response for MIMO systems and are useful in robustness analysis. The singular value response of a SISO system is identical to its Bode magnitude response. When invoked without output arguments, sigma produces a singular value plot on the screen.

sigma(sys) plots the singular values of the frequency response of a model sys. This
model can be continuous or discrete, and SISO or MIMO. The frequency points are
chosen automatically based on the system poles and zeros, or from sys.frequency if
sys is an FRD.

sigma(sys,w) explicitly specifies the frequency range or frequency points to be used for the plot. To focus on a particular frequency interval [wmin,wmax], set w = {wmin,wmax}. To use particular frequency points, set w to the corresponding vector of frequencies. Use logspace to generate logarithmically spaced frequency vectors. Frequencies must be in rad/TimeUnit, where TimeUnit is the time units of the input dynamic system, specified in the TimeUnit property of sys.

sigma(sys,[],type) or sigma(sys,w,type) plots the following modified singular value responses:

	Singular values of the frequency response H^{-1} , where H is the frequency response of sys.	
type = 2	2 Singular values of the frequency response $I + H$.	
type = 3	= 3 Singular values of the frequency response $I + H^{-1}$.	

These options are available only for square systems, that is, with the same number of inputs and outputs.

sigma(sys1,sys2,...,sysN,w,type) plots the singular value plots of several LTI models on a single figure. The arguments w and type are optional. The models sys1,sys2,...,sysN need not have the same number of inputs and outputs. Each model can be either continuous- or discrete-time.

sigma(sys1, 'PlotStyle1',...,sysN, 'PlotStyleN',w,type) specifies a
distinctive color, linestyle, and/or marker for each system plot. See bode for an example.

sv = sigma(sys,w) and [sv,w] = sigma(sys) return the singular values sv of the frequency response at the frequencies w. For a system with Nu input and Ny outputs, the array sv has min(Nu, Ny) rows and as many columns as frequency points (length of w). The singular values at the frequency w(k) are given by sv(:,k).

Examples

Compute and Plot Singular Values

Consider the following two-input, two-output dynamic system.

$$H(s) = \begin{bmatrix} 0 & \frac{3s}{s^2 + s + 10} \\ \frac{s+1}{s+5} & \frac{2}{s+6} \end{bmatrix}.$$

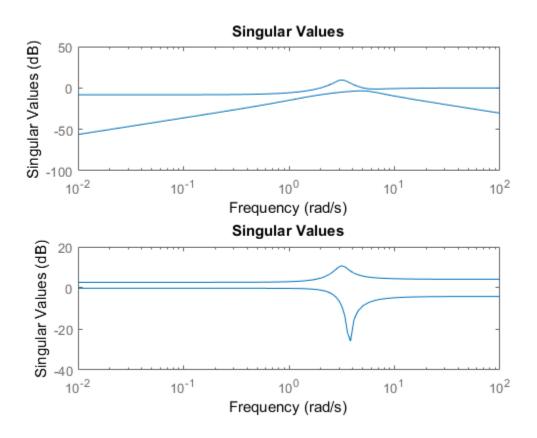
Compute the singular value responses of H(s) and I + H(s).

H = [0, tf([3 0],[1 1 10]) ; tf([1 1],[1 5]), tf(2,[1 6])]; [svH,wH] = sigma(H); [scIH,wIH] = sigma(H,[],2);

In the last command, the input 2 selects the second response type, I + H(s). The vectors svH and svIH contain the singular value response data, at the frequencies in wH and wIH.

Plot the singular value responses of both systems.

subplot(211)
sigma(H)
subplot(212)
sigma(H,[],2)



More About

Tips

You can change the properties of your plot, for example the units. For information on the ways to change properties of your plots, see "Ways to Customize Plots".

Algorithms

sigma uses the MATLAB function svd to compute the singular values of a complex matrix.

For TF, ZPK, and SS models, sigma computes the frequency response using the freqresp algorithms. As a result, small discrepancies may exist between the sigma responses for equivalent TF, ZPK, and SS representations of a given model.

See Also

bode | evalfr | freqresp | linearSystemAnalyzer | nichols | nyquist

sigmaoptions

Create list of singular-value plot options

Syntax

```
P = sigmaoptions
P = sigmaoptions('cstprefs')
```

Description

P = sigma options returns a list of available options for singular value plots with default values set. You can use these options to customize the singular value plot appearance from the command line.

P = sigmaoptions('cstprefs') initializes the plot options with the options you selected in the Control System Toolbox Preferences Editor. For more information about the editor, see "Toolbox Preferences Editor" in the User's Guide documentation.

Option Description Title, XLabel, YLabel Label text and style TickLabel Tick label style Grid Show or hide the grid Specified as one of the following strings: 'off' | 'on' Default: 'off' GridColor Color of the grid lines Specified as one of the following: Vector of RGB values in the range [0,1] | color string | 'none'. Default: [0.15,0.15,0.15] XlimMode, YlimMode Limit modes Xlim, Ylim Axes limits

This table summarizes the sigma plot options.

Option	Description
IOGrouping	Grouping of input-output pairs Specified as one of the following strings: 'none' 'inputs' 'outputs' 'all' Default: 'none'
InputLabels, OutputLabels	Input and output label styles
InputVisible, OutputVisible	Visibility of input and output channels

Option	Description
FreqUnits	Frequency units, specified as one of the following strings:
	• 'Hz'
	<pre>• 'rad/second'</pre>
	• 'rpm'
	• 'kHz'
	• 'MHz'
	• 'GHz'
	 'rad/nanosecond'
	 'rad/microsecond'
	<pre>• 'rad/millisecond'</pre>
	<pre>• 'rad/minute'</pre>
	• 'rad/hour'
	• 'rad/day'
	<pre>• 'rad/week'</pre>
	<pre>• 'rad/month'</pre>
	• 'rad/year'
	 'cycles/nanosecond'
	 'cycles/microsecond'
	 'cycles/millisecond'
	 'cycles/hour'
	• 'cycles/day'
	 'cycles/week'
	<pre>• 'cycles/month'</pre>
	• 'cycles/year'
	Default: 'rad/s'
	You can also specify 'auto' which uses frequency units rad/TimeUnit relative

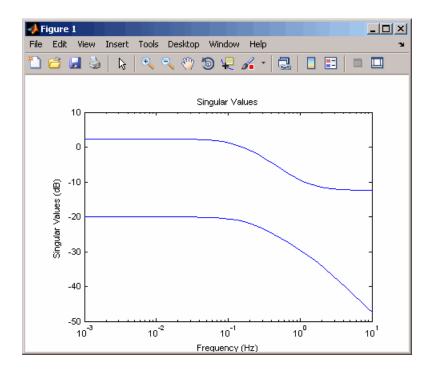
Option	Description
	to system time units specified in the TimeUnit property. For multiple systems with different time units, the units of the first system are used.
FreqScale	Frequency scale Specified as one of the following strings: 'linear' 'log' Default : 'log'
MagUnits	Magnitude units Specified as one of the following strings: 'dB' 'abs' Default : 'dB'
MagScale	Magnitude scale Specified as one of the following strings: 'linear' 'log' Default : 'linear'

Examples

In this example, set the frequency units to Hz before creating a plot.

P = sigmaoptions; % Set the frequency units to Hz in options
P.FreqUnits = 'Hz'; % Create plot with the options specified by P
h = sigmaplot(rss(2,2,3),P);
The following signation using the plot is specified with the frequency units is

The following singular value plot is created with the frequency units in Hz.



See Also

getoptions | setoptions | sigmaplot

Introduced in R2008a

sigmaplot

Plot singular values of frequency response and return plot handle

Syntax

```
h = sigmaplot(sys)
sigmaplot(sys, {wmin,wmax})
sigmaplot(sys,w)
sigmaplot(sys,w,TYPE)
sigmaplot(AX,...)
sigmaplot(..., plotoptions)
```

Description

h = sigmaplot(sys) produces a singular value (SV) plot of the frequency response of the dynamic system sys. It also returns the plot handle h. You can use this handle to customize the plot with the getoptions and setoptions commands. Type

help sigmaoptions

for a list of available plot options.

The frequency range and number of points are chosen automatically. See **bode** for details on the notion of frequency in discrete time.

sigmaplot(sys, {wmin,wmax}) draws the SV plot for frequencies ranging between
wmin and wmax (in rad/TimeUnit, where TimeUnit is the time units of the input
dynamic system, specified in the TimeUnit property of sys).

sigmaplot(sys,w) uses the user-supplied vector w of frequencies, in rad/TimeUnit, at which the frequency response is to be evaluated. See logspace to generate logarithmically spaced frequency vectors.

sigmaplot(sys,w,TYPE) or sigmaplot(sys,[],TYPE) draws the following modified SV plots depending on the value of TYPE:

TYPE = 1	>	SV of inv(SYS)
TYPE = 2	>	SV of I + SYS
TYPE = 3	>	SV of I + $inv(SYS)$

sys should be a square system when using this syntax.

sigmaplot(AX,...) plots into the axes with handle AX.

sigmaplot(..., plotoptions) plots the singular values with the options specified in plotoptions. Type

help sigmaoptions

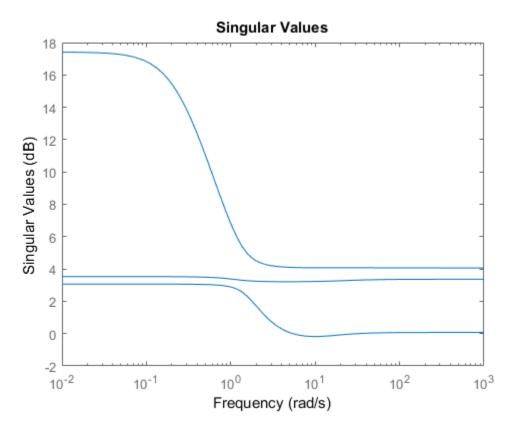
for more details.

Examples

Singular Value Response Plot with Custom Plot Options

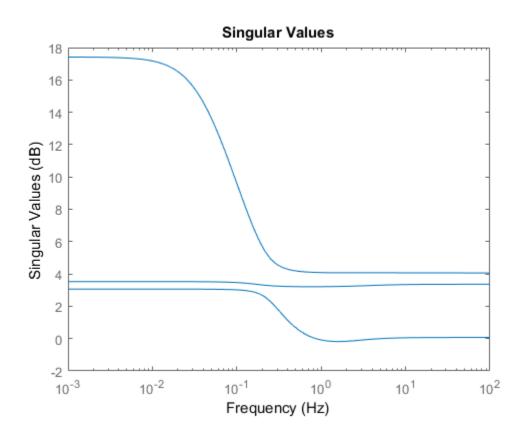
Plot the singular value responses of a dynamic system.

sys = rss(3,3,5); h = sigmaplot(sys);



Set properties of the plot handle h to customize the plot. For example, change the plot units to Hz.

setoptions(h, 'FreqUnits', 'Hz');



More About

Tips

You can change the properties of your plot, for example the units. For information on the ways to change properties of your plots, see "Ways to Customize Plots".

See Also

getoptions | sigma | setoptions | sigmaoptions

Introduced before R2006a

sisoinit

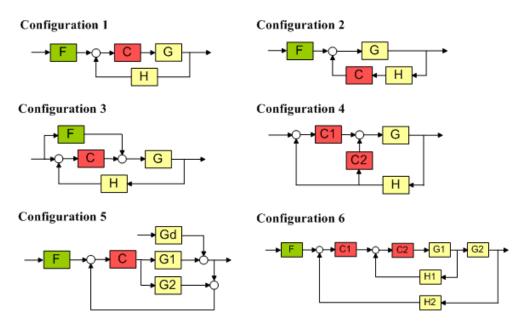
Configure SISO Design Tool at startup

Syntax

```
init_config = sisoinit(config)
```

Description

init_config = sisoinit(config) returns a template init_config for initializing Graphical Tuning window of the SISO Design Tool (Control System Designer) with the one of the following control system configurations:



 $\tt config$ corresponds to the control system configuration. Available configurations include:

- config = 1 (default) C in forward path, F in series
- config = 2 C in feedback path, F in series
- config = 3 C in forward path, feedforward F
- config = 4 Nested loop configuration
- config = 5 Internal model control (IMC) structure
- config = 6 Cascade loop configuration

For each configuration, you can specify the plant models G and H, initialize the compensator C and prefilter F, and configure the open- and closed-loop views by specifying the corresponding fields of the structure init_config. Then use controlSystemDesigner(init_config) to start the SISO Design Tool in the specified configuration.

Output argument init_config is an object with properties. The following tables list the block and loop properties.

Block	Properties	Values
F	Name	String
	Description	String
	Value	LTI object
G	Name	String
	Value	LTI object
		• Row or column array of LTI objects. If the sensor H is also an array of LTI objects, the lengths of G and H must match.
Н	Name	String
	Value	LTI object
		• Row or column array of LTI objects. If the plant G is also an array of LTI objects, the lengths of H and G must match.
С	Name	String
	Description	String
	Value	LTI object

Block Properties

Loop Properties

Loops	Properties	Values
0L1	Name Description View	String String
		'rlocus' 'bode'
CL1	Name Description View	String String
	-	'bode'

Examples

Initialize SISO Design Tool with C in feedback path using an LTI model:

```
% Single-loop configuration with C in the feedback path.
T = sisoinit(2);
% Model for plant G.
T.G.Value = tf(1, [1 1]);
% Initial compensator value.
T.C.Value = tf(1,[1 2]);
% Views for tuning Open-Loop OL1.
T.OL1.View = {'rlocus', 'nichols'};
% Launch SISO Design Tool using configuration T
controlSystemDesigner(T)
```

Initialize SISO Design Tool with C in feedback path using an array of LTI models:

```
% Specify an initial configuration.
initconfig = sisoinit(2);
% Specify model parameters.
m = 3;
b = 0.5;
k = 8:1:10;
T = 0.1:.05:.2;
% Create an LTI array to model variations in plant G.
for ct = 1:length(k);
    G(:,:,ct) = tf(1,[m,b,k(ct)]);
end
% Assign G to the initial configuration.
initconfig.G.Value = G;
```

```
% Create an LTI array to model variations in sensor H.
for ct = 1:length(T);
    H(:,:,ct) = tf(1,[1/T(ct), 1]);
end
% Assign H to the initial configuration.
initconfig.H.Value = H;
% Specify initial controller.
initconfig.C.Value = tf(1,[1 2]);
% Views for tuning Open-Loop (OL1)
initconfig.OL1.View = {'rlocus','bode'};
% Launch SISO Design Tool using initconfig.
controlSystemDesigner(initconfig)
```

More About

- "SISO Design Tool"
- "Control Design Analysis of Multiple Models"

See Also

controlSystemDesigner

Introduced in R2006a

size

Query output/input/array dimensions of input–output model and number of frequencies of FRD model

Syntax

```
size(sys)
d = size(sys)
Ny = size(sys,1)
Nu = size(sys,2)
Sk = size(sys,2+k)
Nf = size(sys,'frequency')
```

Description

When invoked without output arguments, SiZe(SyS) returns a description of type and the input-output dimensions of SyS. If SyS is a model array, the array size is also described. For identified models, the number of free parameters is also displayed. The lengths of the array dimensions are also included in the response to size when SyS is a model array.

d = size(sys) returns:

- The row vector d = [Ny Nu] for a single dynamic model sys with Ny outputs and Nu inputs
- The row vector d = [Ny Nu S1 S2 ... Sp] for an S1-by-S2-by-...-by-Sp array of dynamic models with Ny outputs and Nu inputs

Ny = size(sys,1) returns the number of outputs of sys.

Nu = size(sys,2) returns the number of inputs of sys.

Sk = size(sys, 2+k) returns the length of the k-th array dimension when sys is a model array.

Nf = size(sys, 'frequency') returns the number of frequencies when sys is a frequency response data model. This is the same as the length of sys.frequency.

Examples

Example 1

Consider the model array of random state-space models

```
sys = rss(5,3,2,3);
```

Its dimensions are obtained by typing

```
size(sys)
3x1 array of state-space models
Each model has 3 outputs, 2 inputs, and 5 states.
```

Example 2

Consider the process model:

sys = idproc({'p1d', 'p2'; 'p3uz', 'p0'});

It's input-output dimensions and number of free parameters are obtained by typing:

size(sys)

Process model with 2 outputs, 2 inputs and 12 free parameters.

See Also

issiso | ndims | isempty

Introduced before R2006a

sminreal

Structural pole/zero cancellations

Syntax

```
msys = sminreal(sys)
```

Description

msys = sminreal(sys) eliminates the states of the state-space model sys that don't
affect the input/output response. All of the states of the resulting state-space model msys
are also states of sys and the input/output response of msys is equivalent to that of sys.

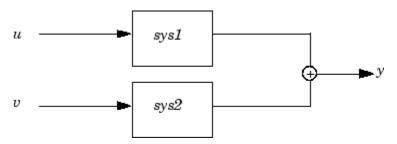
sminreal eliminates only structurally non minimal states, i.e., states that can be discarded by looking only at hard zero entries in the *A*, *B*, and *C* matrices. Such structurally nonminimal states arise, for example, when linearizing a Simulink model that includes some unconnected state-space or transfer function blocks.

Examples

Suppose you concatenate two SS models, sys1 and sys2.

sys = [sys1,sys2];

This operation is depicted in the diagram below.



If you extract the subsystem sys1 from sys, with

sys(1,1)

all of the states of **sys**, including those of **sys2** are retained. To eliminate the unobservable states from **sys2**, while retaining the states of **sys1**, type

```
sminreal(sys(1,1))
```

More About

Tips

The model resulting from sminreal(sys) is not necessarily minimal, and may have a higher order than one resulting from minreal(sys). However, sminreal(sys) retains the state structure of sys, while, in general, minreal(sys) does not.

See Also

minreal

Introduced before R2006a

SS

Create state-space model, convert to state-space model

Syntax

```
sys = ss(a,b,c,d)
sys = ss(a,b,c,d,Ts)
sys = ss(d)
sys = ss(a,b,c,d,ltisys)
sys_ss = ss(sys)
sys_ss = ss(sys,'minimal')
sys_ss = ss(sys,'explicit')
sys_ss = ss(sys, 'measured')
sys_ss = ss(sys, 'noise')
sys ss = ss(sys, 'augmented')
```

Description

Use **ss** to create state-space models (**ss** model objects) with real- or complex-valued matrices or to convert dynamic system models to state-space model form. You can also use **ss** to create Generalized state-space (**genss**) models.

Creation of State-Space Models

sys = ss(a,b,c,d) creates a state-space model object representing the continuoustime state-space model

 $\dot{x} = Ax + Bu$ y = Cx + Du

For a model with Nx states, Ny outputs, and Nu inputs:

- a is an Nx-by-Nx real- or complex-valued matrix.
- b is an Nx-by-Nu real- or complex-valued matrix.

- C is an Ny-by-Nx real- or complex-valued matrix.
- d is an Ny-by-Nu real- or complex-valued matrix.

To set D = 0, set d to the scalar 0 (zero), regardless of the dimension.

sys = ss(a,b,c,d,Ts) creates the discrete-time model

```
x[n+1] = Ax[n] + Bu[n]
y[n] = Cx[n] + Du[n]
```

with sample time Ts (in seconds). Set Ts = -1 or Ts = [] to leave the sample time unspecified.

sys = ss(d) specifies a static gain matrix D and is equivalent to

sys = ss([],[],[],d)

sys = ss(a,b,c,d,ltisys) creates a state-space model with properties inherited
from the model ltisys (including the sample time).

Any of the previous syntaxes can be followed by property name/property value pairs.

'PropertyName', PropertyValue

Each pair specifies a particular property of the model, for example, the input names or some notes on the model history. See "Properties" on page 1-789 for more information about available **ss** model object properties.

The following expression:

sys = ss(a,b,c,d,'Property1',Value1,...,'PropertyN',ValueN)

is equivalent to the sequence of commands:

sys = ss(a,b,c,d)
set(sys,'Property1',Value1,...,'PropertyN',ValueN)

Conversion to State Space

sys_ss = ss(sys) converts a dynamic system model sys to state-space form. The
output sys_ss is an equivalent state-space model (ss model object). This operation is
known as state-space realization.

sys_ss = ss(sys, 'minimal') produces a state-space realization with no
uncontrollable or unobservable states. This state-space realization is equivalent to
sys_ss = minreal(ss(sys)).

sys_ss = ss(sys, 'explicit') computes an explicit realization (E = I) of the
dynamic system model sys. If sys is improper, ss returns an error.

Note: Conversions to state space are not uniquely defined in the SISO case. They are also not guaranteed to produce a minimal realization in the MIMO case. For more information, see "Recommended Working Representation".

Conversion of Identified Models

An identified model is represented by an input-output equation of the form y(t) = Gu(t) + He(t), where u(t) is the set of measured input channels and e(t) represents the noise channels. If $\Lambda = LL'$ represents the covariance of noise e(t), this equation can also be written as y(t) = Gu(t) + HLv(t), where cov(v(t)) = I.

sys_ss = ss(sys) or sys_ss = ss(sys, 'measured') converts the measured component of an identified linear model into the state-space form. sys is a model of type idss, idproc, idtf, idpoly, or idgrey. sys_ss represents the relationship between u and y.

 $sys_s = ss(sys, 'noise')$ converts the noise component of an identified linear model into the state space form. It represents the relationship between the noise input v(t) and output $y_{noise} = HL v(t)$. The noise input channels belong to the InputGroup 'Noise'. The names of the noise input channels are v@yname, where yname is the name of the corresponding output channel. sys_s has as many inputs as outputs.

 $sys_ss = ss(sys, 'augmented')$ converts both the measured and noise dynamics into a state-space model. sys_ss has ny+nu inputs such that the first nu inputs represent the channels u(t) while the remaining by channels represent the noise channels v(t). $sys_ss.InputGroup$ contains 2 input groups- 'measured' and 'noise'. $sys_ss.InputGroup.Measured$ is set to 1:nu while $sys_ss.InputGroup.Noise$ is set to nu+1:nu+ny. sys_ss represents the equation y(t) = [G HL][u; v] **Tip** An identified nonlinear model cannot be converted into a state-space form. Use linear approximation functions such as linearize and linapp.

Creation of Generalized State-Space Models

You can use the syntax:

gensys = ss(A,B,C,D)

to create a Generalized state-space (genss) model when one or more of the matrices A, B, C, D is a tunable realp or genmat model. For more information about Generalized state-space models, see "Models with Tunable Coefficients".

Properties

ss objects have the following properties:

a,b,c,d,e

State-space matrices.

- **a** State matrix *A*. Square real- or complex-valued matrix with as many rows as states.
- b Input-to-state matrix *B*. Real- or complex-valued matrix with as many rows as states and as many columns as inputs.
- **c** State-to-output matrix *C*. Real- or complex-valued matrix with as many rows as outputs and as many columns as states.
- d Feedthrough matrix *D*. Real- or complex-valued matrix with as many rows as outputs and as many columns as inputs.
- e E matrix for implicit (descriptor) state-space models. By default e = [], meaning that the state equation is explicit. To specify an implicit state equation Edx/dt = Ax + Bu, set this property to a square matrix of the same size as a. See dss for more information about creating descriptor state-space models.

Scaled

Logical value indicating whether scaling is enabled or disabled.

When Scaled = 0 (false), most numerical algorithms acting on the state-space model automatically rescale the state vector to improve numerical accuracy. You can disable such auto-scaling by setting Scaled = 1 (true). For more information about scaling, see prescale.

Default: 0 (false)

StateName

State names. For first-order models, set **StateName** to a string. For models with two or more states, set **StateName** to a cell array of strings. Use an empty string '' for unnamed states.

Default: Empty string ' ' for all states

StateUnit

State units. Use StateUnit to keep track of the units each state is expressed in. For first-order models, set StateUnit to a string. For models with two or more states, set StateUnit to a cell array of strings. StateUnit has no effect on system behavior.

Default: Empty string ' ' for all states

InternalDelay

Vector storing internal delays.

Internal delays arise, for example, when closing feedback loops on systems with delays, or when connecting delayed systems in series or parallel. For more information about internal delays, see "Closing Feedback Loops with Time Delays" in the *Control System Toolbox User's Guide*.

For continuous-time models, internal delays are expressed in the time unit specified by the TimeUnit property of the model. For discrete-time models, internal delays are expressed as integer multiples of the sample time Ts. For example, InternalDelay = 3 means a delay of three sampling periods.

You can modify the values of internal delays. However, the number of entries in **sys.InternalDelay** cannot change, because it is a structural property of the model.

InputDelay

Input delay for each input channel, specified as a scalar value or numeric vector. For continuous-time systems, specify input delays in the time unit stored in the TimeUnit

property. For discrete-time systems, specify input delays in integer multiples of the sample time Ts. For example, InputDelay = 3 means a delay of three sample times.

For a system with Nu inputs, set InputDelay to an Nu-by-1 vector. Each entry of this vector is a numerical value that represents the input delay for the corresponding input channel.

You can also set InputDelay to a scalar value to apply the same delay to all channels.

Default: 0

OutputDelay

Output delays. OutputDelay is a numeric vector specifying a time delay for each output channel. For continuous-time systems, specify output delays in the time unit stored in the TimeUnit property. For discrete-time systems, specify output delays in integer multiples of the sample time Ts. For example, OutputDelay = 3 means a delay of three sampling periods.

For a system with Ny outputs, set OutputDelay to an Ny-by-1 vector, where each entry is a numerical value representing the output delay for the corresponding output channel. You can also set OutputDelay to a scalar value to apply the same delay to all channels.

Default: 0 for all output channels

Ts

Sample time. For continuous-time models, Ts = 0. For discrete-time models, Ts is a positive scalar representing the sampling period. This value is expressed in the unit specified by the TimeUnit property of the model. To denote a discrete-time model with unspecified sample time, set Ts = -1.

Changing this property does not discretize or resample the model. Use c2d and d2c to convert between continuous- and discrete-time representations. Use d2d to change the sample time of a discrete-time system.

Default: 0 (continuous time)

TimeUnit

String representing the unit of the time variable. This property specifies the units for the time variable, the sample time Ts, and any time delays in the model. Use any of the following values:

- 'nanoseconds'
- 'microseconds'
- 'milliseconds'
- 'seconds'
- 'minutes'
- 'hours'
- 'days'
- 'weeks'
- 'months'
- 'years'

Changing this property has no effect on other properties, and therefore changes the overall system behavior. Use chgTimeUnit to convert between time units without modifying system behavior.

Default: 'seconds'

InputName

Input channel names. Set InputName to a string for single-input model. For a multiinput model, set InputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign input names for multi-input models. For example, if **sys** is a two-input model, enter:

sys.InputName = 'controls';

The input names automatically expand to { 'controls(1) '; 'controls(2) '}.

You can use the shorthand notation u to refer to the InputName property. For example, sys.u is equivalent to sys.InputName.

Input channel names have several uses, including:

- · Identifying channels on model display and plots
- · Extracting subsystems of MIMO systems
- Specifying connection points when interconnecting models

Default: Empty string ' ' for all input channels

InputUnit

Input channel units. Use InputUnit to keep track of input signal units. For a singleinput model, set InputUnit to a string. For a multi-input model, set InputUnit to a cell array of strings. InputUnit has no effect on system behavior.

Default: Empty string ' ' for all input channels

InputGroup

Input channel groups. The InputGroup property lets you assign the input channels of MIMO systems into groups and refer to each group by name. Specify input groups as a structure. In this structure, field names are the group names, and field values are the input channels belonging to each group. For example:

sys.InputGroup.controls = [1 2]; sys.InputGroup.noise = [3 5];

creates input groups named controls and noise that include input channels 1, 2 and 3, 5, respectively. You can then extract the subsystem from the controls inputs to all outputs using:

```
sys(:,'controls')
```

Default: Struct with no fields

OutputName

Output channel names. Set OutputName to a string for single-output model. For a multioutput model, set OutputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign output names for multi-output models. For example, if **sys** is a two-output model, enter:

```
sys.OutputName = 'measurements';
```

The output names automatically expand to { 'measurements(1) '; 'measurements(2) ' }.

You can use the shorthand notation y to refer to the OutputName property. For example, sys.y is equivalent to sys.OutputName.

Output channel names have several uses, including:

- Identifying channels on model display and plots
- · Extracting subsystems of MIMO systems
- Specifying connection points when interconnecting models

Default: Empty string ' ' for all output channels

OutputUnit

Output channel units. Use OutputUnit to keep track of output signal units. For a single-output model, set OutputUnit to a string. For a multi-output model, set OutputUnit to a cell array of strings. OutputUnit has no effect on system behavior.

Default: Empty string ' ' for all output channels

OutputGroup

Output channel groups. The OutputGroup property lets you assign the output channels of MIMO systems into groups and refer to each group by name. Specify output groups as a structure. In this structure, field names are the group names, and field values are the output channels belonging to each group. For example:

```
sys.OutputGroup.temperature = [1];
sys.InputGroup.measurement = [3 5];
```

creates output groups named temperature and measurement that include output channels 1, and 3, 5, respectively. You can then extract the subsystem from all inputs to the measurement outputs using:

```
sys('measurement',:)
```

Default: Struct with no fields

Name

System name. Set Name to a string to label the system.

Default: ' '

Notes

Any text that you want to associate with the system. Set **Notes** to a string or a cell array of strings.

Default: { }

UserData

Any type of data you want to associate with system. Set UserData to any MATLAB data type.

Default: []

SamplingGrid

Sampling grid for model arrays, specified as a data structure.

For model arrays that are derived by sampling one or more independent variables, this property tracks the variable values associated with each model in the array. This information appears when you display or plot the model array. Use this information to trace results back to the independent variables.

Set the field names of the data structure to the names of the sampling variables. Set the field values to the sampled variable values associated with each model in the array. All sampling variables should be numeric and scalar valued, and all arrays of sampled values should match the dimensions of the model array.

For example, suppose you create a 11-by-1 array of linear models, sysarr, by taking snapshots of a linear time-varying system at times t = 0:10. The following code stores the time samples with the linear models.

sysarr.SamplingGrid = struct('time',0:10)

Similarly, suppose you create a 6-by-9 model array, M, by independently sampling two variables, zeta and w. The following code attaches the (zeta,w) values to M.

```
[zeta,w] = ndgrid(<6 values of zeta>,<9 values of w>)
M.SamplingGrid = struct('zeta',zeta,'w',w)
```

When you display M, each entry in the array includes the corresponding zeta and w values.

М

M(:,:,1,1) [zeta=0.3, w=5] =

```
s^2 + 3 s + 25
M(:,:,2,1) [zeta=0.35, w=5] =
25
s^2 + 3.5 s + 25
....
```

For model arrays generated by linearizing a Simulink model at multiple parameter values or operating points, the software populates SamplingGrid automatically with the variable values that correspond to each entry in the array. For example, the Simulink Control Design commands linearize and slLinearizer populate SamplingGrid in this way.

Default: []

Examples

Discrete-Time State-Space Model

Create a state-space model with a sample time of $0.25~\mathrm{s}$ and the following state-space matrices:

$$A = \begin{bmatrix} 0 & 1 \\ -5 & -2 \end{bmatrix} \quad B = \begin{bmatrix} 0 \\ 3 \end{bmatrix} \quad C = \begin{bmatrix} 0 & 1 \end{bmatrix} \quad D = \begin{bmatrix} 0 \end{bmatrix}$$

To do this, enter the following commands:

```
A = [0 1;-5 -2];
B = [0;3];
C = [0 1];
D = 0;
sys = ss(A,B,C,D,0.25);
```

The last argument sets the sample time.

Discrete-Time State-Space Model with Custom State and Input Names

Create a discrete-time model with matrices A,B,C,D and sample time 0.05 second.

This model has two states labeled **position** and **velocity**, and one input labeled **force** (the dimensions of A, B, C, D should be consistent with these numbers of states and inputs). Finally, a note is attached with the date of creation of the model.

Convert Transfer Function Model to State-Space Model

Convert a transfer function model to a state-space model.

$$H(s) = \begin{bmatrix} \frac{s+1}{s^3 + 3s^2 + 3s + 2} \\ \frac{s^2 + 3}{s^2 + s + 1} \end{bmatrix}$$

by typing

```
H = [tf([1 1],[1 3 3 2]) ; tf([1 0 3],[1 1 1])];
sys = ss(H);
size(sys)
```

```
State-space model with 2 outputs, 1 input, and 5 states.
```

The number of states is equal to the cumulative order of the SISO entries of H(s).

To obtain a minimal realization of H(s), type

```
sys = ss(H, 'min');
size(sys)
State-space model with 2 outputs, 1 input, and 3 states.
```

The resulting state-space model has order of three, which is the minimum number of states needed to represent H(s). You can see this number of states by factoring H(s) as the product of a first-order system with a second-order system.

$$H(s) = \begin{bmatrix} \frac{1}{s+2} & 0\\ 0 & 1 \end{bmatrix} \begin{bmatrix} \frac{s+1}{s^2+s+1}\\ \frac{s^2+3}{s^2+s+1} \end{bmatrix}$$

Explicit Realization of Descriptor State-Space Model

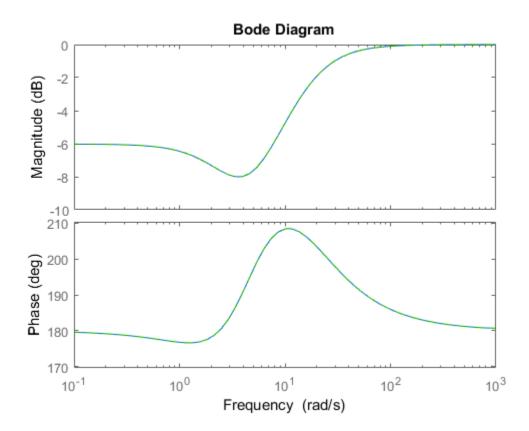
Create a descriptor state-space model ($E \neq I$).

```
a = [2 -4; 4 2];
b = [-1; 0.5];
c = [-0.5, -2];
d = [-1];
e = [1 0; -3 0.5];
sysd = dss(a,b,c,d,e);
```

```
Compute an explicit realization of the system (E = I).
```

```
syse = ss(sysd, 'explicit')
syse =
  a =
        x1
             х2
   х1
        2
             -4
   х2
        20
            -20
  b =
       u1
       - 1
   x1
   x2
       - 5
  с =
         х1
                х2
                -2
   y1
       -0.5
  d =
       u1
   y1 -1
Continuous-time state-space model.
```

Confirm that the descriptor and explicit realizations have equivalent dynamics. bodeplot(sysd,syse,'g--')



Generalized State-Space Model

This example shows how to create a state-space (genss) model having both fixed and tunable parameters.

Create a state-space model having the following state-space matrices:

$$A = \begin{bmatrix} 1 & a+b \\ 0 & ab \end{bmatrix}, \quad B = \begin{bmatrix} -3.0 \\ 1.5 \end{bmatrix}, \quad C = \begin{bmatrix} 0.3 & 0 \end{bmatrix}, \quad D = 0,$$

where a and b are tunable parameters, whose initial values are -1 and 3, respectively.

1 Create the tunable parameters using realp.

```
a = realp('a',-1);
b = realp('b',3);
```

2 Define a generalized matrix using algebraic expressions of **a** and **b**.

 $A = [1 \ a+b; 0 \ a*b]$

A is a generalized matrix whose Blocks property contains a and b. The initial value of A is $M = [1 \ 2; 0 \ -3]$, from the initial values of a and b.

3 Create the fixed-value state-space matrices.

B = [-3.0;1.5]; C = [0.3 0]; D = 0;

4 Use **ss** to create the state-space model.

sys = ss(A,B,C,D)

sys is a generalized LTI model (genss) with tunable parameters a and b.

Extract Components from Identified State-Space Model

Extract the measured and noise components of an identified polynomial model into two separate state-space models. The former (measured component) can serve as a plant model while the latter can serve as a disturbance model for control system design.

```
load icEngine
z = iddata(y,u,0.04);
sys = ssest(z,3);
sysMeas = ss(sys,'measured')
sysNoise = ss(sys,'noise')
```

Alternatively, use **ss(sys)** to extract the measured component.

More About

Algorithms

For TF to SS model conversion, ss(sys_tf) returns a modified version of the controllable canonical form. It uses an algorithm similar to tf2ss, but further rescales the state vector to compress the numerical range in state matrix A and to improve numerics in subsequent computations.

For ZPK to SS conversion, **ss(sys_zpk)** uses direct form II structures, as defined in signal processing texts. See *Discrete-Time Signal Processing* by Oppenheim and Schafer for details.

For example, in the following code, A and ${\tt sys.a}$ differ by a diagonal state transformation:

```
n=[1 1];
d=[1 1 10];
[A,B,C,D]=tf2ss(n,d);
sys=ss(tf(n,d));
А
A =
    -1
          -10
     1
            0
sys.a
ans =
    -1
           - 5
     2
            0
```

For details, see balance.

• "What Are Model Objects?"

See Also

dss | frd | get | set | ssdata | tf | zpk

Introduced before R2006a

ss2ss

State coordinate transformation for state-space model

Syntax

sysT = ss2ss(sys,T)

Description

Given a state-space model sys with equations

$$\dot{x} = Ax + Bu$$
$$y = Cx + Du$$

or the innovations form used by the identified state-space (IDSS) models:

$$\frac{dx}{dt} = Ax + Bu + Ke$$
$$y = Cx + Du + e$$

(or their discrete-time counterpart), **SS2SS** performs the similarity transformation $\bar{x} = Tx$ on the state vector x and produces the equivalent state-space model **SYST** with equations.

$$\dot{\overline{x}} = TAT^{-1}\overline{x} + TBu$$
$$y = CT^{-1}\overline{x} + Du$$

or, in the case of an IDSS model:

$$\dot{\overline{x}} = TAT^{-1}\overline{x} + TBu + TKe$$

 $y = CT^{-1}\overline{x} + Du + e$

(IDSS models require System Identification Toolbox software.)

sysT = ss2ss(sys,T) returns the transformed state-space model sysT given sys and the state coordinate transformation T. The model sys must be in state-space form and the matrix T must be invertible. ss2ss is applicable to both continuous- and discrete-time models.

Examples

Perform a similarity transform to improve the conditioning of the A matrix.

T = balance(sys.a)
sysb = ss2ss(sys,inv(T))

See Also balreal | canon

Introduced before R2006a

ssdata

Access state-space model data

Syntax

```
[a,b,c,d] = ssdata(sys)
[a,b,c,d,Ts] = ssdata(sys)
```

Description

[a,b,c,d] = ssdata(sys) extracts the matrix (or multidimensional array) data A, B, C, D from the state-space model (LTI array) sys. If sys is a transfer function or zero-pole-gain model (LTI array), it is first converted to state space. See ss for more information on the format of state-space model data.

If ${\tt sys}$ appears in descriptor form (nonempty ${\sf E}$ matrix), an equivalent explicit form is first derived.

If **sys** has internal delays, A, B, C, D are obtained by first setting all internal delays to zero (creating a zero-order Padé approximation). For some systems, setting delays to zero creates singular algebraic loops, which result in either improper or ill-defined, zero-delay approximations. For these systems, **ssdata** cannot display the matrices and returns an error. This error does not imply a problem with the model **sys** itself.

[a,b,c,d,Ts] = ssdata(sys) also returns the sample time Ts.

You can access the remaining LTI properties of **sys** with **get** or by direct referencing. For example:

sys.statename

For arrays of state-space models with variable numbers of states, use the syntax:

[a,b,c,d] = ssdata(sys,'cell')

to extract the state-space matrices of each model as separate cells in the cell arrays a, b, c, and d.

See Also

dssdata | getdelaymodel | set | tfdata | zpkdata | get | ss

Introduced before R2006a

stabsep

Stable-unstable decomposition

Syntax

```
[GS,GNS]=stabsep(G)
[G1,GNS] = stabsep(G, 'abstol',ATOL, 'reltol',RTOL)
[G1,G2]=stabsep(G, ..., 'Mode', MODE, 'Offset', ALPHA)
[G1,G2] = stabsep(G, opts)
```

Description

[GS,GNS]=stabsep(G) decomposes the LTI model G into its stable and unstable parts

G = GS + GNS

where GS contains all stable modes that can be separated from the unstable modes in a numerically stable way, and GNS contains the remaining modes. GNS is always strictly proper.

[G1,GNS] = stabsep(G, 'abstol', ATOL, 'reltol', RTOL) specifies absolute and relative error tolerances for the stable/unstable decomposition. The frequency responses of G and GS + GNS should differ by no more than ATOL+RTOL*abs(G). Increasing these tolerances helps separate nearby stable and unstable modes at the expense of accuracy. The default values are ATOL=0 and RTOL=1e-8.

[G1,G2]=stabsep(G, ..., 'Mode', MODE, 'Offset', ALPHA) produces a more general stable/unstable decomposition where G1 includes all separable poles lying in the regions defined using offset ALPHA. This can be useful when there are numerical accuracy issues. For example, if you have a pair of poles close to, but slightly to the left of the $j\omega$ -axis, you can decide not to include them in the stable part of the decomposition if numerical considerations lead you to believe that the poles may be in fact unstable

This table lists the stable/unstable boundaries as defined by the offset ALPHA.

Mode	Continuous Time Region	Discrete Time Region
1	Re(s) < -ALPHA*max(1, Im(s))	1 z < 1-ALPHA

Mode	Continuous Time Region	Discrete Time Region
2	<pre>Re(s)> ALPHA*max(1, Im(s))</pre>	2 z > 1+ALPHA

The default values are MODE=1 and ALPHA=0.

[G1,G2] = stabsep(G, opts) computes the stable/unstable decomposition of G using the options specified in the stabsepOptions object opts.

Examples

Compute a stable/unstable decomposition with absolute error no larger than 1e-5 and an offset of 0.1:

h = zpk(1,[-2 -1 1 -0.001],0.1)
[hs,hns] = stabsep(h,stabsepOptions('AbsTol',1e-5,'Offset',0.1));

The stable part of the decomposition has poles at -1 and -2.

hs

```
Zero/pole/gain:
-0.050075 (s+2.999)
(s+1) (s+2)
```

The unstable part of the decomposition has poles at +1 and -.001 (which is nominally stable).

hns

Zero/pole/gain: 0.050075 (s-1) (s+0.001) (s-1)

See Also

stabsepOptions | modsep

Introduced before R2006a

stabsepOptions

Options for stable-unstable decomposition

Syntax

```
opts = stabsepOptions
opts = stabsepOptions('OptionName', OptionValue)
```

Description

opts = stabsepOptions returns the default options for the stabsep command.

opts = stabsepOptions('OptionName', OptionValue) accepts one or more comma-separated name/value pairs. Specify OptionName inside single quotes.

Input Arguments

Name-Value Pair Arguments

'Focus'

Focus of decomposition. Specified as one of the following values:

'stable'	First output of stabsep contains only stable dynamics.
----------	--

'unstable' First output of stabsep contains only unstable dynamics.

Default: 'stable'

'AbsTol, RelTol'

Absolute and relative error tolerance for stable/unstable decomposition. Positive scalar values. When decomposing a model G, stabsep ensures that the frequency responses of G and GS + GU differ by no more than AbsTol + RelTol*abs(G). Increasing these tolerances helps separate nearby stable and unstable modes at the expense of accuracy. See stabsep for more information.

```
Default: AbsTol = 0; RelTol = 1e-8
```

'Offset'

Offset for the stable/unstable boundary. Positive scalar value. The first output of **stabsep**includes only poles satisfying:

Continuous time:

```
• Re(s) < -Offset * max(1,|Im(s)|) (Focus = 'stable')</pre>
```

• Re(s) > Offset * max(1,|Im(s)|) (Focus = 'unstable')

Discrete time:

```
|z| < 1 - Offset (Focus = 'stable')</li>
|z| >1 + Offset (Focus = 'unstable')
```

Increase the value of Offset to treat poles close to the stability boundary as unstable.

Default: 0

For additional information on the options and how to use them, see the **stabsep** reference page.

Examples

Compute the stable/unstable decomposition of the system given by:

 $G(s) = \frac{10(s+0.5)}{(s+10^{-6})(s+2-5i)(s+2+5i)}$

Use the Offset option to force stabsep to exclude the pole at $s = 10^{-6}$ from the stable term of the stable/unstable decomposition.

G = zpk(-.5,[-1e-6 -2+5i -2-5i],10);
opts = stabsepOptions('Offset',.001); % Create option set
[G1,G2] = stabsep(G,opts) % treats -1e-6 as unstable

These commands return the result:

See Also

stabsep

Introduced in R2010a

stack

Build model array by stacking models or model arrays along array dimensions

Syntax

```
sys = stack(arraydim,sys1,sys2,...)
```

Description

sys = stack(arraydim,sys1,sys2,...) produces an array of dynamic system
models sys by stacking (concatenating) the models (or arrays) sys1,sys2,... along
the array dimension arraydim. All models must have the same number of inputs
and outputs (the same I/O dimensions), but the number of states can vary. The I/O
dimensions are not counted in the array dimensions. For more information about model
arrays and array dimensions, see "Model Arrays".

For arrays of state-space models with variable order, you cannot use the dot operator (e.g., **sys.a**) to access arrays. Use the syntax

[a,b,c,d] = ssdata(sys,'cell')

to extract the state-space matrices of each model as separate cells in the cell arrays ${\tt a}, {\tt b}, {\tt c}, {\tt and } {\tt d}.$

Examples

Example 1

If sys1 and sys2 are two models:

- stack(1,sys1,sys2) produces a 2-by-1 model array.
- stack(2,sys1,sys2) produces a 1-by-2 model array.
- stack(3,sys1,sys2) produces a 1-by-1-by-2 model array.

Example 2

Stack identified state-space models derived from the same estimation data and compare their bode responses.

```
load iddata1 z1
sysc = cell(1,5);
opt = ssestOptions('Focus','simulation');
for i = 1:5
sysc{i} = ssest(z1,i-1,opt);
end
sysArray = stack(1, sysc{:});
bode(sysArray);
```

Introduced before R2006a

step

Step response plot of dynamic system

Syntax

```
step(sys)
step(sys,Tfinal)
step(sys,t)
step(sys1,sys2,...,sysN)
step(sys1,sys2,...,sysN,Tfinal)
step(sys1,sys2,...,sysN,t)
y = step(sys,t)
[y,t] = step(sys)
[y,t] = step(sys,Tfinal)
[y,t,x] = step(sys)
[y,t,x,ysd] = step(sys)
[y,...] = step(sys,...,options)
```

Description

step calculates the step response of a dynamic system. For the state-space case, zero initial state is assumed. When it is invoked with no output arguments, this function plots the step response on the screen.

step(sys) plots the step response of an arbitrary dynamic system model, **sys**. This model can be continuous- or discrete-time, and SISO or MIMO. The step response of multi-input systems is the collection of step responses for each input channel. The duration of simulation is determined automatically, based on the system poles and zeros.

step(sys,Tfinal) simulates the step response from t = 0 to the final time t =
Tfinal. Express Tfinal in the system time units, specified in the TimeUnit property of
sys. For discrete-time systems with unspecified sample time (Ts = -1), step interprets
Tfinal as the number of sampling periods to simulate.

step(sys,t) uses the user-supplied time vector t for simulation. Express t in the
system time units, specified in the TimeUnit property of sys. For discrete-time models,

t should be of the form Ti:Ts:Tf, where Ts is the sample time. For continuous-time models, t should be of the form Ti:dt:Tf, where dt becomes the sample time of a discrete approximation to the continuous system (see "Algorithms" on page 1-823). The step command always applies the step input at t=0, regardless of Ti.

To plot the step response of several models sys1,..., sysN on a single figure, use

```
step(sys1,sys2,...,sysN)
step(sys1,sys2,...,sysN,Tfinal)
step(sys1,sys2,...,sysN,t)
```

All of the systems plotted on a single plot must have the same number of inputs and outputs. You can, however, plot a mix of continuous- and discrete-time systems on a single plot. This syntax is useful to compare the step responses of multiple systems.

You can also specify a distinctive color, linestyle, marker, or all three for each system. For example,

```
step(sys1,'y:',sys2,'g--')
```

plots the step response of **sys1** with a dotted yellow line and the step response of **sys2** with a green dashed line.

When invoked with output arguments:

y = step(sys,t)
[y,t] = step(sys)
[y,t] = step(sys,Tfinal)
[y,t,x] = step(sys)

step returns the output response y, the time vector t used for simulation (if not supplied as an input argument), and the state trajectories X (for state-space models only). No plot generates on the screen. For single-input systems, y has as many rows as time samples (length of t), and as many columns as outputs. In the multi-input case, the step responses of each input channel are stacked up along the third dimension of y. The dimensions of y are then

(*length of t*)×(*number of outputs*)×(*number of inputs*)

and y(:,:,j) gives the response to a unit step command injected in the jth input channel. Similarly, the dimensions of x are

(*length* of *t*)×(*number* of *states*)×(*number* of *inputs*)

For identified models (see idlti and idnlmodlel) [y,t,x,ysd] = step(sys) also computes the standard deviation ysd of the response y (ysd is empty if sys does not contain parameter covariance information).

[y, ...] = step(sys, ..., options) specifies additional options for computing the step response, such as the step amplitude or input offset. Use stepDataOptions to create the option set options.

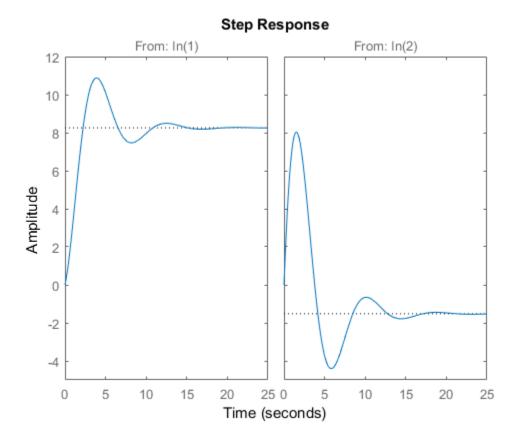
Examples

Step Response Plot of Dynamic System

Plot the step response of the following second-order state-space model:

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} -0.5572 & -0.7814 \\ 0.7814 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 1 & -1 \\ 0 & 2 \end{bmatrix} \begin{bmatrix} u_1 \\ u_2 \end{bmatrix}$$
$$y = \begin{bmatrix} 1.9691 & 6.4493 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$

```
a = [-0.5572,-0.7814;0.7814,0];
b = [1,-1;0,2];
c = [1.9691,6.4493];
sys = ss(a,b,c,0);
step(sys)
```

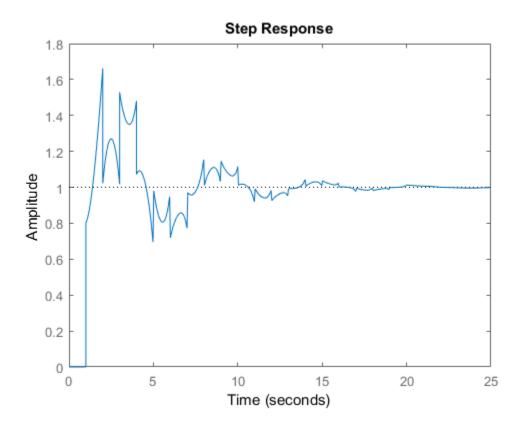


The left plot shows the step response of the first input channel, and the right plot shows the step response of the second input channel.

Step Response Plot of Feedback Loop with Delay

Create a feedback loop with delay and plot its step response.

```
s = tf('s');
G = exp(-s) * (0.8*s^2+s+2)/(s^2+s);
T = feedback(ss(G),1);
step(T)
```



The system step response displayed is chaotic. The step response of systems with internal delays may exhibit odd behavior, such as recurring jumps. Such behavior is a feature of the system and not software anomalies.

Step Responses of Identified Models with Confidence Regions

Compare the step response of a parametric identified model to a non-parametric (empirical) model. Also view their 3 σ confidence regions.

Load the data.

```
load iddata1 z1
```

Esimate a parametric model.

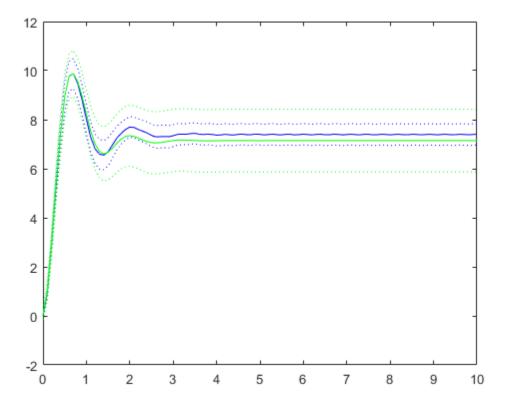
sys1 = ssest(z1,4);

Estimate a non-parametric model.

```
sys2 = impulseest(z1);
```

Plot the step responses for comparision.

```
t = (0:0.1:10)';
[y1, ~, ~, ysd1] = step(sys1,t);
[y2, ~, ~, ysd2] = step(sys2,t);
plot(t, y1, 'b', t, y1+3*ysd1, 'b:', t, y1-3*ysd1, 'b:')
hold on
plot(t, y2, 'g', t, y2+3*ysd2, 'g:', t, y2-3*ysd2, 'g:')
```



Validate Linearization of Identified Nonlinear ARX Model

Validate the linearization of a nonlinear ARX model by comparing the small amplitude step responses of the linear and nonlinear models.

Load the data.

load iddata2 z2;

Estimate a nonlinear ARX model.

 $nlsys = nlarx(z2,[4 \ 3 \ 10], 'tree', 'custom', {'sin(y1(t-2)*u1(t))+y1(t-2)*u1(t)+u1(t).*u1}$

Determine an equilibrium operating point for nlsys corresponding to a steady-state input value of 1.

```
u0 = 1;
[X,~,r] = findop(nlsys, 'steady', 1);
y0 = r.SignalLevels.Output;
```

Obtain a linear approximation of nlsys at this operating point.

```
sys = linearize(nlsys,u0,X);
```

Validate the usefulness of sys by comparing its small-amplitude step response to that of nlsys.

The nonlinear system nlsys is operating at an equilibrium level dictated by (u0, y0). Introduce a step perturbation of size 0.1 about this steady-state and compute the corresponding response.

```
opt = stepDataOptions;
opt.InputOffset = u0;
opt.StepAmplitude = 0.1;
t = (0:0.1:10)';
ynl = step(nlsys, t, opt);
```

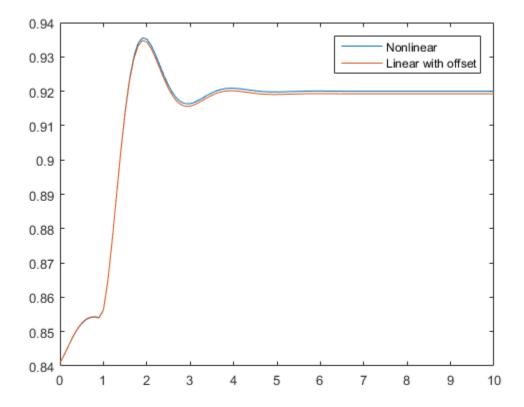
The linear system **sys** expresses the relationship between the perturbations in input to the corresponding perturbation in output. It is unaware of the nonlinear system's equilibrium values.

Plot the step response of the linear system.

```
opt = stepDataOptions;
opt.StepAmplitude = 0.1;
yl = step(sys, t, opt);
```

Add the steady-state offset, y0 , to the response of the linear system and plot the responses.

```
plot(t, ynl, t, yl+y0)
legend('Nonlinear', 'Linear with offset')
```



Step Response of Identified Time-Series Model

Compute the step response of an identified time-series model.

A time-series model, also called a signal model, is one without measured input signals. The step plot of this model uses its (unmeasured) noise channel as the input channel to which the step signal is applied.

Load the data.

load iddata9;

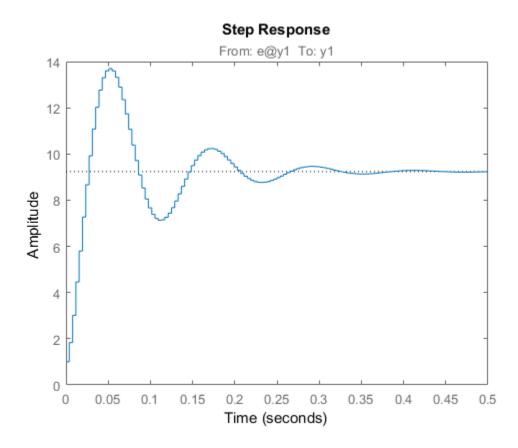
Estimate a time-series model.

sys = ar(z9, 4);

ys is a model of the form A y(t) = e(t), where e(t) represents the noise channel. For computation of step response, e(t) is treated as an input channel, and is named e@y1.

Plot the step response.

step(sys)



More About

Tips

You can change the properties of your plot, for example the units. For information on the ways to change properties of your plots, see "Ways to Customize Plots".

Algorithms

Continuous-time models without internal delays are converted to state space and discretized using zero-order hold on the inputs. The sample time is chosen automatically based on the system dynamics, except when a time vector t = 0:dt:Tf is supplied (dt

is then used as sampling period). The resulting simulation time steps ${\tt t}$ are equisampled with spacing ${\tt dt}.$

For systems with internal delays, Control System Toolbox software uses variable step solvers. As a result, the time steps t are not equisampled.

References

[1] L.F. Shampine and P. Gahinet, "Delay-differential-algebraic equations in control theory," *Applied Numerical Mathematics*, Vol. 56, Issues 3–4, pp. 574–588.

See Also

stepDataOptions | lsim | impulse | initial | linearSystemAnalyzer

Introduced before R2006a

stepDataOptions

Options set for step

Syntax

opt = stepDataOptions
opt = stepDataOptions(Name,Value)

Description

opt = stepDataOptions creates the default options for step.

opt = stepDataOptions(Name,Value) creates an options set with the options
specified by one or more Name,Value pair arguments.

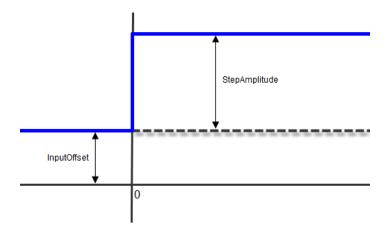
Input Arguments

Name-Value Pair Arguments

Specify optional comma-separated pairs of Name, Value arguments. Name is the argument name and Value is the corresponding value. Name must appear inside single quotes (' '). You can specify several name and value pair arguments in any order as Name1, Value1, ..., NameN, ValueN.

'InputOffset'

Input signal level for all time t < 0, as shown in the next figure.



Default: 0

'StepAmplitude'

Change of input signal level which occurs at time t = 0, as shown in the previous figure.

Default: 1

Output Arguments

opt

Option set containing the specified options for step.

Examples

Specify Input Offset and Step Amplitude Level

Specify the input offset and amplitude level for step response.

```
sys = tf(1,[1,1]);
opt = stepDataOptions('InputOffset',-1,'StepAmplitude',2);
[y,t] = step(sys,opt)
```

See Also

step

Introduced in R2012a

stepinfo

Rise time, settling time, and other step response characteristics

Syntax

```
S = stepinfo(y,t,yfinal)
S = stepinfo(y,t)
S = stepinfo(y)
S = stepinfo(sys)
S = stepinfo(...,'SettlingTimeThreshold',ST)
S = stepinfo(...,'RiseTimeLimits',RT)
```

Description

S = stepinfo(y,t,yfinal) takes step response data (t,y) and a steady-state value yfinal and returns a structure S containing the following performance indicators:

- RiseTime Rise time
- SettlingTime Settling time
- · SettlingMin Minimum value of y once the response has risen
- SettlingMax Maximum value of y once the response has risen
- Overshoot Percentage overshoot (relative to yfinal)
- Undershoot Percentage undershoot
- Peak Peak absolute value of y
- PeakTime Time at which this peak is reached

For SISO responses, t and y are vectors with the same length NS. For systems with NU inputs and NY outputs, you can specify y as an NS-by-NY-by-NU array (see step) and yfinal as an NY-by-NU array. stepinfo then returns a NY-by-NU structure array S of performance metrics for each I/O pair.

S = stepinfo(y,t) uses the last sample value of y as steady-state value yfinal. S =
stepinfo(y) assumes t = 1:ns.

S = stepinfo(sys)computes the step response characteristics for an LTI model sys (see tf, zpk, or ss for details).

S = stepinfo(..., 'SettlingTimeThreshold', ST) lets you specify the threshold ST used in the settling time calculation. The response has settled when the error |y(t) - yfinal| becomes smaller than a fraction ST of its peak value. The default value is ST=0.02 (2%).

S = stepinfo(..., 'RiseTimeLimits', RT) lets you specify the lower and upper thresholds used in the rise time calculation. By default, the rise time is the time the response takes to rise from 10 to 90% of the steady-state value (RT=[0.1 0.9]). Note that RT(2) is also used to calculate SettlingMin and SettlingMax.

Examples

Step Response Characteristics of Fifth-Order System

Create a fifth order system and ascertain the response characteristics.

sys = tf([1 5],[1 2 5 7 2]); S = stepinfo(sys,'RiseTimeLimits',[0.05,0.95])

These commands return the following result:

S =

```
RiseTime: 7.4454
SettlingTime: 13.9378
SettlingMin: 2.3737
SettlingMax: 2.5201
Overshoot: 0.8032
Undershoot: 0
Peak: 2.5201
PeakTime: 15.1869
```

See Also

lsiminfo | step

Introduced in R2006a

stepplot

Plot step response and return plot handle

Syntax

```
h = stepplot(sys)
stepplot(sys,Tfinal)
stepplot(sys,t)
stepplot(sys1,sys2,...,sysN)
stepplot(sys1,sys2,...,sysN,Tfinal)
stepplot(sys1,sys2,...,sysN,t)
stepplot(AX,...)
stepplot(..., plotoptions)
stepplot(..., dataoptions)
```

Description

h = stepplot(sys) plots the step response of the dynamic system model sys. It also returns the plot handle h. You can use this handle to customize the plot with the getoptions and setoptions commands. Type

help timeoptions

for a list of available plot options.

For multiinput models, independent step commands are applied to each input channel. The time range and number of points are chosen automatically.

stepplot(sys,Tfinal) simulates the step response from t = 0 to the final time t =
Tfinal. Express Tfinal in the system time units, specified in the TimeUnit property
of sys. For discrete-time systems with unspecified sample time (Ts = -1), stepplot
interprets Tfinal as the number of sampling intervals to simulate.

stepplot(sys,t) uses the user-supplied time vector t for simulation. Express t in the system time units, specified in the TimeUnit property of sys. For discrete-time models, t should be of the form Ti:Ts:Tf, where Ts is the sample time. For continuoustime models, t should be of the form Ti:dt:Tf, where dt becomes the sample time of a discrete approximation to the continuous system (see step). The stepplot command always applies the step input at t=0, regardless of Ti.

To plot the step responses of multiple models sys1,sys2,... on a single plot, use:

```
stepplot(sys1,sys2,...,sysN)
```

stepplot(sys1,sys2,...,sysN,Tfinal)

stepplot(sys1,sys2,...,sysN,t)

You can also specify a color, line style, and marker for each system, as in

stepplot(sys1,'r',sys2,'y--',sys3,'gx')

stepplot(AX,...) plots into the axes with handle AX.

stepplot(..., plotoptions) customizes the plot appearance using the options set, plotoptions. Use timeOptions to create the options set.

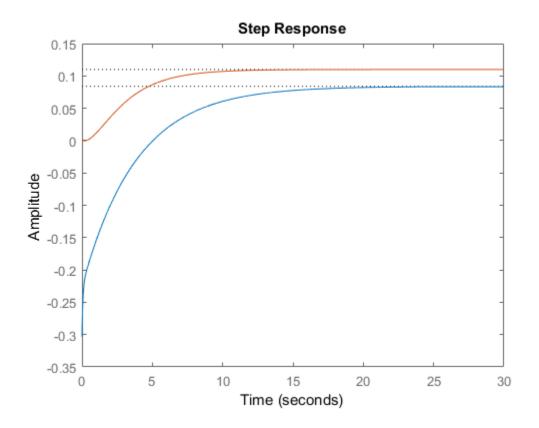
stepplot(..., dataoptions) specifies options such as the step amplitude and input
offset using the options set, dataoptions. Use stepDataOptions to create the options
set.

Examples

Normalized Response on Step Plot

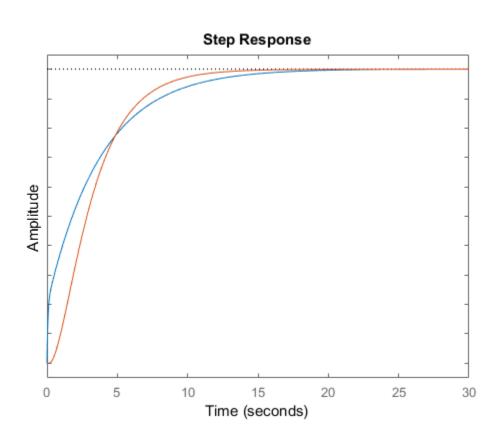
Generate a step response plot for two dynamic systems.

```
sys1 = rss(3);
sys2 = rss(3);
h = stepplot(sys1,sys2);
```



Each step response settles at a different steady-state value. Use the plot handle to normalize the plotted response.

setoptions(h, 'Normalize', 'on')



Now, the responses settle at the same value expressed in arbitrary units.

Step Responses of Identified Models with Confidence Region

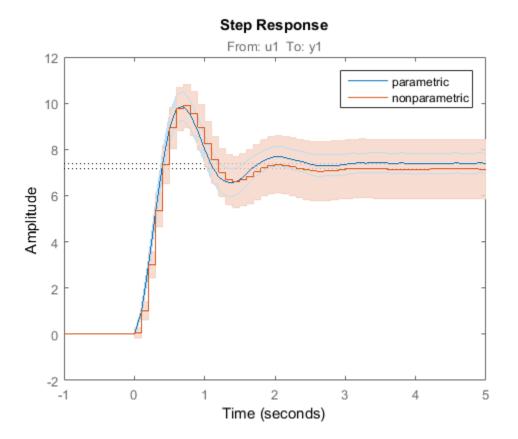
Compare the step response of a parametric identified model to a nonparametric (empirical) model, and view their 3- σ confidence regions. (Identified models require System Identification ToolboxTM software.)

Identify a parametric and a nonparametric model from sample data.

```
load iddata1 z1
sys1 = ssest(z1,4);
sys2 = impulseest(z1);
```

Plot the step responses of both identified models. Use the plot handle to display the 3- σ confidence regions.

```
t = -1:0.1:5;
h = stepplot(sys1,sys2,t);
showConfidence(h,3)
legend('parametric','nonparametric')
```



The nonparametric model sys2 shows higher uncertainty.

Step Response of Nonlinear Model

Plot the step response of a nonlinear (Hammerstein-Wiener) model using a starting offset of 2 and step amplitude of 0.5. (Hammerstein-Weiner models require System Identification Toolbox software.)

```
load twotankdata
z = iddata(y, u, 0.2, 'Name', 'Two tank system');
sys = nlhw(z, [1 5 3], pwlinear, poly1d);
dataoptions = stepDataOptions('InputOffset', 2, 'StepAmplitude', 0.5);
stepplot(sys,60,dataoptions);
```

More About

Tips

You can change the properties of your plot, for example the units. For information on the ways to change properties of your plots, see "Ways to Customize Plots".

See Also

setoptions | getoptions | step

Introduced before R2006a

strseq

Create sequence of indexed strings

Syntax

```
strvec = strseq(STR,INDICES)
```

Description

strvec = strseq(STR, INDICES) creates a sequence of indexed strings in the string
vector strvec by appending the integer values INDICES to the string STR.

Note: You can use **strvec** to aid in system interconnection. For an example, see the **sumblk** reference page.

Examples

Create a string vector by indexing the string e' at 1, 2, and 4.

```
strseq('e',[1 2 4])
This command returns the following result:
```

ans =

'e1' 'e2' 'e4'

See Also

strcat | connect

Introduced in R2008b

sumblk

Summing junction for name-based interconnections

Syntax

```
S = sumblk(formula)
```

```
S = sumblk(formula,signalsize)
```

```
S = sumblk(formula,signames1,signames2,...)
```

Description

S = sumblk(formula) creates the transfer function, S, of the summing junction described by the string formula. The string formula specifies an equation that relates the scalar input and output signals of S.

S = sumblk(formula, signalsize) returns a vector-valued summing junction. The input and output signals are vectors with signalsize elements.

S = sumblk(formula, signames1, signames2,...) replaces aliases (signal names beginning with %) in formula by the signal names signames. The number of signames arguments must match the number of aliases in formula. The first alias in formula is replaced by signames1, the second by signames2, and so on.

Input Arguments

formula

String specifying the equation that relates the input and output signals of the summing junction transfer function S. For example, the following command:

S = sumblk('e = r - y + d')

creates a summing junction with input names 'r', 'y', and 'd', output name 'e' and equation e = r-y+d.

If you specify a **signalsize** greater than 1, the inputs and outputs of **S** are vectorvalued signals. **sumblk** automatically performs vector expansion of the signal names of **S**. For example, the following command:

S = sumblk('v = u + d', 2)

specifies a summing junction with input names {'u(1)'; 'u(2)'; 'd(1)'; 'd(2)'} and output names {'v(1)'; 'v(2)'}. The formulas of this summing junction are v(1) = u(1) + d(1); v(2) = u(2) + d(2).

You can use one or more aliases in formula to refer to signal names defined in a variable. An alias is a signal name that begins with %. When formula contains aliases, sumblk replaces each alias with the corresponding signames argument.

Aliases are useful when you want to name individual entries in a vector-valued signal. Aliases also allow you to use input or output names of existing models. For example, if C and G are dynamic system models with nonempty InputName and OutputName properties, respectively, you can create a summing junction using the following expression.

S = sumblk('%e = r - %y',C.InputName,G.OutputName)

sumblk uses the values of C.InputName and G.OutputName in place of %e and %y,
respectively. The vector dimension of C.InputName and G.OutputName must match.
sumblk assigns the signal r the same dimension.

signalsize

Number of elements in each input and output signal of S. Setting signalsize greater than 1 lets you specify a summing junction that operates on vector-valued signals.

Default: 1

signames

Signal names to replace one alias (signal name beginning with %) in the formula string. You must provide one signames argument for each alias in formula.

Specify signames as:

- A cell array of name strings.
- The InputName or OutputName property of a model in the MATLAB workspace. For example:

S = sumblk('%e = r - y',C.InputName)

This command creates a summing junction whose outputs have the same name as the inputs of the model C in the MATLAB workspace.

Output Arguments

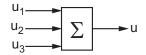
S

Transfer function for the summing junction, represented as a MIMO tf model object.

Examples

Summing Junction with Scalar-Valued Signals

Create the summing junction of the following illustration. All signals are scalar-valued.



This summing junction has the formula u = u1 + u2 + u3.

S = sumblk('u = u1+u2+u3');

S is the transfer function (tf) representation of the sum u = u1 + u2 + u3. The transfer function S gets its input and output names from the formula string.

S.OutputName, S.Inputname

ans = 'u' ans = 'u1' 'u2' 'u3'

Summing Junction with Vector-Valued Signals

Create the summing junction v = u - d where u, d, v are vector-valued signals of length 2.

S = sumblk('v = u-d', 2);

sumblk automatically performs vector expansion of the signal names of S.

S.OutputName, S.Inputname

ans =

'v(1)' 'v(2)'

ans =

'u(1)' 'u(2)' 'd(1)' 'd(2)'

Summing Junction with Vector-Valued Signals That Have Specified Signal Names

Create the summing junction

e(1) = setpoint(1) - alpha + d(1)e(2) = setpoint(2) - q + d(2)

The signals alpha and q have custom names that are not merely the vector expansion of a single signal name. Therefore, use an alias in the formula specifying the summing junction.

```
S = sumblk('e = setpoint - %y + d', {'alpha';'q'});
```

sumblk replaces the alias %y with the cell array { 'alpha'; 'q'}.

S.OutputName, S.Inputname

```
ans =
    'e(1)'
    'e(2)'
ans =
    'setpoint(1)'
    'setpoint(2)'
    'alpha'
    'q'
    'd(1)'
    'd(2)'
```

More About

Tips

- Use sumblk in conjunction with connect to interconnect dynamic system models and derive aggregate models for block diagrams.
- "Multi-Loop Control System"
- "MIMO Control System"

See Also

connect | series | parallel | strseq

Introduced in R2008a

ff

Create transfer function model, convert to transfer function model

Syntax

```
sys = tf(num,den)
sys = tf(num,den,Ts)
sys = tf(M)
sys = tf(num,den,ltisys)
tfsys = tf(sys)
tfsys = tf(sys, 'measured')
tfsys = tf(sys, 'noise')
tfsys = tf(sys, 'augmented')
```

Description

Use tf to create real- or complex-valued transfer function models (TF objects) or to convert state-space or zero-pole-gain models to transfer function form. You can also use tf to create generalized state-space (genss) models or uncertain state-space (uss) models.

Creation of Transfer Functions

sys = tf(num,den) creates a continuous-time transfer function with numerator(s)
and denominator(s) specified by num and den. The output sys is:

- A tf model object, when num and den are numeric arrays.
- A generalized state-space model (genss) when num or den include tunable parameters, such as realp parameters or generalized matrices (genmat).
- An uncertain state-space model (**uss**) when **num** or **den** are uncertain (requires Robust Control Toolbox software).

In the SISO case, num and den are the real- or complex-valued row vectors of numerator and denominator coefficients ordered in *descending* powers of s. These two vectors need not have equal length and the transfer function need not be proper. For example, $h = tf([1 \ 0], 1)$ specifies the pure derivative h(s) = s.

To create MIMO transfer functions, using one of the following approaches:

- Concatenate SISO tf models.
- Use the tf command with cell array arguments. In this case, num and den are cell arrays of row vectors with as many rows as outputs and as many columns as inputs. The row vectors num{i,j} and den{i,j} specify the numerator and denominator of the transfer function from input j to output i.

For examples of creating MIMO transfer functions, see "Examples" on page 1-845 and "MIMO Transfer Functions" in the *Control System Toolbox User Guide*.

If all SISO entries of a MIMO transfer function have the same denominator, you can set den to the row vector representation of this common denominator. See "Examples" for more details.

sys = tf(num, den, Ts) creates a discrete-time transfer function with sample time Ts (in seconds). Set Ts = -1 to leave the sample time unspecified. The input arguments num and den are as in the continuous-time case and must list the numerator and denominator coefficients in *descending* powers of z.

sys = tf(M) creates a static gain M (scalar or matrix).

sys = tf(num,den,ltisys) creates a transfer function with properties inherited
from the dynamic system model ltisys (including the sample time).

There are several ways to create arrays of transfer functions. To create arrays of SISO or MIMO TF models, either specify the numerator and denominator of each SISO entry using multidimensional cell arrays, or use a for loop to successively assign each TF model in the array. See "Model Arrays".

Any of the previous syntaxes can be followed by property name/property value pairs

'Property',Value

Each pair specifies a particular property of the model, for example, the input names or the transfer function variable. For information about the properties of tf objects, see "Properties" on page 1-851. Note that

```
sys = tf(num,den,'Property1',Value1,...,'PropertyN',ValueN)
```

is a shortcut for

```
sys = tf(num,den)
set(sys,'Property1',Value1,...,'PropertyN',ValueN)
```

Transfer Functions as Rational Expressions in s or z

You can also use real- or complex-valued rational expressions to create a TF model. To do so, first type either:

- s = tf('s') to specify a TF model using a rational function in the Laplace variable,
 s.
- z = tf('z', Ts) to specify a TF model with sample time Ts using a rational function in the discrete-time variable, z.

Once you specify either of these variables, you can specify TF models directly as rational expressions in the variable s or z by entering your transfer function as a rational expression in either s or z.

Conversion to Transfer Function

tfsys = tf(sys) converts the dynamic system model sys to transfer function form. The output tfsys is a tf model object representing sys expressed as a transfer function.

If sys is a model with tunable components, such as a genss, genmat, ltiblock.tf, or ltiblock.ss model, the resulting transfer function tfsys takes the current values of the tunable components.

Conversion of Identified Models

An identified model is represented by an input-output equation of the form y(t) = Gu(t) + He(t), where u(t) is the set of measured input channels and e(t) represents the noise channels. If $\Lambda = LL'$ represents the covariance of noise e(t), this equation can also be written as: y(t) = Gu(t) + HLv(t), where cov(v(t)) = I.

tfsys = tf(sys), or tfsys = tf(sys, 'measured') converts the measured component of an identified linear model into the transfer function form. sys is a model of type idss, idproc, idtf, idpoly, or idgrey. tfsys represents the relationship between u and y.

tfsys = tf(sys, 'noise') converts the noise component of an identified linear model into the transfer function form. It represents the relationship between the noise input, v(t) and output, y_noise = HL v(t). The noise input channels belong to the InputGroup 'Noise'. The names of the noise input channels are v@yname, where yname is the name of the corresponding output channel. tfsys has as many inputs as outputs.

tfsys = tf(sys, 'augmented') converts both the measured and noise dynamics into a transfer function. tfsys has ny+nu inputs such that the first nu inputs represent the channels u(t) while the remaining by channels represent the noise channels v(t). tfsys.InputGroup contains 2 input groups- 'measured' and 'noise'. tfsys.InputGroup.Measured is set to 1:nu while tfsys.InputGroup.Noise is set to nu+1:nu+ny.tfsys represents the equation y(t) = [G HL] [u; v].

Tip An identified nonlinear model cannot be converted into a transfer function. Use linear approximation functions such as linearize and linapp.

Creation of Generalized State-Space Models

You can use the syntax:

gensys = tf(num,den)

to create a Generalized state-space (genss) model when one or more of the entries num and den depends on a tunable realp or genmat model. For more information about Generalized state-space models, see "Models with Tunable Coefficients".

Examples

Transfer Function Model with One-Input Two-Outputs

Create the one-input, two-output transfer function

$$H\left(p\right) = \begin{bmatrix} \frac{p+1}{p^2 + 2p + 2} \\ \frac{1}{p} \end{bmatrix}$$

with input current and outputs torque and ang velocity.

To do this, enter

```
num = {[1 1] ; 1};
den = {[1 2 2] ; [1 0]};
H = tf(num,den,'inputn','current',...
```

```
'outputn',{'torque' 'ang. velocity'},...
'variable','p')
```

These commands produce the result:

Setting the 'variable' property to 'p' causes the result to be displayed as a transfer function of the variable p.

Transfer Function Model Using Rational Expression

To use a rational expression to create a SISO TF model, type

s = tf('s');H = s/(s² + 2*s +10);

This produces the same transfer function as

h = tf([1 0], [1 2 10]);

Second-Order Transfer Function from Damping and Natural Frequency

Create a tf model that represents a second-order system with known natural frequency and damping ratio.

The transfer function of a second-order system, expressed in terms of its damping ratio ζ and natural frequency ω_0 , is:

$$H\left(s\right) = \frac{\omega_0^2}{s^2 + 2\zeta\omega_0 s + \omega_0^2}.$$

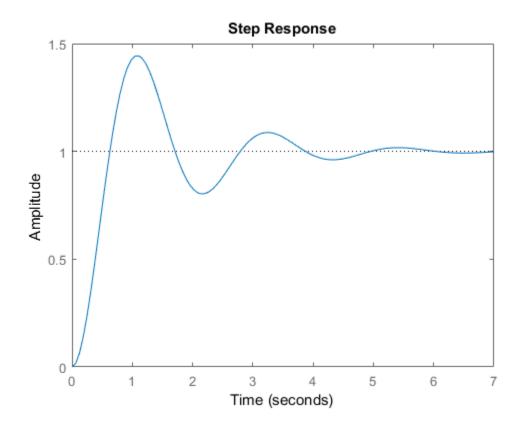
Represent this transfer function in MATLAB using the tf command. For example, suppose you have a system with $\zeta=0.25$ and $\omega_0=3$ rad/s.

zeta = 0.25; w0 = 3;

Continuous-time transfer function.

 $\ensuremath{\mathsf{Examine}}$ the response of this transfer function to a step input.

stepplot(H)



The plot shows the ringdown expected of a second-order system with a low damping ratio.

Multiple-Input Multiple-Output Transfer Function Model

Specify the discrete MIMO transfer function

$$H(z) = \begin{bmatrix} \frac{1}{z+0.3} & \frac{z}{z+0.3} \\ \frac{-z+2}{z+0.3} & \frac{3}{z+0.3} \end{bmatrix}$$

with common denominator d(z) = z + 0.3 and sample time of 0.2 seconds.

nums = {1 [1 0];[-1 2] 3}; Ts = 0.2; H = tf(nums,[1 0.3],Ts) % Note: row vector for common den. d(z)

Convert State-Space Model to Transfer Function

Compute the transfer function of the state-space model with the following data.

$$A = \begin{bmatrix} -2 & -1 \\ 1 & -2 \end{bmatrix}, \quad B = \begin{bmatrix} 1 & 1 \\ 2 & -1 \end{bmatrix}, \quad C = \begin{bmatrix} 1 & 0 \end{bmatrix}, \quad D = \begin{bmatrix} 0 & 1 \end{bmatrix}.$$

To do this, type

sys = ss([-2 -1;1 -2],[1 1;2 -1],[1 0],[0 1]);
tf(sys)

These commands produce the result:

```
Transfer function from input 1 to output:

s - 4.441e-016

s^2 + 4 s + 5

Transfer function from input 2 to output:

s^2 + 5 s + 8

s^2 + 4 s + 5
```

Array of Transfer Function Models

You can use a for loop to specify a 10-by-1 array of SISO TF models.

```
H = tf(zeros(1,1,10));
s = tf('s')
for k=1:10,
H(:,:,k) = k/(s^2+s+k);
end
```

The first statement pre-allocates the TF array and fills it with zero transfer functions.

Tunable Low-Pass Filter

This example shows how to create the low-pass filter F = a/(s + a) with one tunable parameter *a*.

You cannot use ltiblock.tf to represent F, because the numerator and denominator coefficients of an ltiblock.tf block are independent. Instead, construct F using the tunable real parameter object realp.

1 Create a tunable real parameter.

a = realp('a',10);

The realp object **a** is a tunable parameter with initial value 10.

2 Use tf to create the tunable filter F:

F = tf(a,[1 a]);

F is a genss object which has the tunable parameter a in its Blocks property. You can connect F with other tunable or numeric models to create more complex models of control systems. For an example, see "Control System with Tunable Components".

Extract Transfer Functions from Identified Model

Extract the measured and noise components of an identified polynomial model into two separate transfer functions (requires System Identification Toolbox). The measured component can serve as a plant model, while the noise component can serve as a disturbance model for control system design.

```
load icEngine;
z = iddata(y,u,0.04);
```

nb = 2; nf = 2; nc = 1; nd = 3; nk = 3; sys = bj(z, [nb nc nd nf nk]);

sys is a model of the form: y(t) = B/F u(t) + C/D e(t), where B/F represents the measured component and C/D the noise component.

```
sysMeas = tf(sys, 'measured')
sysNoise = tf(sys, 'noise')
```

Alternatively, use can simply use tf(sys) to extract the measured component.

Discrete-Time Conventions

The control and digital signal processing (DSP) communities tend to use different conventions to specify discrete transfer functions. Most control engineers use the z variable and order the numerator and denominator terms in descending powers of z, for example,

$$h(z) = \frac{z^2}{z^2 + 2z + 3}.$$

The polynomials z^2 and $z^2 + 2z + 3$ are then specified by the row vectors $\begin{bmatrix} 1 & 0 & 0 \end{bmatrix}$ and $\begin{bmatrix} 1 \\ 2 & 3 \end{bmatrix}$, respectively. By contrast, DSP engineers prefer to write this transfer function as

$$h\left(z^{-1}\right) = \frac{1}{1 + 2z^{-1} + 3z^{-2}}$$

and specify its numerator as 1 (instead of $\begin{bmatrix} 1 & 0 & 0 \end{bmatrix}$) and its denominator as $\begin{bmatrix} 1 & 2 & 3 \end{bmatrix}$.

tf switches convention based on your choice of variable (value of the 'Variable' property).

Variable	Convention
'z' (default), 'q'	Use the row vector [ak \dots a1 a0] to specify the polynomial
	$a_k z^k + + a_1 z + a_0$ (coefficients ordered in <i>descending</i> powers of z or q).
'z^-1'	Use the row vector [b0 b1 bk] to specify the polynomial
	$b_0 + b_1 z^{-1} + + b_k z^{-k}$ (coefficients in ascending powers of z^{-1}).

For example,

 $g = tf([1 \ 1], [1 \ 2 \ 3], 0.1);$

specifies the discrete transfer function

$$g(z) = \frac{z+1}{z^2+2z+3}$$

because z is the default variable. In contrast,

uses the DSP convention and creates

$$h(z^{-1}) = \frac{1+z^{-1}}{1+2z^{-1}+3z^{-2}} = zg(z).$$

See also filt for direct specification of discrete transfer functions using the DSP convention.

Note that tf stores data so that the numerator and denominator lengths are made equal. Specifically, tf stores the values

for g (the numerator is padded with zeros on the left) and the values

num = [1 1 0]; den = [1 2 3];

for h (the numerator is padded with zeros on the right).

Properties

tf objects have the following properties:

num

Transfer function numerator coefficients.

For SISO transfer functions, num is a row vector of polynomial coefficients in order of descending power (for Variable values s, z, p, or q) or in order of ascending power (for Variable values z^{-1} or q^{-1}).

For MIMO transfer functions with Ny outputs and Nu inputs, num is a Ny-by-Nu cell array of the numerator coefficients for each input/output pair.

den

Transfer function denominator coefficients.

For SISO transfer functions, den is a row vector of polynomial coefficients in order of descending power (for Variable values s, z, p, or q) or in order of ascending power (for Variable values z^{-1} or q^{-1}).

For MIMO transfer functions with Ny outputs and Nu inputs, den is a Ny-by-Nu cell array of the denominator coefficients for each input/output pair.

Variable

String specifying the transfer function display variable. Variable can take the following values:

- 's' Default for continuous-time models
- 'z' Default for discrete-time models
- 'p' Equivalent to 's'
- 'q' Equivalent to 'z'
- 'z^-1' Inverse of 'z'
- 'q^-1' Equivalent to 'z^-1'

The value of Variable is reflected in the display, and also affects the interpretation of the num and den coefficient vectors for discrete-time models. For Variable = 'z' or 'q', the coefficient vectors are ordered in descending powers of the variable. For Variable = 'z^-1' or 'q^-1', the coefficient vectors are ordered as ascending powers of the variable.

Default: 'S'

ioDelay

Transport delays. **ioDelay** is a numeric array specifying a separate transport delay for each input/output pair.

For continuous-time systems, specify transport delays in the time unit stored in the TimeUnit property. For discrete-time systems, specify transport delays in integer multiples of the sample time, TS.

For a MIMO system with Ny outputs and Nu inputs, set ioDelay to a Ny-by-Nu array. Each entry of this array is a numerical value that represents the transport delay for the corresponding input/output pair. You can also set ioDelay to a scalar value to apply the same delay to all input/output pairs.

Default: 0 for all input/output pairs

InputDelay

Input delay for each input channel, specified as a scalar value or numeric vector. For continuous-time systems, specify input delays in the time unit stored in the TimeUnit property. For discrete-time systems, specify input delays in integer multiples of the sample time Ts. For example, InputDelay = 3 means a delay of three sample times.

For a system with Nu inputs, set InputDelay to an Nu-by-1 vector. Each entry of this vector is a numerical value that represents the input delay for the corresponding input channel.

You can also set InputDelay to a scalar value to apply the same delay to all channels.

Default: 0

OutputDelay

Output delays. OutputDelay is a numeric vector specifying a time delay for each output channel. For continuous-time systems, specify output delays in the time unit stored in the TimeUnit property. For discrete-time systems, specify output delays in integer multiples of the sample time TS. For example, OutputDelay = 3 means a delay of three sampling periods.

For a system with Ny outputs, set OutputDelay to an Ny-by-1 vector, where each entry is a numerical value representing the output delay for the corresponding output channel. You can also set OutputDelay to a scalar value to apply the same delay to all channels.

Default: 0 for all output channels

Ts

Sample time. For continuous-time models, Ts = 0. For discrete-time models, Ts is a positive scalar representing the sampling period. This value is expressed in the unit specified by the TimeUnit property of the model. To denote a discrete-time model with unspecified sample time, set Ts = -1.

Changing this property does not discretize or resample the model. Use c2d and d2c to convert between continuous- and discrete-time representations. Use d2d to change the sample time of a discrete-time system.

Default: 0 (continuous time)

TimeUnit

String representing the unit of the time variable. This property specifies the units for the time variable, the sample time Ts, and any time delays in the model. Use any of the following values:

- 'nanoseconds'
- 'microseconds'
- 'milliseconds'
- 'seconds'
- 'minutes'
- 'hours'
- 'days'
- 'weeks'
- 'months'
- 'years'

Changing this property has no effect on other properties, and therefore changes the overall system behavior. Use chgTimeUnit to convert between time units without modifying system behavior.

Default: 'seconds'

InputName

Input channel names. Set InputName to a string for single-input model. For a multiinput model, set InputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign input names for multi-input models. For example, if **sys** is a two-input model, enter:

```
sys.InputName = 'controls';
```

The input names automatically expand to { 'controls(1) '; 'controls(2) '}.

You can use the shorthand notation u to refer to the InputName property. For example, sys.u is equivalent to sys.InputName.

Input channel names have several uses, including:

- · Identifying channels on model display and plots
- Extracting subsystems of MIMO systems
- Specifying connection points when interconnecting models

Default: Empty string ' ' for all input channels

InputUnit

Input channel units. Use InputUnit to keep track of input signal units. For a singleinput model, set InputUnit to a string. For a multi-input model, set InputUnit to a cell array of strings. InputUnit has no effect on system behavior.

Default: Empty string ' ' for all input channels

InputGroup

Input channel groups. The InputGroup property lets you assign the input channels of MIMO systems into groups and refer to each group by name. Specify input groups as a structure. In this structure, field names are the group names, and field values are the input channels belonging to each group. For example:

```
sys.InputGroup.controls = [1 2];
sys.InputGroup.noise = [3 5];
```

creates input groups named controls and noise that include input channels 1, 2 and 3, 5, respectively. You can then extract the subsystem from the controls inputs to all outputs using:

```
sys(:,'controls')
```

Default: Struct with no fields

OutputName

Output channel names. Set OutputName to a string for single-output model. For a multioutput model, set OutputName to a cell array of strings. Alternatively, use automatic vector expansion to assign output names for multi-output models. For example, if **sys** is a two-output model, enter:

```
sys.OutputName = 'measurements';
```

The output names automatically expand to { 'measurements(1)'; 'measurements(2)'}.

You can use the shorthand notation y to refer to the OutputName property. For example, sys.y is equivalent to sys.OutputName.

Output channel names have several uses, including:

- · Identifying channels on model display and plots
- · Extracting subsystems of MIMO systems
- · Specifying connection points when interconnecting models

Default: Empty string ' ' for all output channels

OutputUnit

Output channel units. Use OutputUnit to keep track of output signal units. For a single-output model, set OutputUnit to a string. For a multi-output model, set OutputUnit to a cell array of strings. OutputUnit has no effect on system behavior.

Default: Empty string ' ' for all output channels

OutputGroup

Output channel groups. The OutputGroup property lets you assign the output channels of MIMO systems into groups and refer to each group by name. Specify output groups as a structure. In this structure, field names are the group names, and field values are the output channels belonging to each group. For example:

```
sys.OutputGroup.temperature = [1];
sys.InputGroup.measurement = [3 5];
```

creates output groups named temperature and measurement that include output channels 1, and 3, 5, respectively. You can then extract the subsystem from all inputs to the measurement outputs using:

```
sys('measurement',:)
```

Default: Struct with no fields

Name

System name. Set Name to a string to label the system.

Default: ' '

Notes

Any text that you want to associate with the system. Set **Notes** to a string or a cell array of strings.

Default: { }

UserData

Any type of data you want to associate with system. Set UserData to any MATLAB data type.

Default: []

SamplingGrid

Sampling grid for model arrays, specified as a data structure.

For model arrays that are derived by sampling one or more independent variables, this property tracks the variable values associated with each model in the array. This information appears when you display or plot the model array. Use this information to trace results back to the independent variables.

Set the field names of the data structure to the names of the sampling variables. Set the field values to the sampled variable values associated with each model in the array. All sampling variables should be numeric and scalar valued, and all arrays of sampled values should match the dimensions of the model array.

For example, suppose you create a 11-by-1 array of linear models, sysarr, by taking snapshots of a linear time-varying system at times t = 0:10. The following code stores the time samples with the linear models.

```
sysarr.SamplingGrid = struct('time',0:10)
```

Similarly, suppose you create a 6-by-9 model array, M, by independently sampling two variables, zeta and w. The following code attaches the (zeta,w) values to M.

[zeta,w] = ndgrid(<6 values of zeta>,<9 values of w>)

```
M.SamplingGrid = struct('zeta',zeta,'w',w)
```

When you display M, each entry in the array includes the corresponding zeta and w values.

For model arrays generated by linearizing a Simulink model at multiple parameter values or operating points, the software populates SamplingGrid automatically with the variable values that correspond to each entry in the array. For example, the Simulink Control Design commands linearize and slLinearizer populate SamplingGrid in this way.

Default: []

More About

Algorithms

tf uses the MATLAB function poly to convert zero-pole-gain models, and the functions zero and pole to convert state-space models.

• "What Are Model Objects?"

See Also

```
filt | frd | get | set | ss | tfdata | zpk | genss | realp | genmat |
ltiblock.tf
```

Introduced before R2006a

tfdata

Access transfer function data

Syntax

```
[num,den] = tfdata(sys)
[num,den,Ts] = tfdata(sys)
[num,den,Ts,sdnum,sdden]=tfdata(sys)
[num,den,Ts,...]=tfdata(sys,J1,...,Jn)
```

Description

[num,den] = tfdata(sys) returns the numerator(s) and denominator(s) of the transfer function for the TF, SS or ZPK model (or LTI array of TF, SS or ZPK models) sys. For single LTI models, the outputs num and den of tfdata are cell arrays with the following characteristics:

- num and den have as many rows as outputs and as many columns as inputs.
- The (i, j) entries num{i, j} and den{i, j} are row vectors specifying the numerator and denominator coefficients of the transfer function from input j to output i. These coefficients are ordered in *descending* powers of s or z.

For arrays ${\tt sys}$ of LTI models, ${\tt num}$ and ${\tt den}$ are multidimensional cell arrays with the same sizes as ${\tt sys}.$

If sys is a state-space or zero-pole-gain model, it is first converted to transfer function form using tf. For more information on the format of transfer function model data, see the tf reference page.

For SISO transfer functions, the syntax

[num,den] = tfdata(sys,'v')

forces tfdata to return the numerator and denominator directly as row vectors rather than as cell arrays (see example below).

[num,den,Ts] = tfdata(sys) also returns the sample time Ts.

[num,den,Ts,sdnum,sdden]=tfdata(sys) also returns the uncertainties in the numerator and denominator coefficients of identified system sys. $sdnum{i,j}(k)$ is the 1 standard uncertainty in the value $num{i,j}(k)$ and $sdden{i,j}(k)$ is the 1 standard uncertainty in the value $den{i,j}(k)$. If sys does not contain uncertainty information, sdnum and sdden are empty ([]).

[num,den,Ts,...]=tfdata(sys,J1,...,Jn) extracts the data for the (J1,...,JN) entry in the model array sys.

You can access the remaining LTI properties of **sys** with **get** or by direct referencing, for example,

sys.Ts sys.variable

Examples

Example 1

Given the SISO transfer function

```
h = tf([1 \ 1], [1 \ 2 \ 5])
```

you can extract the numerator and denominator coefficients by typing

This syntax returns two row vectors.

If you turn h into a MIMO transfer function by typing

```
H = [h ; tf(1, [1 1])]
```

the command

[num,den] = tfdata(H)

now returns two cell arrays with the numerator/denominator data for each SISO entry. Use celldisp to visualize this data. Type

```
celldisp(num)
```

This command returns the numerator vectors of the entries of H.

```
num{1} =
0 1 1
num{2} =
0 1
```

Similarly, for the denominators, type

```
celldisp(den)
den{1} =
    1    2    5
den{2} =
    1    1
```

Example 2

Extract the numerator, denominator and their standard deviations for a 2-input, 1 output identified transfer function.

```
load iddata7
transfer function model
sys1 = tfest(z7, 2, 1, 'InputDelay',[1 0]);
an equivalent process model
sys2 = procest(z7, {'P2UZ', 'P2UZ'}, 'InputDelay',[1 0]);
[num1, den1, ~, dnum1, dden1] = tfdata(sys1);
[num2, den2, ~, dnum2, dden2] = tfdata(sys2);
```

See Also

```
ssdata | zpkdata | get | tf
```

Introduced before R2006a

thiran

Generate fractional delay filter based on Thiran approximation

Syntax

```
sys = thiran(tau, Ts)
```

Description

sys = thiran(tau, Ts) discretizes the continuous-time delay tau using a Thiran
filter to approximate the fractional part of the delay. Ts specifies the sample time.

Input Arguments

tau

Time delay to discretize.

Ts

Sample time.

Output Arguments

sys

Discrete-time tf object.

Examples

Approximate and discretize a time delay that is a noninteger multiple of the target sample time.

```
sys1 = thiran(2.4, 1)
Transfer function:
0.004159 z^3 - 0.04813 z^2 + 0.5294 z + 1
z^3 + 0.5294 z^2 - 0.04813 z + 0.004159
```

```
Sample time: 1
```

The time delay is 2.4 s, and the sample time is 1 s. Therefore, **sys1** is a discrete-time transfer function of order 3.

Discretize a time delay that is an integer multiple of the target sample time.

```
sys2 = thiran(10, 1)
Transfer function:
    1
----
z^10
Sample time: 1
```

More About

```
Tips
```

- If tau is an integer multiple of Ts, then sys represents the pure discrete delay z^{-N} , with $N = \tan/\text{Ts}$. Otherwise, sys is a discrete-time, all-pass, infinite impulse response (IIR) filter of order ceil(tau/Ts).
- thiran approximates and discretizes a pure time delay. To approximate a pure continuous-time time delay without discretizing, use pade. To discretize continuous-time models having time delays, use c2d.

Algorithms

The Thiran fractional delay filter has the following form:

$$H(z) = \frac{a_N z^N + a_{N-1} z^{N-1} + \dots + a_1}{a_0 z^N + a_1 z^{N-1} + \dots + a_N}.$$

The coefficients $a_0, ..., a_N$ are given by:

$$a_k = (-1)^k \binom{N}{k} \prod_{i=0}^N \frac{D - N + i}{D - N + k + i}, \quad \forall k : 1, 2, \dots, N$$
$$a_0 = 1$$

where $D = \tau/T_s$ and N = ceil(D) is the filter order. See [1].

References

 [1] T. Laakso, V. Valimaki, "Splitting the Unit Delay", *IEEE Signal Processing Magazine*, Vol. 13, No. 1, p.30-60, 1996.

See Also

c2d | pade | tf

Introduced in R2010a

timeoptions

Create list of time plot options

Syntax

```
P = timeoptions
P = timeoptions('cstprefs')
```

Description

P = timeoptions returns a list of available options for time plots with default values set. You can use these options to customize the time value plot appearance from the command line.

P = timeoptions('cstprefs') initializes the plot options you selected in the Control System and System Identification Toolbox Preferences Editor. For more information about the editor, see "Toolbox Preferences Editor" in the User's Guide documentation.

This table summarizes the available time plot options.

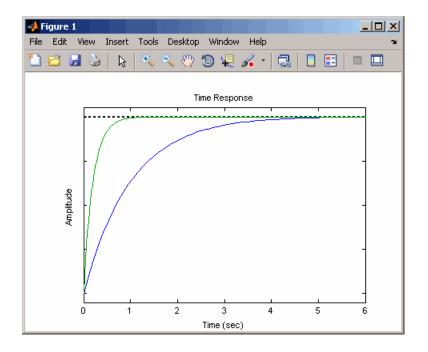
Option	Description
Title, XLabel, YLabel	Label text and style
TickLabel	Tick label style
Grid	Show or hide the grid Specified as one of the following strings: 'off' 'on' Default : 'off'
GridColor	Color of the grid lines Specified as one of the following: Vector of RGB values in the range [0,1] color string 'none'. Default: [0.15,0.15,0.15]
XlimMode, YlimMode	Limit modes
Xlim, Ylim	Axes limits

Option	Description
IOGrouping	Grouping of input-output pairs Specified as one of the following strings: 'none' 'inputs' 'outputs' 'all' Default: 'none'
InputLabels, OutputLabels	Input and output label styles
InputVisible, OutputVisible	Visibility of input and output channels
Normalize	Normalize responses Specified as one of the following strings: 'on' 'off' Default : 'off'
SettleTimeThreshold	Settling time threshold
RiseTimeLimits	Rise time limits
TimeUnits	Time units, specified as one of the following strings:
	 'nanoseconds'
	 'microseconds'
	• 'milliseconds'
	• 'seconds'
	• 'minutes'
	• 'hours'
	• 'days'
	• 'weeks'
	• 'months'
	• 'years'
	Default: 'seconds'
	You can also specify 'auto' which uses time units specified in the TimeUnit property of the input system. For multiple systems with different time units, the units of the first system is used.

Examples

In this example, enable the normalized response option before creating a plot.

```
P = timeoptions;
% Set normalize response to on in options
P.Normalize = 'on';
% Create plot with the options specified by P
h = stepplot(tf(10,[1,1]),tf(5,[1,5]),P);
The following step plot is created with the responses normalized.
```



See Also

impulseplot | lsimplot | setoptions | stepplot | getoptions | initialplot

Introduced in R2008a

totaldelay

Total combined I/O delays for LTI model

Syntax

```
td = totaldelay(sys)
```

Description

td = totaldelay(sys) returns the total combined I/O delays for an LTI model sys. The matrix td combines contributions from the InputDelay, OutputDelay, and ioDelayMatrix properties.

Delays are expressed in seconds for continuous-time models, and as integer multiples of the sample period for discrete-time models. To obtain the delay times in seconds, multiply td by the sample time sys.Ts.

Examples

The resulting I/O map is

$$e^{-2s} \times \frac{1}{s} e^{-1.5s} = e^{-3.5s} \frac{1}{s}$$

This is equivalent to assigning an I/O delay of 3.5 seconds to the original model sys.

See Also

hasdelay | absorbDelay

Introduced before R2006a

tzero

Invariant zeros of linear system

Syntax

z = tzero(sys)
z = tzero(A,B,C,D,E)
z = tzero(____,tol)
[z,nrank] = tzero(____)

Description

z = tzero(sys) returns the invariant zeros of the multi-input, multi-output (MIMO) dynamic system, sys. If sys is a minimal realization, the invariant zeros coincide with the transmission zeros of sys.

z = tzero(A,B,C,D,E) returns the invariant zeros of the state-space model

$$E\frac{dx}{dt} = Ax + Bu$$
$$y = Cx + Du.$$

Omit E for an explicit state-space model (E = I).

z = tzero(_____,tol) specifies the relative tolerance, tol, controlling rank decisions.

 $[z,nrank] = tzero(___)$ also returns the normal rank of the transfer function of sys or of the transfer function $H(s) = D + C(sE - A)^{-1}B$.

Input Arguments

sys

MIMO dynamic system model. If sys is not a state-space model, then tzero computes tzero(ss(sys)).

A,B,C,D,E

State-space matrices describing the linear system

$$E\frac{dx}{dt} = Ax + Bu$$
$$y = Cx + Du.$$

tzero does not scale the state-space matrices when you use the syntax z = tzero(A,B,C,D,E). Use prescale if you want to scale the matrices before using tzero.

Omit E to use E = I.

tol

Relative tolerance controlling rank decisions. Increasing tolerance helps detect nonminimal modes and eliminate very large zeros (near infinity). However, increased tolerance might artificially inflate the number of transmission zeros.

Default: eps^(3/4)

Output Arguments

z

Column vector containing the invariant zeros of sys or the state-space model described by A,B,C,D,E.

nrank

Normal rank of the transfer function of sys or of the transfer function $H(s) = D + C(sE - A)^{-1}B$. The *normal rank* is the rank for values of *s* other than the transmission zeros.

To obtain a meaningful result for nrank, the matrix s*E-A must be regular (invertible for most values of *s*). In other words, sys or the system described by A,B,C,D,E must have a finite number of poles.

Examples

Transmission Zeros of MIMO Transfer Function

Find the invariant zeros of a MIMO transfer function and confirm that they coincide with the transmission zeros.

Create a MIMO transfer function, and locate its invariant zeros.

```
s = tf('s');
H = [1/(s+1) 1/(s+2);1/(s+3) 2/(s+4)];
z = tzero(H)
z =
-2.5000 + 1.3229i
-2.5000 - 1.3229i
```

The output is a column vector listing the locations of the invariant zeros of H. This output shows that H a has complex pair of invariant zeros.

Check whether the first invariant zero is a transmission zero of H.

If z(1) is a transmission zero of H, then H drops rank at s = z(1).

```
H1 = evalfr(H,z(1));
svd(H1)
ans =
1.5000
0.0000
```

H1 is the transfer function, H, evaluated at s = z(1). H1 has a zero singular value, indicating that H drops rank at that value of s. Therefore, z(1) is a transmission zero of H. A similar analysis shows that z(2) is also a transmission zero.

Unobservable and Uncontrollable Modes of MIMO Model

Identify the unobservable and uncontrollable modes of a MIMO model using the statespace matrix syntax of tzero.

Obtain a MIMO model.

```
load ltiexamples gasf
size(gasf)
```

State-space model with 4 outputs, 6 inputs, and 25 states.

gasf is a MIMO model that might contain uncontrollable or unobservable states.

Scale the state-space matrices of gasf.

[A,B,C,D] = ssdata(prescale(gasf));

To identify the unobservable and uncontrollable modes of gasf, you need access to the state-space matrices A, B, C, and D of the model. tzero does not scale state-space matrices when you use the syntax. Therefore, use prescale with ssdata to extract scaled values of these matrices.

Use tzero to identify the uncontrollable states of gasf.

```
uncon = tzero(A,B,[],[])
uncon =
    -0.0568
    -0.0568
    -0.0568
    -0.0568
    -0.0568
    -0.0568
```

When you provide A and B matrices to tzero, but no C and D matrices, the command returns the eigenvalues of the uncontrollable modes of gasf. The output shows that there are six degenerate uncontrollable modes.

Identify the unobservable states of gasf.

```
unobs = tzero(A,[],C,[])
unobs =
Empty matrix: 0-by-1
```

When you provide A and C matrices, but no B and D matrices, the command returns the eigenvalues of the unobservable modes. The empty result shows that gasf contains no unobservable states.

Alternatives

To calculate the zeros and gain of a single-input, single-output (SISO) system, use zero.

More About

Invariant zeros

For a MIMO state-space model

$$E\frac{dx}{dt} = Ax + Bu$$
$$y = Cx + Du,$$

the *invariant zeros* are the complex values of s for which the rank of the system matrix

$$\begin{bmatrix} A - sE & B \\ C & D \end{bmatrix}$$

drops from its normal value. (For explicit state-space models, E = I).

Transmission zeros

For a MIMO state-space model

$$E\frac{dx}{dt} = Ax + Bu$$
$$y = Cx + Du,$$

the *transmission zeros* are the complex values of *s* for which the rank of the equivalent transfer function $H(s) = D + C(sE - A)^{-1}B$ drops from its normal value. (For explicit statespace models, E = I.)

Transmission zeros are a subset of the invariant zeros. For minimal realizations, the transmission zeros and invariant zeros are identical.

Tips

 You can use the syntax z = tzero(A,B,C,D,E) to find the uncontrollable or unobservable modes of a state-space model. When C and D are empty or zero, tzero returns the uncontrollable modes of (A-SE,B). Similarly, when B and D are empty or zero, tzero returns the unobservable modes of (C,A-SE). See "Unobservable and Uncontrollable Modes of MIMO Model" on page 1-874 for an example.

Algorithms

tzero is based on SLICOT routines AB08ND, AG08BD, and AB8NXZ. tzero implements the algorithms in [1] and [2].

References

- [1] Emami-Naeini, A. and P. Van Dooren, "Computation of Zeros of Linear Multivariable Systems," *Automatica*, 18 (1982), pp. 415–430.
- [2] Misra, P, P. Van Dooren, and A. Varga, "Computation of Structural Invariants of Generalized State-Space Systems," *Automatica*, 30 (1994), pp. 1921-1936.

See Also

pole | pzmap | zero

Introduced in R2012a

updateSystem

Update dynamic system data in a response plot

Syntax

```
updateSystem(h,sys)
updateSystem(h,sys,N)
```

Description

updateSystem(h, sys) replaces the dynamic system used to compute a response plot with the dynamic system model or model array sys, and updates the plot. If the plot with handle h contains more than one system response, this syntax replaces the first response in the plot. updateSystem is useful, for example, to cause a plot in a GUI to update in response to interactive input. See "Build GUI With Interactive Response-Plot Updates".

updateSystem(h,sys,N) replaces the data used to compute the Nth response in the
plot.

Examples

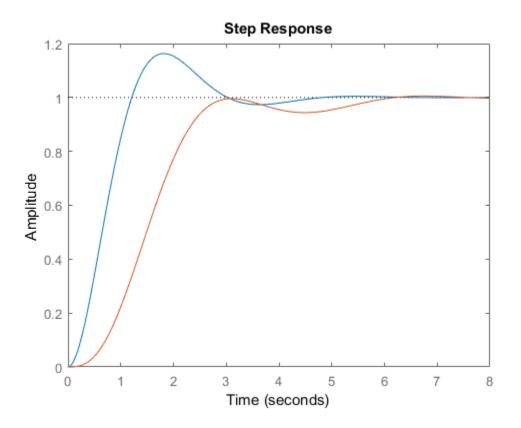
Update System Data in Response Plot

Replace step response data in an existing plot with data computed from a different dynamic system model.

Suppose you have a plant model and pure integrator controller that you designed for that plant. Plot the step responses of the plant and the closed-loop system.

```
w = 2;
zeta = 0.5;
G = tf(w^2,[1,2*zeta*w,w^2]);
C1 = pid(0,0.621);
CL1 = feedback(G*C1,1);
```

h = stepplot(G,CL1);



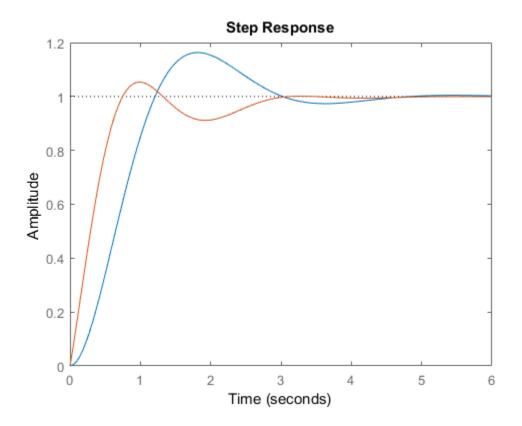
h is the plot handle that identifies the plot created by stepplot. In this figure, G is used to compute the first response, and CL1 is used to compute the second response. This ordering corresponds to the order of inputs to stepplot.

Suppose you also have a PID controller design that you want to analyze. Create a model of the closed-loop system using this alternate controller.

C2 = pid(2,2.6,0.4,0.002); CL2 = feedback(G*C2,1);

Update the step plot to display the second closed-loop system instead of the first. The closed-loop system is the second response in the plot, so specify the index value 2.

updateSystem(h,CL2,2);



The updateSystem command replaces the system used to compute the second response displayed in the plot. Instead of displaying response data derived from CL1, the plot now shows data derived from CL2.

When you build a GUI that displays a response plot, use updateSystem in GUI control callbacks to cause those GUI controls to update the response plot. For an example showing how to implement such a GUI control, see "Build GUI With Interactive Response-Plot Updates".

"Build GUI With Interactive Response-Plot Updates"

Input Arguments

h - Plot to update

plot handle

Plot to update with new system data, specified as a plot handle. Typically, you obtain the plot handle as an output argument of a response plotting command such as stepplot or bodeplot. For example, the command h = bodeplot(G) returns a handle to a plot containing the Bode response of a dynamic system, G.

sys - System for new response data

dynamic system model | model array

System from which to compute new response data for the response plot, specified as a dynamic system model or model array.

sys must match the plotted system that it replaces in both I/O dimensions and array dimensions. For example, suppose h refers to a plot that displays the step responses of a 5-element vector of 2-input, 2-output systems. In this case, **sys** must also be a 5-element vector of 2-input, 2-output systems. The number of states in the elements of **sys** need not match the number of states in the plotted systems.

N - Index of system to replace

1 (default) | positive integer

Index of system to replace in the plot, specified as a positive integer. For example, suppose you create a plot using the following command.

h = impulseplot(G1,G2,G3,G4);

To replace the impulse data of G3 with data from a new system, sys, use the following command.

```
updateSystem(h,sys,3);
```

Introduced in R2013b

upsample

Upsample discrete-time models

Syntax

```
sys1 = upsample(sys,L)
```

Description

sysl = upsample(sys, L) resamples the discrete-time dynamic system model sys at a sampling rate that is L-times faster than the sample time of $sys(Ts_0)$. L must be a positive integer. When sys is a TF model, H(z), upsample returns sysl as $H(z^L)$ with the sample time Ts_0 / L .

The responses of models sys and sys1 have the following similarities:

- The time responses of sys and sys1 match at multiples of Ts_0 .
- The frequency responses of sys and sys1 match up to the Nyquist frequency π / Ts_0 .

Note: sys1 has L times as many states as sys.

Examples

Create a transfer function with a sample time that is 14 times faster than that of the following transfer function:

To create the upsampled transfer function **sys1**, type the following commands:

L=14; sys1 = upsample(sys,L) These commands return the result:

Transfer function: 0.75 z^28 + 10 z^14 + 2

Sample time: 0.16071 The sample time of sys1 is 0.16071 seconds, which is 14 times faster than the 2.25 second sample time of sys.

See Also

d2c | c2d | d2d

Introduced in R2008b

xperm

Reorder states in state-space models

Syntax

sys = xperm(sys,P)

Description

sys = xperm(sys, P) reorders the states of the state-space model sys according to the permutation P. The vector P is a permutation of 1:NX, where NX is the number of states in sys. For information about creating state-space models, see ss and dss.

Examples

Order the states in the ssF8 model in alphabetical order.

1 Load the ssF8 model by typing the following commands:

```
load ltiexamples
ssF8
```

These commands return:

a =				
	PitchRate	Velocity	AOA	PitchAngle
PitchRate	-0.7	-0.0458	-12.2	0
Velocity	0	-0.014	-0.2904	-0.562
AOA	1	-0.0057	-1.4	0
PitchAngle	1	0	0	0
b =				
	Elevator Fla	peron		
PitchRate	-19.1	-3.1		
Velocity	-0.0119 -0	.0096		
AOA	-0.14	-0.72		
PitchAngle	0	0		
с =				
	PitchRate	Velocity	AO	A PitchAngle

FlightPath		0	0	-1	1
Acceleration		0	0	0.733	0
d =					
	Elevator	Flaperon			
FlightPath	0	0			
Acceleration	0.0768	0.1134			

Continuous-time model.

2 Order the states in alphabetical order by typing the following commands:

```
[y,P]=sort(ssF8.StateName);
sys=xperm(ssF8,P)
These commands return:
```

a = AOA PitchAngle PitchRate Velocity	A0A -1.4 0 -12.2 -0.2904	PitchAngle 0 0 -0.562	PitchRate 1 1 -0.7 0	Velocity -0.0057 0 -0.0458 -0.014
b =				
AOA PitchAngle PitchRate Velocity	-0.14 0 -19.1	laperon -0.72 0 -3.1 -0.0096		
с =				
	A0.		-	Velocity
FlightPath Acceleration	0.73	• •	0	0
ACCELETATION	0.73	3 0	0	0
d =				
FlightPath Acceleration	Elevator 0 0.0768	Flaperon 0 0.1134		

Continuous-time model.

The states in **SSF8** now appear in alphabetical order.

See Also

ss | dss

Introduced in R2008b

zero

Zeros and gain of SISO dynamic system

Syntax

```
z = zero(sys)
[z,gain] = zero(sys)
[z,gain] = zero(sysarr,J1,...,JN)
```

Description

z = zero(sys) returns the zeros of the single-input, single-output (SISO) dynamic system model, sys.

```
[z,gain] = zero(sys) also returns the overall gain of sys.
```

[z,gain] = zero(sysarr,J1,...,JN) returns the zeros and gain of the model with subscripts J1,...,JN in the model array sysarr.

Input Arguments

sys

SISO dynamic system model.

If **sys** has internal delays, **zero** sets all internal delays to zero, creating a zero-order Padé approximation. This approximation ensures that the system has a finite number of zeros. **zero** returns an error if setting internal delays to zero creates singular algebraic loops.

sysarr

Array of dynamic system models.

J1,...,JN

Indices identifying the model sysarr(J1,...,JN) in the array sysarr.

Output Arguments

z

Column vector containing the locations of zeros in **sys**. The zero locations are expressed in the reciprocal of the time units of **sys**. For example, the zeros are in units of 1/minutes if the **TimeUnit** property of **sys** is **minutes**.

gain

Gain of sys (in the zero-pole-gain sense).

Examples

Zero Locations and Gain of Transfer Function

Calculate the zero locations and overall gain of the transfer function

```
H(s) = \frac{4.2s^2 + 0.25s - 0.004}{s^2 + 9.6s + 17}.
H = tf([4.2,0.25,-0.004],[1,9.6,17]);
[z,gain] = zero(H)
z =
-0.0726
0.0131
gain =
4.2000
```

The zero locations are expressed in radians per second, because the time unit of the transfer function (H.TimeUnit) is seconds. Change the model time units, and zero returns pole locations relative to the new unit.

```
H = chgTimeUnit(H, 'minutes');
[z,gain] = zero(H)
z =
```

-4.3581 0.7867 gain = 4.2000

Alternatives

To calculate the transmission zeros of a multi-input, multi-output system, use tzero.

See Also pzmap | pole | tzero

Introduced before R2006a

zgrid

Generate z-plane grid of constant damping factors and natural frequencies

Syntax

zgrid zgrid(z,wn) zgrid([],[])

Description

zgrid generates, for root locus and pole-zero maps, a grid of constant damping factors from zero to one in steps of 0.1 and natural frequencies from zero to π in steps of $\pi/10$, and plots the grid over the current axis. If the current axis contains a discrete *z*-plane root locus diagram or pole-zero map, **zgrid** draws the grid over the plot without altering the current axis limits.

Zgrid(z,wn) plots a grid of constant damping factor and natural frequency lines for the damping factors and normalized natural frequencies in the vectors z and wn, respectively. If the current axis contains a discrete z-plane root locus diagram or pole-zero map, Zgrid(z,wn) draws the grid over the plot. The frequency lines for unnormalized (true) frequencies can be plotted using

zgrid(z,wn/Ts)

where Ts is the sample time.

zgrid([],[]) draws the unit circle.

Alternatively, you can select **Grid** from the right-click menu to generate the same zplane grid.

Examples

Plot z-plane grid lines on the root locus

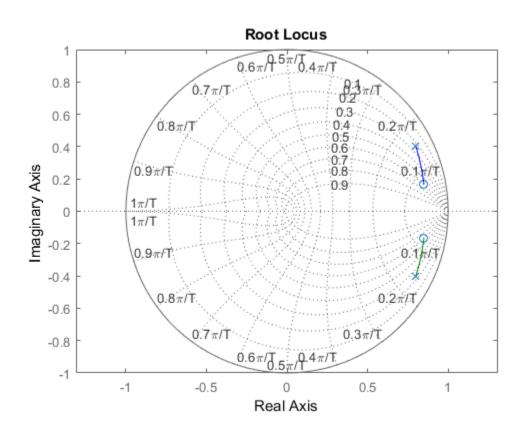
To see the z-plane grid on the root locus plot, type

```
H = tf([2 -3.4 1.5],[1 -1.6 0.8],-1)
rlocus(H)
zgrid
axis equal
```

Η =

```
2 z<sup>2</sup> - 3.4 z + 1.5
z<sup>2</sup> - 1.6 z + 0.8
```

```
Sample time: unspecified Discrete-time transfer function.
```



See Also sgrid | pzmap | rlocus

Introduced before R2006a

zpk

Create zero-pole-gain model; convert to zero-pole-gain model

Syntax

```
sys = zpk(z,p,k)
sys = zpk(z,p,k,Ts)
sys = zpk(M)
sys = zpk(z,p,k,ltisys)
s = zpk('s')
z = zpk('z',Ts)
zsys = zpk(sys)
zsys = zpk(sys, 'measured')
zsys = zpk(sys, 'noise')
zsys = zpk(sys, 'augmented')
```

Description

Used **zpk** to create zero-pole-gain models (**zpk** model objects), or to convert dynamic systems to zero-pole-gain form.

Creation of Zero-Pole-Gain Models

sys = zpk(z,p,k) creates a continuous-time zero-pole-gain model with zeros z, poles p, and gain(s) k. The output sys is a zpk model object storing the model data.

In the SISO case, z and p are the vectors of real- or complex-valued zeros and poles, and k is the real- or complex-valued scalar gain:

$$h(s) = k \frac{(s-z(1))(s-z(2))...(s-z(m))}{(s-p(1))(s-p(2))...(s-p(n))}$$

Set z or p to [] for systems without zeros or poles. These two vectors need not have equal length and the model need not be proper (that is, have an excess of poles).

To create a MIMO zero-pole-gain model, specify the zeros, poles, and gain of each SISO entry of this model. In this case:

- z and p are cell arrays of vectors with as many rows as outputs and as many columns as inputs, and k is a matrix with as many rows as outputs and as many columns as inputs.
- The vectors $z\{i, j\}$ and $p\{i, j\}$ specify the zeros and poles of the transfer function from input j to output i.
- k(i,j) specifies the (scalar) gain of the transfer function from input j to output i.

See below for a MIMO example.

sys = zpk(z,p,k,Ts) creates a discrete-time zero-pole-gain model with sample time Ts (in seconds). Set Ts = -1 or Ts = [] to leave the sample time unspecified. The input arguments z, p, k are as in the continuous-time case.

sys = zpk(M) specifies a static gain M.

sys = zpk(z,p,k,ltisys) creates a zero-pole-gain model with properties inherited
from the LTI model ltisys (including the sample time).

To create an array of zpk model objects, use a for loop, or use multidimensional cell arrays for z and p, and a multidimensional array for k.

Any of the previous syntaxes can be followed by property name/property value pairs.

```
'PropertyName', PropertyValue
```

Each pair specifies a particular property of the model, for example, the input names or the input delay time. For more information about the properties of **zpk** model objects, see "Properties" on page 1-895. Note that

sys = zpk(z,p,k,'Property1',Value1,...,'PropertyN',ValueN)

is a shortcut for the following sequence of commands.

```
sys = zpk(z,p,k)
set(sys,'Property1',Value1,...,'PropertyN',ValueN)
```

Zero-Pole-Gain Models as Rational Expressions in s or z

You can also use rational expressions to create a ZPK model. To do so, first type either:

- s = zpk('s') to specify a ZPK model using a rational function in the Laplace variable, s.
- z = zpk('z', Ts) to specify a ZPK model with sample time Ts using a rational function in the discrete-time variable, z.

Once you specify either of these variables, you can specify ZPK models directly as rational expressions in the variable s or z by entering your transfer function as a rational expression in either s or z.

Conversion to Zero-Pole-Gain Form

zsys = zpk(sys) converts an arbitrary LTI model sys to zero-pole-gain form. The
output zsys is a ZPK object. By default, zpk uses zero to compute the zeros when
converting from state-space to zero-pole-gain. Alternatively,

zsys = zpk(sys,'inv')

uses inversion formulas for state-space models to compute the zeros. This algorithm is faster but less accurate for high-order models with low gain at s = 0.

Conversion of Identified Models

An identified model is represented by an input-output equation of the form y(t) = Gu(t) + He(t), where u(t) is the set of measured input channels and e(t) represents the noise channels. If $\Lambda = LL'$ represents the covariance of noise e(t), this equation can also be written as y(t) = Gu(t) + HLv(t), where cov(v(t)) = I.

zsys = zpk(sys), or zsys = zpk(sys, 'measured') converts the measured component of an identified linear model into the ZPK form. sys is a model of type idss, idproc, idtf, idpoly, or idgrey. zsys represents the relationship between u and y.

zsys = zpk(sys, 'noise') converts the noise component of an identified linear model into the ZPK form. It represents the relationship between the noise input, v(t) and output, y_noise = HL v(t). The noise input channels belong to the InputGroup 'Noise'. The names of the noise input channels are v@yname, where yname is the name of the corresponding output channel. zsys has as many inputs as outputs.

zsys = zpk(sys, 'augmented') converts both the measured and noise dynamics into a ZPK model. zsys has ny+nu inputs such that the first nu inputs represent the channels u(t) while the remaining by channels represent the noise channels

```
v(t). zsys.InputGroup contains 2 input groups, 'measured' and 'noise'.
zsys.InputGroup.Measured is set to 1:nu while zsys.InputGroup.Noise is set to
nu+1:nu+ny. zsys represents the equation y(t) = [G HL] [u; v].
```

Tip An identified nonlinear model cannot be converted into a ZPK system. Use linear approximation functions such as linearize and linapp.

Variable Selection

As for transfer functions, you can specify which variable to use in the display of zeropole-gain models. Available choices include *s* (default) and *p* for continuous-time models, and *z* (default), z^{-1} , q^{-1} (equivalent to z^{-1}), or *q* (equivalent to *z*) for discrete-time models. Reassign the 'Variable' property to override the defaults. Changing the variable affects only the display of zero-pole-gain models.

Properties

zpk objects have the following properties:

z

System zeros.

The z property stores the transfer function zeros (the numerator roots). For SISO models, z is a vector containing the zeros. For MIMO models with Ny outputs and Nu inputs, z is a Ny-by-Nu cell array of vectors of the zeros for each input/output pair.

р

System poles.

The p property stores the transfer function poles (the denominator roots). For SISO models, p is a vector containing the poles. For MIMO models with Ny outputs and Nu inputs, p is a Ny-by-Nu cell array of vectors of the poles for each input/output pair.

k

System gains.

The k property stores the transfer function gains. For SISO models, k is a scalar value. For MIMO models with Ny outputs and Nu inputs, k is a Ny-by-Nu matrix storing the gains for each input/output pair.

DisplayFormat

String specifying the way the numerator and denominator polynomials are factorized for display purposes.

The numerator and denominator polynomials are each displayed as a product of first- and second-order factors. DisplayFormat controls the display of those factors. DisplayFormat can take the following values:

- 'roots' (default) Display factors in terms of the location of the polynomial roots.
- 'frequency' Display factors in terms of root natural frequencies ω_0 and damping ratios ζ .

The 'frequency' display format is not available for discrete-time models with Variable value 'z^-1' or 'q^-1'.

• 'time constant' — Display factors in terms of root time constants τ and damping ratios ζ .

The 'time constant' display format is not available for discrete-time models with Variable value 'z^-1' or 'q^-1'.

For continuous-time models, the following table shows how the polynomial factors are written in each display format.

DisplayName Value	First-Order Factor (Real Root <i>R</i>)	Second-Order Factor (Complex Root pair $R = a \pm jb$)
'roots'	(s-R)	$(s^2 - as + \beta)$, where $a = 2a$, $\beta = a^2 + b^2$
'frequency'	$(1 - s/\omega_0)$, where $\omega_0 = R$	$1 - 2\zeta(s/\omega_0) + (s/\omega_0)^2, \text{ where}$ $\omega_0^2 = a^2 + b^2, \zeta = a/\omega_0$
'time constant'	$(1 - \tau s)$, where $\tau = 1/R$	$1 - 2\zeta(\tau s) + (\tau s)^2, \text{ where } \tau = 1/\omega_0,$ $\zeta = a\tau$

For discrete-time models, the polynomial factors are written as in continuous time, with the following variable substitutions:

$$s \rightarrow w = \frac{z-1}{T_s}; \quad R \rightarrow \frac{R-1}{T_s},$$

where T_s is the sample time. In discrete time, τ and ω_0 closely match the time constant and natural frequency of the equivalent continuous-time root, provided $|z-1| \ll T_s$ $(\omega_0 \ll \pi/T_s = \text{Nyquist frequency}).$

Default: 'roots'

Variable

String specifying the transfer function display variable. Variable can take the following values:

- 's' Default for continuous-time models
- 'z' Default for discrete-time models
- 'p' Equivalent to 's'
- 'q' Equivalent to 'z'
- 'z^-1' Inverse of 'z'
- 'q^-1' Equivalent to 'z^-1'

The value of Variable only affects the display of zpk models.

Default: 'S'

ioDelay

Transport delays. **ioDelay** is a numeric array specifying a separate transport delay for each input/output pair.

For continuous-time systems, specify transport delays in the time unit stored in the TimeUnit property. For discrete-time systems, specify transport delays in integer multiples of the sample time, TS.

For a MIMO system with Ny outputs and Nu inputs, set ioDelay to a Ny-by-Nu array. Each entry of this array is a numerical value that represents the transport delay for the corresponding input/output pair. You can also set ioDelay to a scalar value to apply the same delay to all input/output pairs.

Default: 0 for all input/output pairs

InputDelay

Input delay for each input channel, specified as a scalar value or numeric vector. For continuous-time systems, specify input delays in the time unit stored in the TimeUnit property. For discrete-time systems, specify input delays in integer multiples of the sample time Ts. For example, InputDelay = 3 means a delay of three sample times.

For a system with Nu inputs, set InputDelay to an Nu-by-1 vector. Each entry of this vector is a numerical value that represents the input delay for the corresponding input channel.

You can also set InputDelay to a scalar value to apply the same delay to all channels.

Default: 0

OutputDelay

Output delays. OutputDelay is a numeric vector specifying a time delay for each output channel. For continuous-time systems, specify output delays in the time unit stored in the TimeUnit property. For discrete-time systems, specify output delays in integer multiples of the sample time Ts. For example, OutputDelay = 3 means a delay of three sampling periods.

For a system with Ny outputs, set OutputDelay to an Ny-by-1 vector, where each entry is a numerical value representing the output delay for the corresponding output channel. You can also set OutputDelay to a scalar value to apply the same delay to all channels.

Default: 0 for all output channels

Ts

Sample time. For continuous-time models, Ts = 0. For discrete-time models, Ts is a positive scalar representing the sampling period. This value is expressed in the unit specified by the TimeUnit property of the model. To denote a discrete-time model with unspecified sample time, set Ts = -1.

Changing this property does not discretize or resample the model. Use c2d and d2c to convert between continuous- and discrete-time representations. Use d2d to change the sample time of a discrete-time system.

Default: 0 (continuous time)

TimeUnit

String representing the unit of the time variable. This property specifies the units for the time variable, the sample time Ts, and any time delays in the model. Use any of the following values:

- 'nanoseconds'
- 'microseconds'
- 'milliseconds'
- 'seconds'
- 'minutes'
- 'hours'
- 'days'
- 'weeks'
- 'months'
- 'years'

Changing this property has no effect on other properties, and therefore changes the overall system behavior. Use chgTimeUnit to convert between time units without modifying system behavior.

Default: 'seconds'

InputName

Input channel names. Set InputName to a string for single-input model. For a multiinput model, set InputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign input names for multi-input models. For example, if **sys** is a two-input model, enter:

sys.InputName = 'controls';

The input names automatically expand to { 'controls(1) '; 'controls(2) '}.

You can use the shorthand notation u to refer to the InputName property. For example, sys.u is equivalent to sys.InputName.

Input channel names have several uses, including:

- · Identifying channels on model display and plots
- · Extracting subsystems of MIMO systems
- · Specifying connection points when interconnecting models

Default: Empty string ' ' for all input channels

InputUnit

Input channel units. Use InputUnit to keep track of input signal units. For a singleinput model, set InputUnit to a string. For a multi-input model, set InputUnit to a cell array of strings. InputUnit has no effect on system behavior.

Default: Empty string ' ' for all input channels

InputGroup

Input channel groups. The InputGroup property lets you assign the input channels of MIMO systems into groups and refer to each group by name. Specify input groups as a structure. In this structure, field names are the group names, and field values are the input channels belonging to each group. For example:

```
sys.InputGroup.controls = [1 2];
sys.InputGroup.noise = [3 5];
```

creates input groups named controls and noise that include input channels 1, 2 and 3, 5, respectively. You can then extract the subsystem from the controls inputs to all outputs using:

```
sys(:,'controls')
```

Default: Struct with no fields

OutputName

Output channel names. Set OutputName to a string for single-output model. For a multioutput model, set OutputName to a cell array of strings.

Alternatively, use automatic vector expansion to assign output names for multi-output models. For example, if **sys** is a two-output model, enter:

```
sys.OutputName = 'measurements';
```

```
The output names automatically expand to { 'measurements(1) '; 'measurements(2) '}.
```

You can use the shorthand notation y to refer to the OutputName property. For example, sys.y is equivalent to sys.OutputName.

Output channel names have several uses, including:

- Identifying channels on model display and plots
- Extracting subsystems of MIMO systems
- Specifying connection points when interconnecting models

Default: Empty string ' ' for all output channels

OutputUnit

Output channel units. Use OutputUnit to keep track of output signal units. For a single-output model, set OutputUnit to a string. For a multi-output model, set OutputUnit to a cell array of strings. OutputUnit has no effect on system behavior.

Default: Empty string ' ' for all output channels

OutputGroup

Output channel groups. The OutputGroup property lets you assign the output channels of MIMO systems into groups and refer to each group by name. Specify output groups as a structure. In this structure, field names are the group names, and field values are the output channels belonging to each group. For example:

```
sys.OutputGroup.temperature = [1];
sys.InputGroup.measurement = [3 5];
```

creates output groups named temperature and measurement that include output channels 1, and 3, 5, respectively. You can then extract the subsystem from all inputs to the measurement outputs using:

```
sys('measurement',:)
```

Default: Struct with no fields

Name

System name. Set Name to a string to label the system.

Default: ' '

Notes

Any text that you want to associate with the system. Set **Notes** to a string or a cell array of strings.

Default: { }

UserData

Any type of data you want to associate with system. Set UserData to any MATLAB data type.

Default: []

SamplingGrid

Sampling grid for model arrays, specified as a data structure.

For model arrays that are derived by sampling one or more independent variables, this property tracks the variable values associated with each model in the array. This information appears when you display or plot the model array. Use this information to trace results back to the independent variables.

Set the field names of the data structure to the names of the sampling variables. Set the field values to the sampled variable values associated with each model in the array. All sampling variables should be numeric and scalar valued, and all arrays of sampled values should match the dimensions of the model array.

For example, suppose you create a 11-by-1 array of linear models, sysarr, by taking snapshots of a linear time-varying system at times t = 0:10. The following code stores the time samples with the linear models.

```
sysarr.SamplingGrid = struct('time',0:10)
```

Similarly, suppose you create a 6-by-9 model array, M, by independently sampling two variables, zeta and w. The following code attaches the (zeta,w) values to M.

```
[zeta,w] = ndgrid(<6 values of zeta>,<9 values of w>)
M.SamplingGrid = struct('zeta',zeta,'w',w)
```

When you display M, each entry in the array includes the corresponding zeta and w values.

М

For model arrays generated by linearizing a Simulink model at multiple parameter values or operating points, the software populates SamplingGrid automatically with the variable values that correspond to each entry in the array. For example, the Simulink Control Design commands linearize and slLinearizer populate SamplingGrid in this way.

Default: []

Examples

Example 1

Create the continuous-time SISO transfer function:

$$h(s) = \frac{-2s}{(s-1+j)(s-1-j)(s-2)}$$

Create h(s) as a **zpk** object using:

h = zpk(0, [1-i 1+i 2], -2);

Example 2

Specify the following one-input, two-output zero-pole-gain model:

$$H(z) = \begin{bmatrix} \frac{1}{z - 0.3} \\ \frac{2(z + 0.5)}{(z - 0.1 + j)(z - 0.1 - j)} \end{bmatrix}.$$

To do this, enter:

z = {[]; -0.5}; p = {0.3; [0.1+i 0.1-i]}; k = [1; 2]; H = zpk(z,p,k,-1); % unspecified sample time

Example 3

Convert the transfer function

 $h = tf([-10 \ 20 \ 0], [1 \ 7 \ 20 \ 28 \ 19 \ 5]);$

to zero-pole-gain form, using:

zpk(h)

This command returns the result:

Zero/pole/gain: -10 s (s-2) (s+1)^3 (s^2 + 4s + 5)

Example 4

Create a discrete-time ZPK model from a rational expression in the variable z.

z = zpk('z',0.1); H = (z+.1)*(z+.2)/(z^2+.6*z+.09)

This command returns the following result:

Zero/pole/gain: (z+0.1) (z+0.2) (z+0.3)^2 Sample time: 0.1

Example 5

Create a MIMO zpk model using cell arrays of zeros and poles.

Create the two-input, two-output zero-pole-gain model

$$H(s) = \begin{bmatrix} \frac{-1}{s} & \frac{3(s+5)}{(s+1)^2} \\ \frac{2(s^2 - 2s + 2)}{(s-1)(s-2)(s-3)} & 0 \end{bmatrix}$$

by entering:

Use [] as a place holder in Z or P when the corresponding entry of H(s) has no zeros or poles.

Example 6

Extract the measured and noise components of an identified polynomial model into two separate ZPK models. The former (measured component) can serve as a plant model while the latter can serve as a disturbance model for control system design.

```
load icEngine
z = iddata(y,u,0.04);
nb = 2; nf = 2; nc = 1; nd = 3; nk = 3;
sys = bj(z, [nb nc nd nf nk]);
```

sys is a model of the form, y(t) = B/F u(t) + C/D e(t), where B/F represents the measured component and C/D the noise component.

sysMeas = zpk(sys, 'measured')

Alternatively, use can simply use zpk(sys) to extract the measured component.

```
sysNoise = zpk(sys, 'noise')
```

More About

Algorithms

zpk uses the MATLAB function roots to convert transfer functions and the functions zero and pole to convert state-space models.

See Also

frd | get | set | ss | tf | zpkdata

Introduced before R2006a

zpkdata

Access zero-pole-gain data

Syntax

```
[z,p,k] = zpkdata(sys)
[z,p,k,Ts] = zpkdata(sys)
[z,p,k,Ts,covz,covp,covk] = zpkdata(sys)
```

Description

[z,p,k] = zpkdata(sys) returns the zeros z, poles p, and gain(s) k of the zero-polegain model sys. The outputs z and p are cell arrays with the following characteristics:

- z and p have as many rows as outputs and as many columns as inputs.
- The (i, j) entries $z\{i, j\}$ and $p\{i, j\}$ are the (column) vectors of zeros and poles of the transfer function from input j to output i.

The output k is a matrix with as many rows as outputs and as many columns as inputs such that k(i, j) is the gain of the transfer function from input j to output i. If sys is a transfer function or state-space model, it is first converted to zero-pole-gain form using zpk.

For SISO zero-pole-gain models, the syntax

[z,p,k] = zpkdata(sys,'v')

forces zpkdata to return the zeros and poles directly as column vectors rather than as cell arrays (see example below).

[z,p,k,Ts] = zpkdata(sys) also returns the sample time Ts.

[z,p,k,Ts,covz,covp,covk] = zpkdata(sys) also returns the covariances of the zeros, poles and gain of the identified model sys. covz is a cell array such that covz{ky,ku} contains the covariance information about the zeros in the vector z{ky,ku}. covz{ky,ku} is a 3-D array of dimension 2-by-2-by-Nz, where Nz is the length of $z\{ky, ku\}$, so that the (1, 1) element is the variance of the real part, the (2, 2) element is the variance of the imaginary part, and the (1, 2) and (2, 1) elements contain the covariance between the real and imaginary parts. covp has a similar relationship to p.covk is a matrix containing the variances of the elements of k.

You can access the remaining LTI properties of **sys** with **get** or by direct referencing, for example,

sys.Ts sys.inputname

Examples

Example 1

Given a zero-pole-gain model with two outputs and one input

you can extract the zero/pole/gain data embedded in H with

```
[z,p,k] = zpkdata(H)
z =
        [ 0]
      [-0.5000]
p =
        [ 0.3000]
      [2x1 double]
k =
        1
        2
```

To access the zeros and poles of the second output channel of $H,\,{\rm get}$ the content of the second cell in z and p by typing

```
z{2,1}
ans =
    -0.5000
p{2,1}
ans =
    0.1000+ 1.0000i
    0.1000- 1.0000i
```

Example 2

Extract the ZPK matrices and their standard deviations for a 2-input, 1 output identified transfer function.

load iddata7

transfer function model

sys1 = tfest(z7, 2, 1, 'InputDelay',[1 0]);

an equivalent process model

sys2 = procest(z7, {'P2UZ', 'P2UZ'}, 'InputDelay',[1 0]);

1, p1, k1, ~, dz1, dp1, dk1] = zpkdata(sys1);
[z2, p2, k2, ~, dz2, dp2, dk2] = zpkdata(sys2);

Use iopzplot to visualize the pole-zero locations and their covariances

```
h = iopzplot(sys1, sys2);
showConfidence(h)
```

See Also

ssdata | tfdata | get | zpk

Introduced before R2006a

Block Reference

Kalman Filter

Estimate states of discrete-time or continuous-time linear system

Description



Use the Kalman Filter block to estimate states of a state-space plant model given process and measurement noise covariance data. The state-space model can be time-varying. A steady-state Kalman filter implementation is used if the state-space model and the noise covariance matrices are all time-invariant. A time-varying Kalman filter is used otherwise.

Kalman filter provides the optimal solution to the following continuous or discrete estimation problems:

Continuous-Time Estimation

Given the continuous plant

 $\dot{x}(t) = A(t)x(t) + B(t)u(t) + G(t)w(t)$ (state equation) y(t) = C(t)x(t) + D(t)u(t) + H(t)w(t) + v(t) (measurement equation)

with known inputs u, white process noise w, and white measurement noise v satisfying:

$$E[w(t)] = E[v(t)] = 0$$
$$E[w(t)w^{T}(t)] = Q(t)$$
$$E[w(t)v^{T}(t)] = N(t)$$
$$E[v(t)v(t)^{T}] = R(t)$$

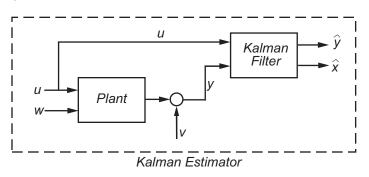
construct a state estimate \hat{x} that minimizes the state estimation error covariance $P(t) = E[(x-x)(x-x)^T].$ The optimal solution is the Kalman filter with equations

$$\begin{split} & L(t) = (P(t)C^{T}(t) + \bar{N}), \\ & \dot{P}(t) = A(t)P(t) + P(t)A^{T}(t) + \bar{Q}(t) - L(t)\bar{R}(t)L^{T}(t), \\ & \dot{x}(t) = A(t)x(t) + B(t)u(t) + L(t)(y(t) - C(t)x(t) - D(t)u(t)), \end{split}$$

where

$$\begin{split} & \bar{Q}(t) = G(t)Q(t)G^T(t), \\ & \bar{R}(t) = R(t) + H(t)N(t) + N^T(t)H^T(t) + H(t)Q(t)H^T(t), \\ & \bar{N}(t) = G(t)(Q(t)H^T(t) + N(t)). \end{split}$$

The Kalman filter uses the known inputs u and the measurements y to generate the state estimates \hat{x} . If you want, the block can also output the estimates of the true plant output \hat{y} .



The block implements the steady-state Kalman filter when the system matrices (A(t), B(t), C(t), D(t), G(t), H(t)) and noise covariance matrices (Q(t), R(t), N(t)) are constant (specified in the Block Parameters dialog box). The steady-state Kalman filter uses a constant matrix P that minimizes the steady-state estimation error covariance and solves the associated continuous-time algebraic Riccati equation:

$$P = \lim_{t \to \infty} E[(x-x)(x-x)^T].$$

Discrete-Time Estimation

Given the discrete plant

$$\begin{aligned} x[n+1] &= A[n] x[n] + B[n] u[n] + G[n] w[n], \\ y[n] &= C[n] x[n] + D[n] u[n] + H[n] w[n] + v[n], \end{aligned}$$

with known inputs u, white process noise w and white measurement noise v satisfying

$$E[u[n]] = E[v[n]] = 0,$$

$$E[u[n]v^{T}[n]] = Q[n],$$

$$E[v[n]v^{T}[n]] = R[n],$$

$$E[u[n]v^{T}[n]] = N[n].$$

The estimator has the following state equation

$$\hat{x}[n+1|n] = A[n]\hat{x}[n|n-1] + B[n]u[n] + L[n](y[n] - C[n]\hat{x}[n|n-1] - D[n]u[n]),$$

where the gain L[n] is calculated through the discrete Riccati equation:

$$\begin{split} &L[n] = (A[n]P[n]C^{T}[n] + \bar{N}[n])(C[n]P[n]C^{T}[n] + \bar{R}[n])^{-1}, \\ &M[n] = P[n]C^{T}[n](C[n]P[n]C^{T}[n] + \bar{R}[n])^{-1}, \\ &Z[n] = (I - M[n]C[n])P[n](I - M[n]C[n])^{T} + M[n]\bar{R}[n]M^{T}[n], \\ &P[n+1] = (A[n] - \bar{N}[n]\bar{R}^{-1}[n]C[n])Z(A[n] - \bar{N}[n]\bar{R}^{-1}[n]C[n])^{T} + \bar{Q}[n] - N[n]\bar{R}^{-1}[n]N^{T}[n], \end{split}$$

where I is the identity matrix of appropriate size and

$$\begin{split} \bar{Q}[\mathbf{n}] &= G[\mathbf{n}]Q[\mathbf{n}]G^{T}[\mathbf{n}], \\ \bar{R}[\mathbf{n}] &= R[\mathbf{n}] + H[\mathbf{n}]N[\mathbf{n}] + N^{T}[\mathbf{n}]H^{T}[\mathbf{n}] + H[\mathbf{n}]Q[\mathbf{n}]H^{T}[\mathbf{n}], \\ \bar{N}[\mathbf{n}] &= G[\mathbf{n}](Q[\mathbf{n}]H^{T}[\mathbf{n}] + N[\mathbf{n}]), \\ \text{and} \\ P[\mathbf{n}] &= E[(x - x[n \mid n - 1])(x - \hat{x}[n \mid n - 1])^{T}], \\ Z[\mathbf{n}] &= E[(x - \hat{x}[n \mid n])(x - \hat{x}[n \mid n])^{T}], \end{split}$$

The steady-state Kalman filter uses a constant matrix P that minimizes the steady-state estimation error covariance and solves the associated discrete-time algebraic Riccati equation.

There are two variants of discrete-time Kalman filters:

The current estimator generates the state estimates $\hat{x}[n \mid n]$ using all measurement available, including y[n]. The filter updates $\hat{x}[n \mid n-1]$ with y[n] and outputs:

 $\hat{x}[n \mid n] = \hat{x}[n \mid n-1] + M[n](y[n] - C[n]\hat{x}[n \mid n-1] - D[n]u[n]),$ $\hat{y}[n \mid n] = C[n]\hat{x}[n \mid n] + D[n]u[n].$

• The delayed estimator generates the state estimates $\hat{x}[n \mid n-1]$ using measurements up to y[n-1]. The filter outputs $\hat{x}[n \mid n-1]$ as defined previously, along with the optional output $\hat{y}[n \mid n-1]$

$$\hat{y}[n | n-1] = C[n]\hat{x}[n | n-1] + D[n]u[n]$$

The current estimator has better estimation accuracy compared to the delayed estimator, which is important for slow sample times. However, it has higher computational cost, making it harder to implement inside control loops. More specifically, it has direct feedthrough. This leads to an algebraic loop if the Kalman filter is used in a feedback loop that does not contain any delays (the feedback loop itself also has direct feedthrough). The algebraic loop can impact the speed of simulation. You cannot generate code if your model contains algebraic loops.

The Kalman Filter block differs from the kalman command in the following ways:

- When calling kalman(sys,...), sys includes the G and H matrices. Specifically, sys.B has [B G] and sys.D has [D H]. When you provide a LTI variable to the Kalman Filter block, it does not assume that the LTI variable provided contains G and H. They are optional and separate.
- The kalman command outputs [yhat;xhat] by default. The block only outputs xhat by default.

Dialog Box and Parameters

The following table summarizes the Kalman Filter block parameters, accessible via the Block Parameter dialog box.

Task	Parameters
Specify filter settings	Time domain

Task	Parameters
	• Use the current measurement y[n] to improve xhat[n]
Specify the system model	Model source in Model Parameters tab
Specify initial state estimates	Source in Model Parameters tab
Specify noise characteristics	In Model Parameters tab:
	• Use G and H matrices (default G=I and H=0)
	• Q, Time-invariant Q
	• R, Time-invariant R
	• N, Time-invariant N
Specify additional inports	In Options tab:
	• Add input port u
	 Add input port Enable to control measurement updates
	External reset
Specify additional outports	In Options tab:
	Output estimated model output y
	Output state estimation error covariance Z

Time domain

Specify whether to estimate continuous-time or discrete-time states:

- + Discrete-Time (Default) Block estimates discrete-time states
- Continuous-Time Block estimates continuous-time states

Use the current measurement y[n] to improve xhat[n]

Use the current estimator variant of the discrete-time Kalman filter. When not selected, the delayed estimator (variant) is used.

This option is available only when **Time Domain** is **Discrete-Time**.

Model source

Specify how the A, B, C, D matrices are provided to the block. Must be one of the following:

- Dialog: LTI State-Space Variable Use the values specified in the LTI statespace variable. You must also specify the variable name in Variable. The sample time of the model must match the setting in the **Time domain** option, i.e. the model must be discrete-time if the **Time domain** is discrete-time.
- Dialog: Individual A, B, C, D matrices Specify values in the following block parameters:
 - A Specify the A matrix. It must be real and square.
 - **B**—Specify the B matrix. It must be real and have as many rows as the A matrix. This option is available only when **Add input port u** is selected in the **Options** tab.
 - **C** Specify the C matrix. It must be real and have as many columns as the A matrix.
 - D Specify the D matrix. It must be real. It must have as many rows as the C matrix and as many columns as the B matrix. This option is available only when Add input port u is selected in the Options tab.
- External Specify the A, B, C, D matrices as input signals to the Kalman Filter block. If you select this option, the block includes additional input ports A, B, C and D. You must also specify the following in the block parameters:
 - Number of states Number of states to be estimated, specified as a positive integer. The default value is 2.
 - Number of inputs Number of known inputs in the model, specified as a positive integer. The default value is 2. This option is only available when Add input port u is selected.
 - Number of outputs Number of measured outputs in the model, specified as a positive integer. The default value is 2.

Sample Time

Block sample time, specified as -1 or a positive scalar.

This option is available only when **Time Domain** is **Discrete** Time and **Model Source** is **Dialog**: Individual A, B, C, D matrices or External. The sample time is obtained from the LTI state-space variable if the Model Source is **Dialog**: LTI State-Space Variable.

The default value is -1, which implies that the block inherits its sample time based on the context of the block within the model. All block input ports must have the same sample time.

Source

Specify how to enter the initial state estimates and initial state estimation error covariance:

- **Dialog** Specify the values directly in the dialog box. You must also specify the following parameters:
 - Initial states x[0] Specify the initial state estimate as a real scalar or vector. If you specify a scalar, all initial state estimates are set to this scalar. If you specify a vector, the length of the vector must match with the number of states in the model.
 - State estimation error covariance P[0] (only when time-varying Kalman filter is used) Specify the initial state estimation error covariance P[0] for discrete-time Kalman filter or P(0) for continuous-time Kalman filter. Must be specified as one of the following:
 - Real nonnegative scalar. P is an Ns-by-Ns diagonal matrix with the scalar on the diagonals. Ns is the number of states in the model.
 - Vector of real nonnegative scalars. P is an Ns-by-Ns diagonal matrix with the elements of the vector on the diagonals of P.
 - Ns-by-Ns positive semi-definite matrix.
- External Inherit the values from input ports. The block includes an additional input port X0. A second additional input port P0 is added when time-varying Kalman filter is used. X0 and P0 must satisfy the same conditions described previously when you specify them in the dialog box.

Use the Kalman Gain K from the model variable

Specify whether to use the pre-identified Kalman Gain contained in the state-space plant model. This option is available only when:

- Model Source is Dialog: LTI State-Space Variable and Variable is an identified state-space model (idss) with a nonzero K matrix.
- Time Invariant Q, Time Invariant R and Time Invariant N options are selected.

If the Use G and H matrices (default G=I and H=0) option is selected, Time Invariant G and Time Invariant H options must also be selected.

Use G and H matrices (default G=I and H=0)

Specify whether to use non-default values for the G and H matrices. If you select this option, you must specify:

- **G** Specify the G matrix. It must be a real matrix with as many rows as the A matrix. The default value is 1.
- **Time-invariant G** Specify if the G matrix is time invariant. If you unselect this option, the block includes an additional input port G.
- **H** Specify the H matrix. It must be a real matrix with as many rows as the C matrix and as many columns as the G matrix. The default value is 0.
- **Time-invariant H** Specify if the H matrix is time invariant. If you unselect this option, the block includes an additional input port G.
- **Number of process noise inputs** Specify the number of process noise inputs in the model. The default value is 1.

This option is available only when **Time-invariant G** and **Time-invariant H** are unselected. Otherwise, this information is inferred from the G or H matrix.

Q

Process noise covariance matrix, specified as one of the following:

- Real nonnegative scalar. Q is an Nw-by-Nw diagonal matrix with the scalar on the diagonals. Nw is the number of process noise inputs in the model.
- Vector of real nonnegative scalars. Q is an Nw-by-Nw diagonal matrix with the elements of the vector on the diagonals of Q.

• Nw-by-Nw positive semi-definite matrix.

Time Invariant Q

Specify if the Q matrix is time invariant. If you unselect this option, the block includes an additional input port Q.

R

Measurement noise covariance matrix, specified as one of the following:

- Real positive scalar. R is an Ny-by-Ny diagonal matrix with the scalar on the diagonals. Ny is the number of measured outputs in the model.
- Vector of real positive scalars. R is an Ny-by-Ny diagonal matrix with the elements of the vector on the diagonals of R.
- Ny-by-Ny positive-definite matrix.

Time Invariant R

Specify if the R matrix is time invariant. If you unselect this option, the block includes an additional input port R.

Ν

Process and measurement noise cross-covariance matrix. Specify it as a Nw-by-Ny matrix. The matrix $[Q N; N^T R]$ must be positive definite.

Time Invariant N

Specify if the N matrix is time invariant. If you unselect this option, the block includes an additional input port N.

Add input port u

Select this option if your model contains known inputs u(t) or u[k]. The option is selected by default. Unselecting this option removes the input port u from the block and removes the **B**, **D** and **Number of inputs** parameters from the block dialog box.

Add input port Enable to control measurement updates

Select this option if you want to control the measurement updates. The block includes an additional inport Enable. The Enable input port takes a scalar signal. This option is unselected by default.

By default the block does measurement updates at each time step to improve the state and output estimates \hat{x} and \hat{y} based on measured outputs. The measurement update is skipped for the current sample time when the signal in the Enable port is 0. Concretely, the equation for state estimates become $\dot{\hat{x}}(t) = A(t)\hat{x}(t) + B(t)u(t)$ for continuous-time Kalman filter and $\hat{x}[n+1|n] = A[n]\hat{x}[n|n-1] + B[n]u[n]$ for discrete-time.

External Reset

Option to reset estimated states and parameter covariance matrix using specified initial values.

Suppose you reset the block at a time step, t. If the block is enabled at t, the software uses the initial parameter values specified either in the block dialog or the input ports P0 and X0 to estimate the states. In other words, at t, the block performs a time update and if it is enabled, a measurement update after the reset. The block outputs these updated estimates.

Specify one of the following:

- None (Default) Estimated states \hat{x} and state estimation error covariance matrix P values are not reset.
- **Rising** Triggers a reset when the control signal rises from a negative or zero value to a positive value. If the initial value is negative, rising to zero triggers a reset.
- Falling Triggers a reset when the control signal falls from a positive or a zero value to a negative value. If the initial value is positive, falling to zero triggers a reset.
- Either Triggers a reset when the control signal is either rising or falling.
- Level Triggers a reset in either of these cases:
 - The control signal is nonzero at the current time step.
 - The control signal changes from nonzero at the previous time step to zero at the current time step.

• Level hold — Triggers reset when the control signal is nonzero at the current time step.

When you choose an option other than None, a Reset input port is added to the block to provide the reset control input signal.

Output estimated model output y

Add \hat{y} output port to the block to output the estimated model outputs. The option is unselected by default.

Output estimated model output P or Z

Add P output port or Z output port to the block. The Z matrix is provided only when **Time Domain** is **Discrete Time** and the **Use the current measurement y[n] to improve xhat[n]** is selected. Otherwise, the P matrix, as described in the "Description" on page 2-2 section previously, is provided.

The option is unselected by default.

Ports

Port Name	Port Type	Description
	(In/ Out)	
u (Optional)	In	Known inputs, specified as a real scalar or vector.
У	In	Measured outputs, specified as a real scalar or vector.
xhat	Out	Estimated states, returned as a real scalar or vector.
yhat (Optional)	Out	Estimated outputs, returned as a real scalar or vector.
P or Z (Optional)	Out	State estimation error covariance, returned as a matrix.
A (Optional)	In	A matrix, specified as a real matrix.

Port Name	Port Type	Description
	(In/ Out)	
B (Optional)	In	B matrix, specified as a real matrix.
C (Optional)	In	C matrix, specified as a real matrix.
D (Optional)	In	D matrix, specified as a real matrix.
G (Optional)	In	G matrix, specified as a real matrix.
H (Optional)	In	H matrix, specified as a real matrix.
Q (Optional)	In	Q matrix, specified as a real scalar, vector or matrix.
R (Optional)	In	R matrix, specified as a real scalar, vector or matrix.
N (Optional)	In	N matrix, specified as a real matrix.
P0 (Optional)	In	P matrix at initial time, specified as a real scalar, vector, or matrix.
X0 (Optional)	In	Initial state estimates, specified as a real scalar or vector.
Enable (Optional)	In	Control signal to enable measurement updates, specified as a real scalar.
Reset (Optional)	In	Control signal to reset state estimates, specified as a real scalar.

Supported Data Types

- Double-precision floating point
- Single-precision floating point (for discrete-time Kalman filter only)

Note:

- All input ports except **Enable** and **Reset** must have the same data type (single or double).
- Enable and Reset ports support single, double, int8, uint8, int16, uint16, int32, uint32, and boolean data types.

Limitations

- The plant and noise data must satisfy:
 - (C,A) detectable
 - $\bar{R} > 0$ and $\bar{Q} \bar{N}\bar{R}^{-1}\bar{N}^T \ge 0$
 - $(A \overline{N}\overline{R}^{-1}C, \overline{Q} \overline{N}\overline{R}^{-1}\overline{N}^T)$ has no uncontrollable mode on the imaginary axis (or unit circle in discrete time) with the notation

$$\begin{split} & \bar{Q} = GQG^T \\ & \bar{R} = R + HN + N^T H^T + HQH^T \\ & \bar{N} = G(QH^T + N) \end{split}$$

• The continuous-time Kalman filter cannot be used in Function-Call Subsystems or Triggered Subsystems.

References

[1] Franklin, G.F., J.D. Powell, and M.L. Workman, *Digital Control of Dynamic Systems*, Second Edition, Addison-Wesley, 1990.

[2] Lewis, F., Optimal Estimation, John Wiley & Sons, Inc, 1986.

See Also

kalman

Related Examples

• "State Estimation Using Time-Varying Kalman Filter"

More About

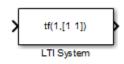
"Recursive Algorithms for Online Parameter Estimation"

Introduced in R2014b

LTI System

Use linear system model object in Simulink

Description



The LTI System block imports linear system model objects into the Simulink environment.

The imported system must be proper. State-space models are always proper. SISO transfer functions or zero-pole-gain models are proper if the degree of their numerator is less than or equal to the degree of their denominator. MIMO transfer functions are proper if all their SISO entries are proper.

Dialog Box

Tunction Block Parameters: LTI System
LTI Block (mask) (link)
The LTI System block accepts both continuous and discrete LTI models as defined in the Control System Toolbox. Transfer function, state-space, and zero-pole-gain formats are all supported in this block.
Note: Initial states are only meaningful for state-space systems.
Parameters
LTI system variable
(tf(1,[1 1])
Initial states (state-space only)
OK Cancel Help Apply

LTI system variable

Enter your LTI model. This block supports state-space, zero/pole/gain, and transfer function formats. Your model can be discrete- or continuous-time.

Initial states (state-space only)

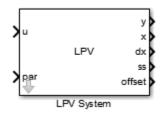
If your model is in state-space format, you can specify the initial states in vector format. The default is zero for all states.

Introduced before R2006a

LPV System

Simulate Linear Parameter-Varying (LPV) systems

Description



Represent and simulate Linear Parameter-Varying (LPV) systems in Simulink. The block also supports code generation.

A *linear parameter-varying* (LPV) system is a linear state-space model whose dynamics vary as a function of certain time-varying parameters called *scheduling parameters*. In MATLAB, an LPV model is represented in a state-space form using coefficients that are parameter dependent.

Mathematically, an LPV system is represented as:

$$dx(t) = A(p)x(t) + B(p)u(t)$$
$$y(t) = C(p)x(t) + D(p)u(t)$$
$$x(0) = x_0$$

where

- u(t) are the inputs
- y(t) the outputs
- x(t) are the model states with initial value x0
- dx(t) is the state derivative vector \dot{x} for continuous-time systems and the state update vector $x(t + \Delta T)$ for discrete-time systems. ΔT is the sample time.

- A(p), B(p), C(p) and D(p) are the state-space matrices parameterized by the scheduling parameter vector p.
- The parameters p = p(t) are measurable functions of the inputs and the states of the model. They can be a scalar quantity or a vector of several parameters. The set of scheduling parameters define the *scheduling space* over which the LPV model is defined.

The block implements a grid-based representation of the LPV system. You pick a grid of values for the scheduling parameters. At each value $p = p^*$, you specify the corresponding linear system as a state-space (**ss** or **idss**) model object. You use the generated array of state-space models to configure the LPV System block.

The block accepts an array of state-space models with operating point information. The information on the scheduling variables is extracted from the SamplingGrid property of the LTI array. The scheduling variables define the grid of the LPV models. They are scalar-valued quantities that can be functions of time, inputs and states, or constants. They are used to pick the local dynamics in the operating space. The software interpolates the values of these variables. The block uses this array with data interpolation and extrapolation techniques for simulation.

The LPV system representation can be extended to allow offsets in dx, x, u and y variables. This form is known as *affine form* of the LPV model. Mathematically, the following represents an LPV system:

$$dx(t) = A(p)x(t) + B(p)u(t) + (\overline{dx}(p) - A(p)\overline{x}(p) - B(p)\overline{u}(p))$$
$$y(t) = C(p)x(t) + D(p)u(t) + (\overline{y}(p) - C(p)\overline{x}(p) - D(p)\overline{u}(p))$$
$$x(0) = x_0$$

 $\overline{dx}(p)$, $\overline{x}(p)$, $\overline{u}(p)$, $\overline{y}(p)$ are the offsets in the values of dx(t), x(t), u(t) and y(t) at a given parameter value p = p(t).

You obtain such representations of the linear system array by linearizing a Simulink model over a batch of operating points (see "Batch Linearization" in Simulink Control Design documentation.) The offsets then correspond to the operating points at which you linearized the model.

The following limitations apply to the LPV System block:

- Internal delays cannot be extrapolated to be less than their minimum value in the state-space model array.
- When using an irregular grid of linear models to define the LPV system, only the nearest neighbor interpolation scheme is used. This may reduce the accuracy of simulation results. It is recommended to work with regular grids. To learn more about regular and irregular grids, see "Regular vs. Irregular Grids".

Data Type Support

Single and double data. You must convert any other data type for input signals or model properties to these data types.

Parameters

The LPV System Block Parameter dialog box contains five tabs for specifying the system data, scheduling algorithm and output ports. The following table summarizes the block parameters.

Task	Parameters
Specify an array of state-space models and initial states	In LPV Model tab: State-space array
	Initial state
Specify operating point offsets	In LPV Model tab:
	Input offset
	Output offset
	State offset
Specify offsets in state derivative or update variable	in the LPV Model tab:
	State derivative/update offset
Specify which model matrices are fixed and their nominal values to override entries in	In the Fixed Entries tab:
model data.	Nominal Model
	Fixed Coefficient Indices

Task	Parameters
In some situations, you may want to replace a parameter-dependent matrix such as $A(p)$ with a fixed value A^* for simulation. For example, A^* may represent an average value over the scheduling range.	
Specify options for interpolation and extrapolation	 In the Scheduling tab: Interpolation method Extrapolation method Index search method Begin index search using previous index result
Specify additional outputs for the block	 In the Outputs tab: Output states Output state derivatives (continuous-time) or updates (discrete-time) Output interpolated state-space data Output interpolated offsets
Specify code generation settings	 In the Code Generation tab: Block data type (discrete-time case only) Initial buffer size for delays Use fixed buffer size

State-space array

An array of state-space (**ss** or **idss**) models. All the models in the array must use the same definition of states. Use the **SamplingGrid** property of the state-space object to specify scheduling parameters for the model. See the **ss** or **idss** model reference page for more information on the **SamplingGrid** property.

Initial state

Initial conditions to use with the local model to start the simulation, specified one of the following:

- 0 (Default)
- Double vector of length equal to the number of model states

Input offset

Offsets in input u(t), specified as one of the following:

- 0 (**Default**) Use when there are no input offsets ($\overline{u}(p) = 0 \forall p$).
- Double vector of length equal to the number of inputs Use when input offset is the same across the scheduling space.
- Double array of size [nu 1 sysArraySize] Use when offsets are present and they vary across the scheduling space. Here, nu = number of inputs, sysArraySize = array size of state-space array. Use size to determine the array size.

Output offset

Offsets in output y(t), specified as one of the following:

- 0 (**Default**) Use when there are no output offsets $\overline{y}(p) = 0 \forall p$.
- Double vector of length equal to the number of outputs. Use when output offsets are the same across the scheduling space.
- Double array of size [ny 1 sysArraySize]. Use when offsets are present and they vary across the scheduling space. Here, ny = number of outputs, sysArraySize = array size of state-space array. Use size to determine the array size.

State offset

Offsets in states x(t), specified as one of the following:

- 0 (**Default**) Use when there are no state offsets $\overline{x}(p) = 0 \forall p$.
- Double vector of length equal to the number of states. Use when the state offsets are the same across the scheduling space.

• Double array of size [nx 1 sysArraySize], where nx = number of states, sysArraySize = array size of state-space array. Use when offsets are present and they vary across the scheduling space. Here, nx = number of states, sysArraySize = array size of state-space array. Use size to determine the array size.

State derivative/update offset

Offsets in state derivative or update variable dx(t), specified as one of the following:

- If you obtained the linear system array by linearization under equilibrium conditions, select the **Assume equilibrium conditions** option. This corresponds to an offset of $\overline{dx}(p) = 0$ for a continuous-time system and $\overline{dx}(p) = \overline{x}(p)$ for a discrete-time system. This option is selected by default.
- If the linear system contains at least one system that you obtained under nonequilibrium conditions, uncheck the **Assume equilibrium conditions** option. Specify one of the following in the **Offset value** field:
 - If the dx offset values are the same across the scheduling space, specify as a double vector of length equal to the number of states.
 - If the dx offsets are present and they vary across the scheduling space, specify as a double array of size [nx 1 sysArraySize], where nx = number of states, and sysArraySize = array size of state-space array.

Nominal Model

State-space model that provides the values of the fixed coefficients, specified as one of the following:

• Use the first model in state-space array (**Default**:) — The first model in the state-space array is used to represent the LPV model. In the following example, the state-space array is specified by object **sys** and the fixed coefficients are taken from model **sys**(:,:,1).

```
% Specify a 4-by-5 array of state-space models.
sys = rss(4,2,3,4,5);
a = 1:4;
b = 10:10:50;
[av,bv] = ndgrid(a,b);
% Use "alpha" and "beta" variables as scheduling parameters.
```

```
sys.SamplingGrid = struct('alpha',av,'beta',bv);
```

Fixed coefficients are taken from the model sysFixed = sys(:,:,1), which corresponds to [alpha=1, beta=10]. If the (2,1) entry of A matrix is forced to be fixed, its value used during the simulation is sysFixed.a(2,1).

• Custom value — Specify a different state-space model for fixed entries. Specify a variable for the fixed model in the **State space model** field. The fixed model must use the same state basis as the state-space array in the LPV model.

Fixed Coefficient Indices

Specify which coefficients of the state-space matrices and delay vectors are fixed.

Specify one of the following:

• Scalar Boolean (true or false), if all entries of a matrix are to be treated the same way.

The default value is **false** for the state-space matrices and delay vectors, which means that they are treated as free.

• Logical matrix of a size compatible with the size of the corresponding matrix:

State-space matrix	Size of fixed entry matrix
A matrix	nx-by-nx
B matrix	nx-by-nu
C matrix	ny-by-nx
D matrix	ny-by-nu
Input delay	nu-by-1
Output delay	ny-by-1
Internal delay	ni-by-1

where, nu = number of inputs, ny = number of outputs, nx = number of states, ni = length of internal delay vector.

• Numerical indices to specify the location of fixed entries. See sub2ind reference page for more information on how to generate numerical indices corresponding to a given subscript (i,j) for an element of a matrix.

Interpolation method

Interpolation method. Defines how the state-space data must be computed for scheduling parameter values that are located away from their grid locations.

Specify one of the following options:

- Flat Choose the state-space data at the grid point closest, but not larger than, the current point. The *current point* is the value of the scheduling parameters at current time.
- Nearest Choose the state-space data at the closest grid point in the scheduling space.
- Linear Obtain state-space data by linear interpolation of the nearest 2d neighbors in the scheduling space, where d = number of scheduling parameters.

The default interpolation scheme is Linear for regular grids of scheduling parameter values. For irregular grids, the Nearest interpolation scheme is always used regardless of the choice made. to learn more about regular and irregular grids, see "Regular vs. Irregular Grids".

The Linear method provides the highest accuracy but takes longer to compute. The Flat and Nearest methods are good for models that have mode-switching dynamics.

Extrapolation method

Extrapolation method. Defines how to compute the state-space data for scheduling parameter values that fall outside the range over which the state-space array has been provided (as specified in the SamplingGrid property).

Specify one of the following options:

- Clip (**Default:**) Disables extrapolation and returns the data corresponding to the last available scheduling grid point that is closest to the current point.
- Linear Fits a line between the first or last pair of values for each scheduling parameter, depending upon whether the current value is less than the first or greater than the last grid point value, respectively. This method returns the point on that line corresponding to the current value. Linear extrapolation requires that the interpolation scheme be linear too.

Index search method

The location of the current scheduling parameter values in the scheduling space is determined by a prelookup algorithm. Select Linear search or Binary search. Each search method has speed advantages in different situations. For more information on this parameter, see the Prelookup block reference page in Simulink documentation.

Begin index search using previous index result

Select this check box when you want the block to start its search using the index found at the previous time step. For more information on this parameter. see the Prelookup block reference page in Simulink documentation.

Output states

Add x port to the block to output state values. This option is selected by default.

Output state derivatives (continuous-time) or updates (discrete-time)

Add dx port to the block to output state derivative values or update the values. This option is selected by default.

Output interpolated state-space data

Add **ss** port to the block to output state-space data as a structure. This option is selected by default.

The fields of the generated structure are:

- State-space matrices A, B, C, D.
- Delays InputDelay, OutputDelay, and InternalDelay. The InternalDelay field is available only when the model has internal delay.

Output interpolated offsets

Add offset port to the block to output LPV model offsets $(\bar{u}(p), \bar{y}(p), \bar{x}(p), \bar{dx}(p))$.

The fields of the structure are:

- InputOffset, OutputOffset, StateOffset, and StateDerivativeOffset in continuous-time.
- InputOffset, OutputOffset, StateOffset, and StateUpdateOffset in discretetime.

Block data type (discrete-time case only)

Supported data type. Use this option only for discrete-time state-space models. Specify double or single.

Initial buffer size for delays

Initial memory allocation for the number of input points to store for models that contain delays. If the number of input points exceeds the initial buffer size, the block allocates additional memory. The default size is 1024.

When you run the model in Accelerator mode or build the model, make sure the initial buffer size is large enough to handle maximum anticipated delay in the model.

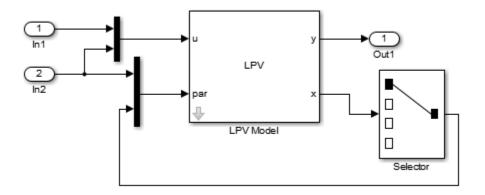
Use fixed buffer size

Specify whether to use a fixed buffer size to save delayed input and output data from previous time steps. Use this option for continuous-time LPV systems that contain input or output delays. If the buffer is full, new data replaces data already in the buffer. The software uses linear extrapolation to estimate output values that are not in the buffer.

Examples

Configure the Scheduling Parameter Input Port

Consider a 2-input, 3 output, 4-state LPV model. Use input u(2) and state x(1) as scheduling parameters. Configure the Simulink model as shown in the following figure.



Simulate a Linear Parameter-Varying System

Consider a linear mass-spring-damper system whose mass changes as a function of an external load command. The governing equation is:

$$m(u) y + c\dot{y} + k(y) y = F(t)$$

where m(u) is the mass dependent upon the external command u, c is the damping ratio, k is the stiffness of the spring and F(t) is the forcing input. y(t) is position of the mass at a given time t. For a fixed value of u, the system is linear and expressed as:

$$A = \begin{bmatrix} 0 & 1 \\ -\frac{k}{m} & -\frac{c}{m} \end{bmatrix}, B = \begin{bmatrix} 0 \\ \frac{1}{m} \end{bmatrix}, C = \begin{bmatrix} 1 & 0 \end{bmatrix}$$
$$\dot{x} = Ax + Bu, \ y = Cx$$

where $x = \begin{bmatrix} y \\ \dot{y} \end{bmatrix}$ is the state vector and **m** is the value of the mass for a given value of **u**.

In this example, you want to study the model behavior over a range of input values from 1 to 10 Volts. For each value of U, measure the mass and compute the linear representation of the system. Suppose, mass is related to the input by the relationship:

 $m(u) = 10u + 0.1u^2$. For values of u ranging from 1:10 results in the following array of linear systems.

```
% Specify damping coefficient.
c = 5;
% Specify stiffness.
k = 300;
% Specify load command.
u = 1:10;
% Specify mass.
m = 10*u + 0.1*u.^2;
% Compute linear system at a given mass value.
for i = 1:length(u)
        A = [0 1; -k/m(i), -c/m(i)];
        B = [0; -1/m(i)];
        C = [1 0];
        sys(:,:,i) = ss(A,B,C,0);
end
```

The variable u is the scheduling input. Add this information to the model.

sys.SamplingGrid = struct('LoadCommand',u);

Configure the LPV System block:

- Type sys in the State-space array field.
- Connect the input port par to a one-dimensional source signal that generates the values of the load command. If the source provides values between 1 and 10, interpolation is used to compute the linear model at a given time instance. Otherwise, extrapolation is used.

LPV Block (mask) (link) Linear Parameter Varying (LPV) Model. For "State-space array", specify an @ss object array. The SamplingGrid property of the object specifies the scheduling parameters for the model. The offsets specify the affine terms for the model's inputs, outputs, states and		
For "State-space array", specify an @ss object array. The SamplingGrid property of the object specifies the scheduling parameters for the model. The offsets specify the affine terms for the model's inputs, outputs, states and		
of the object specifies the scheduling parameters for the model. The offsets specify the affine terms for the model's inputs, outputs, states and		
state derivatives.		
LPV Model Fixed Entries Scheduling Outputs		
LTI Array		
State-space array: sys		
Initial state: 0		
Operating Point Offsets		
Input offset: 0		
Output offset: 0		

Ports

Port Name	Port Type	Description
	(In/ Out)	
u	In	Input signal u(t) in Equation 2-2 described previously. In multi- input case, this port accepts a signal of the dimension of the input.
par	In	Provides the signals for variables defining the scheduling space ("sampling grid" variables). The scheduling variables can be functions of time, inputs and states, or constants. The required dependence can be achieved by preparing a scheduling signal

Port Name	Port Type	Description
	(In/ Out)	
		using clock input (for time), input signal (u), and the outputs signals (x , dx/dt , y) of the LPV block, as required.
У	Out	Model output
x	Out	Values of the model states
xdot	Out	Values of the state derivatives. The state derivatives are sometimes used to define the scheduling parameters.
ss	Out	Local state-space model at the major simulation time steps
offset	Out	LPV model offsets

Related Examples

- "Using LTI Arrays for Simulating Multi-Mode Dynamics"
- "Approximating Nonlinear Behavior using an Array of LTI Systems"
- "LPV Approximation of a Boost Converter Model"

More About

"Linear Parameter-Varying Models"

Introduced in R2014b